
***Technique for Controlling Power-Mode
Transition Noise in Distributed Sleep
Transistor Network***

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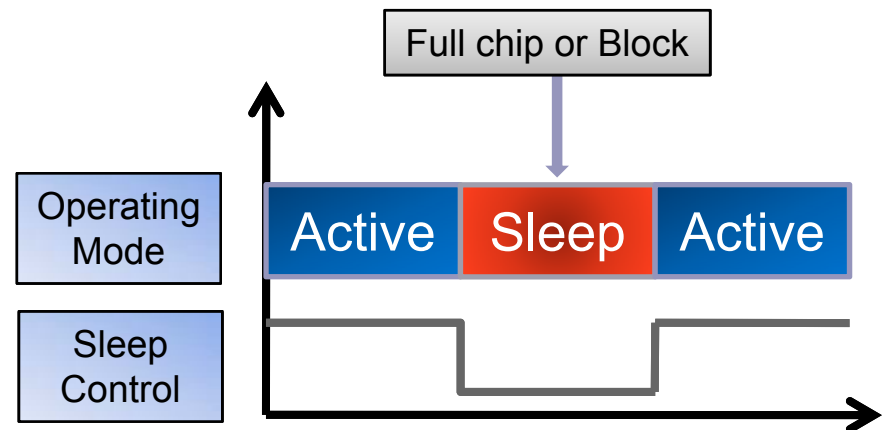
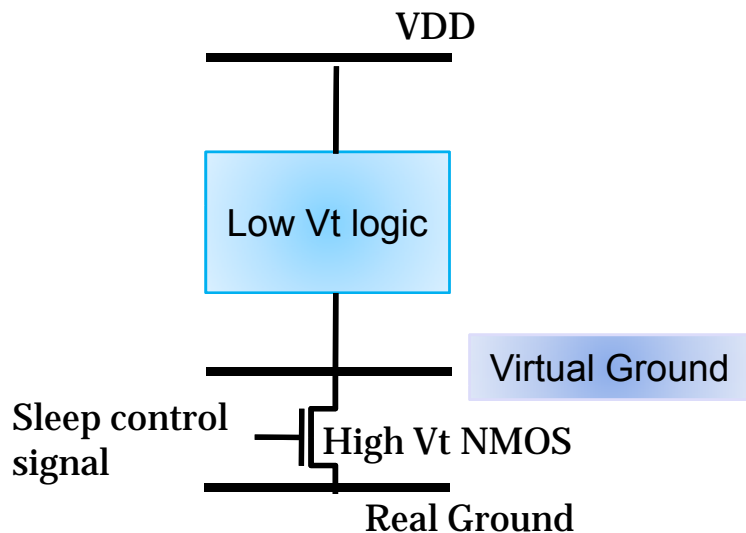
Outline

- Introduction
- Related Work
- Motivation example
- The proposed algorithm
- Experimental results
- Conclusion

Power Gating on Circuits

- Basic idea

- Reduce the leakage power by inserting power gating cell(s) into the power or ground nets



Design Issues in Power Gated Logic Circuit

● Active mode

- IR drop between source and drain node of sleep transistor
- Sleep transistor overhead

● Sleep mode

- State retention FFs

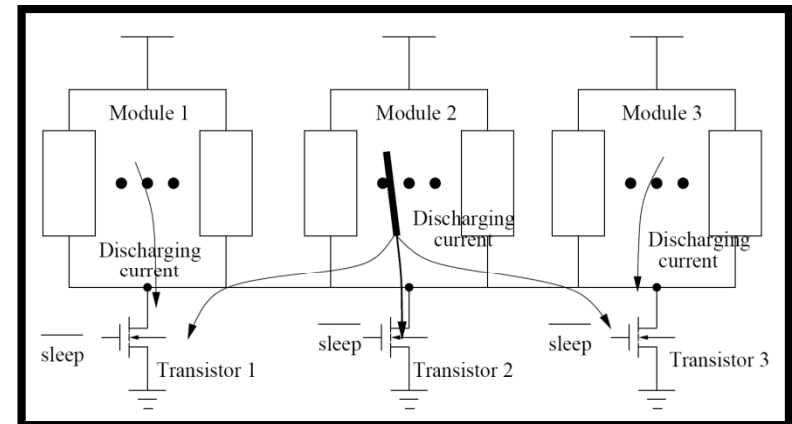
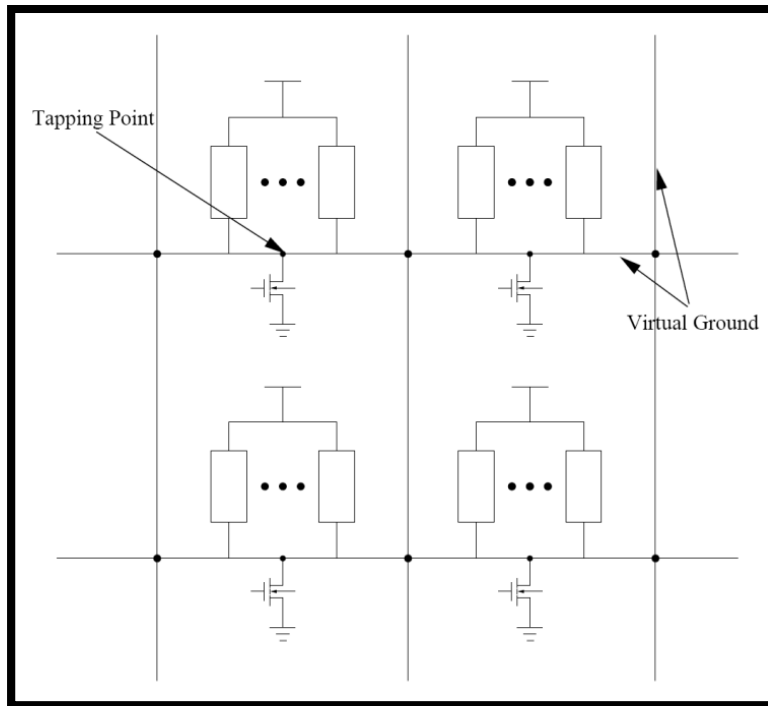
● Mode transition

- Wakeup delay
- Huge discharging current
 - Accumulated charges in '0' state nodes and virtual ground rail
 - Short circuit current

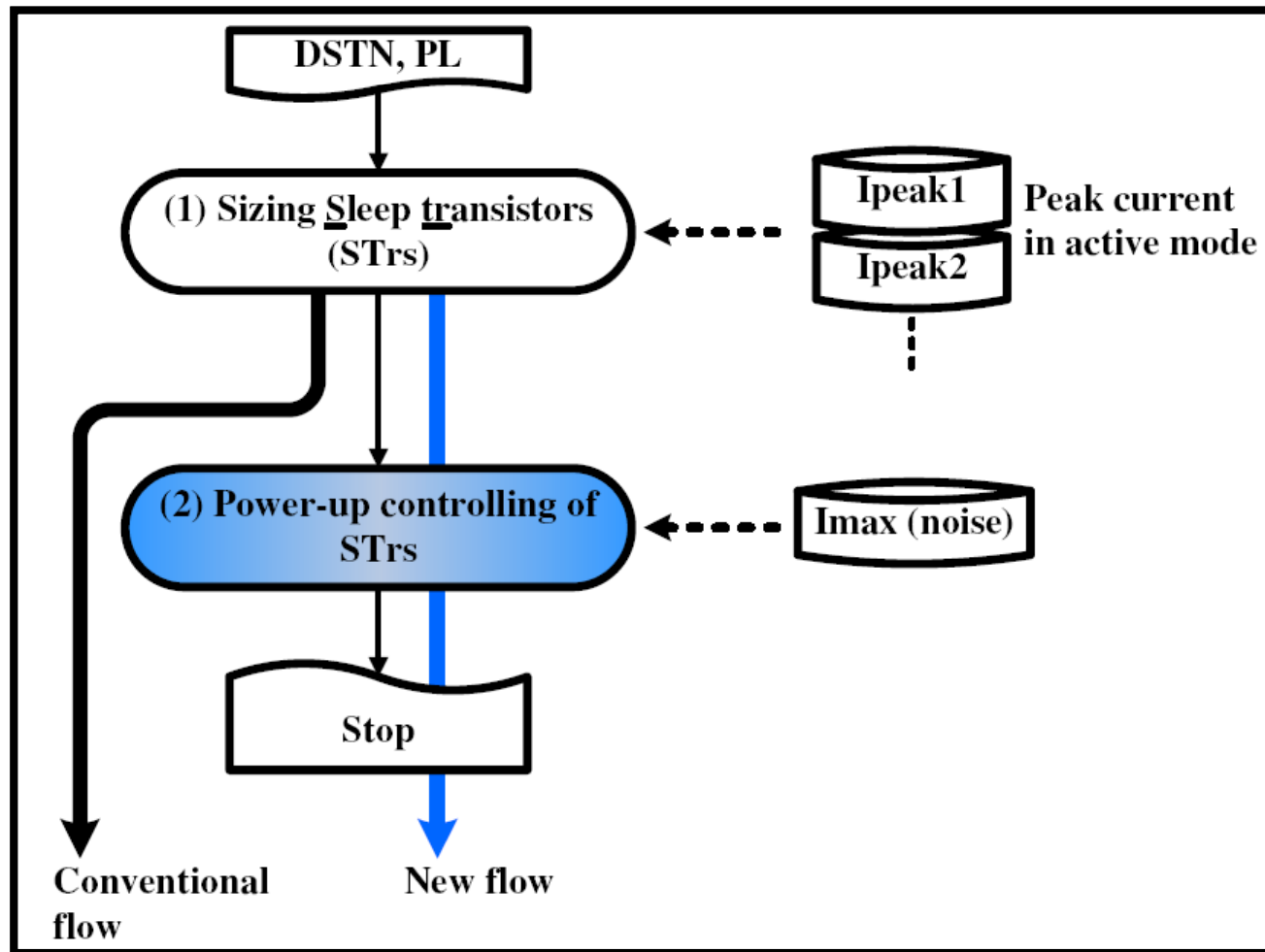
Related work

- Sleep transistor design
 - Module based [5]– centralized sleep transistor design
 - Large interconnect resistance of virtual ground
 - Cluster based [6]
 - Design overhead
 - **Distributed sleep transistor network: DSTN** [7]
 - **Current balancing effect, PVT tolerance**
- Sleep transistor sizing
 - Based on MSSC & PL [8]
 - Average current method [11]
 - Path based switching current method [12]
- Mode transition noise
 - Wakeup order scheduling of power gated blocks in system level [13]
 - Incremental turn-on scheme; gradually or sequentially [3]
 - Logic cell clustering method [14]

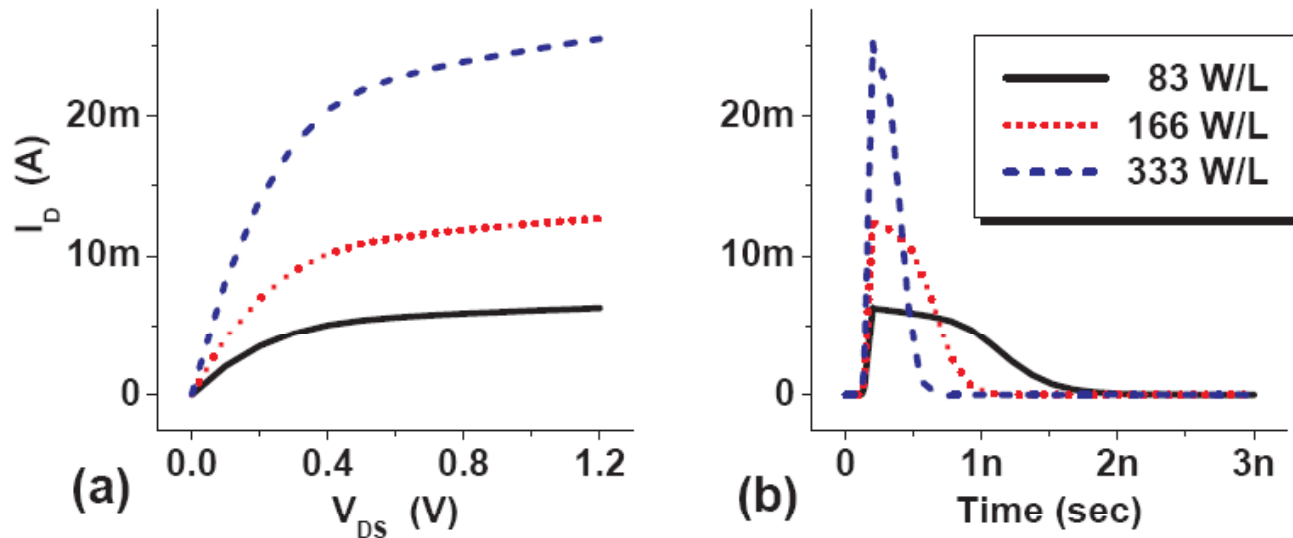
DSTN: distributed sleep transistor network



Design flow of power gated circuits



Characteristics of sleep transistors



$$I_D = \begin{cases} 0 & (V_{GS} \leq V_t : \text{cutoff region}) \\ \frac{K}{2} \{ (2V_{GS} - V_t)V_{DS} - V_{DS}^2 \} (1 + \lambda V_{DS}) & (V_{DS} < V_{SAT} : \text{linear region}) \\ \frac{K}{2} (V_{GS} - V_t)^2 (1 + \lambda V_{DS}) & (V_{DS} \geq V_{SAT} : \text{saturation region}) \end{cases}$$

$$K = \mu_n C_{ox} (W/L)$$

Sleep transistor sizing

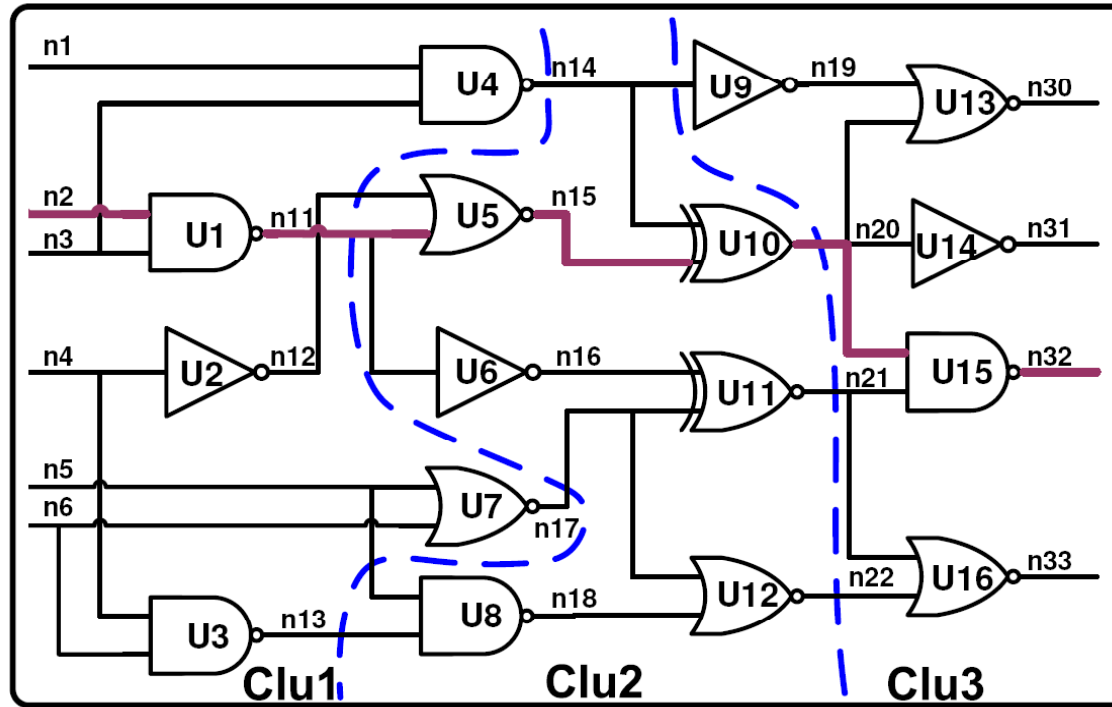
$$\left(\frac{W}{L}\right)_{STr, total} = \frac{I_{STr, total}(t)}{\delta\mu_n C_{ox} (V_{DD} - V_{tl})(V_{DD} - V_{th})}$$

$$I_{STr, total}(t) = \sum_{i \in gates} I_{STr, i}(t)$$

$$I_{STr, total}(t) \leq I_{MSSC}$$

Relation between:

Sleep transistor size and switching current



	Original circuit	Power gated circuit	
	Switching current [mA]	Size [W/L]	Delay increase[%]
CASE1	1.98	75	2.3
CASE2	0.78	29	4.5

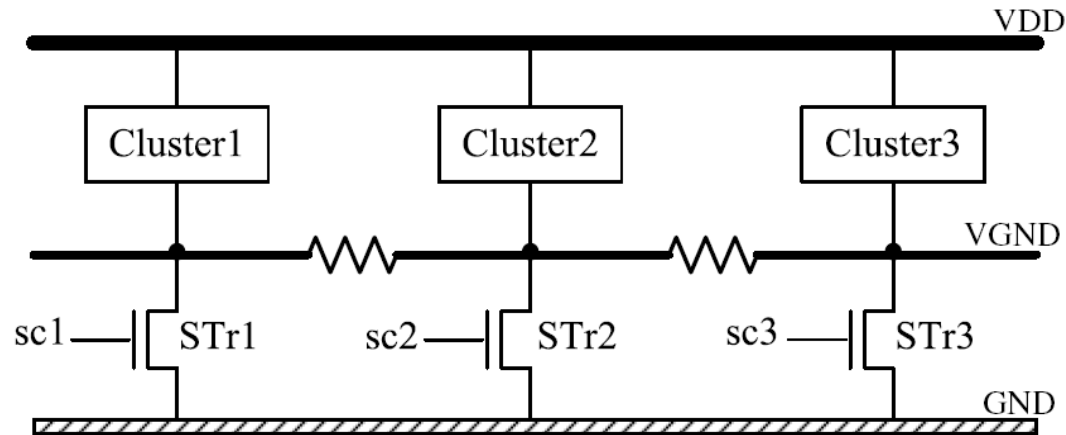
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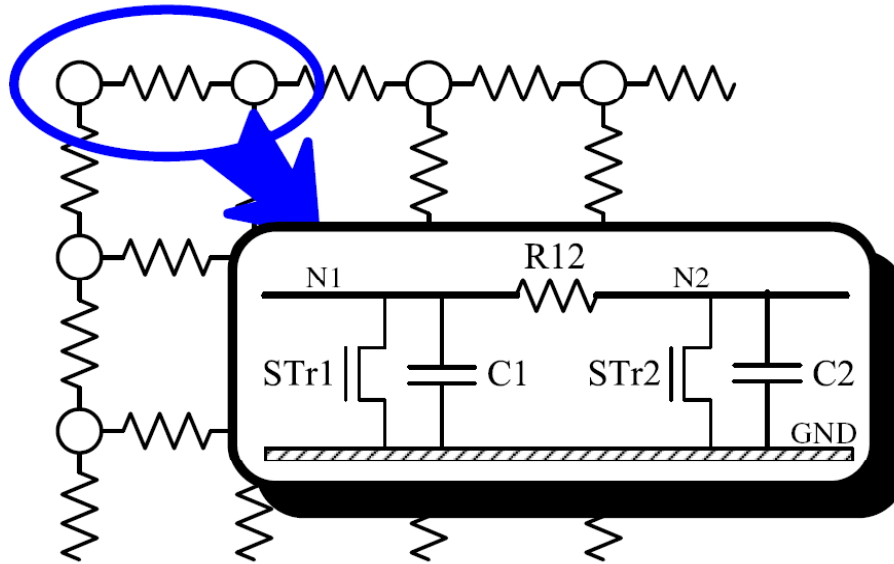
Relation between:

Power mode trans. noise & sleep transistor size

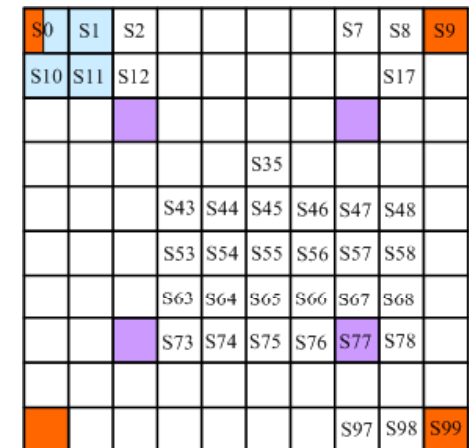


Combinations of STr to be turned on	Peak value [mA]	
	Case1	Case2
STR1 + STR2 + STR3	4.73	2.30
STR1 + STR2	3.83	1.64
STR1	1.96	0.79
STR2	2.19	0.89
STR3	1.79	0.72

Power-up controlling of sleep transistors



Sleep transistor location	Delay [ns]	Ratio
Loc1 ¹	4.17	1
Loc2 ²	3.96	0.95
Loc3 ³	3.84	0.92



Unate Covering Problem (UCP)

- Method for the two level logic optimization
 - Given a Boolean function f , find a minimum SOP formula
- Let $M_{m \times n}$ be a Boolean matrix, the UCP is to find a minimum number of columns to cover M in the sense that any row with a 1-entry has at least one of its 1-entries covered by these columns.

UCP example

$$f(w, x, y, z) = x' y' + wxy + x' yz' + wy' z$$

	wxy	wxz	wyz'	wy'z	x'y'	x'z'
wx'y'z'					1	1
w'x'y'z					1	
w'x'y'z'					1	1
wxyz	1	1				
wxyz'	1		1			
wx'yz'			1			1
w'x'yz'						1
wxy'z		1		1		
wx'y'z				1	1	

Solutions to UCP:

$\{x' y', x' z', wxy, wxz\}$

UCP example

$$f(w, x, y, z) = x' y' + wxy + x' yz' + wy' z$$

	wxy	wxz	wyz'	wy'z	x'y'	x'z'
wx'y'z'					1	1
w'x'y'z					1	
w'x'y'z'					1	1
wxyz	1	1				
wxyz'	1		1			
wx'yz'			1			1
w'x'yz'						1
wxy'z		1		1		
wx'y'z				1	1	

Solutions to UCP:

$\{x' y', x' z', wxy, wxz\}$

UCP example

$$f(w, x, y, z) = x' y' + wxy + x' yz' + wy' z$$

	wxy	wxz	wyz'	wy'z	x'y'	x'z'
wx'y'z'					1	1
wx'yz					1	
w'x'yz'					1	1
wxyz	1	1				
wxyz'	1		1			
wx'y'z			1			1
w'x'yz						1
wxy'z		1		1		
wx'y'z				1	1	

Solutions to UCP:

$\{x' y', x' z', wxy, wxz\}$

UCP formulation

S0	S1	S2					S7	S8	S9
S10	S11	S12						S17	
				S35					
		S43	S44	S45	S46	S47	S48		
		S53	S54	S55	S56	S57	S58		
		S63	S64	S65	S66	S67	S68		
		S73	S74	S75	S76	S77	S78		
						S97	S98	S99	

(a) Cover range of sleep transistor

	S0	...	S8	...	S55	S99
C0	1								
C1	1								
...									
C7			1						
C8			1						
C9			1						
C10	1								
...									
C17			1						
...									
C64					1				
C65					1				
C66					1				
...									
C99									1

(b) Constraint matrix of (a)

UCP solution d_j ; a disjoint subset of sleep transistors

$$D = \{ d_1, d_2, \dots \}$$

$$T = \{ t_1, t_2, \dots \}$$

$$\text{Schedule } T, \quad t_1 \leq t_2 \leq \dots, \quad I_T \leq I_{\max}$$

Experimental setup

- Implemented the proposed algorithm in C++
- Tested on a set of ISCAS benchmark circuits
- Decomposed with INV, NAND2, NOR2, XOR2, XNOR2
- Simulated with 130nm standard cell library
- Controlled input vectors using SAT formulation

Experimental Results:

Sleep transistor sizing

● PL: 5%

Circuit	#PI	#gate	LONG [7] [W/L]	STSizing [W/L]	Ratio
c432	36	176	353.58	120.17	33.99
c880	60	332	536.58	278.14	51.84
c1355	41	201	347.42	164.11	47.24
c1908	33	244	373.92	112.84	30.18
c2670	233	455	600.25	398.78	66.44
c3540	50	996	883.83	378.11	42.78
c5315	178	1,295	1,878.33	1,060.00	56.43
c7552	207	1,219	1,593.83	1,048.65	65.79
Avg.					49.34

Experimental Results:

Power-mode transition noise controlling

		LONG [7]					
		CONV		SEQ		STC	
circuit	I_{max} [mA] (W/L)	I [mA]	$T_{wakeup}(ns)$	I [mA]	$T_{wakeup}(ns)$	I [mA]	$T_{wakeup}(ns)$
c432	10 (116)	28.39	1.54	9.75	2.24	9.71	1.72
c880	14 (165)	43.77	1.78	13.08	2.89	13.96	2.07
c1355	9 (105)	28.43	1.10	8.99	2.60	8.94	1.45
c1908	10 (116)	30.74	1.07	8.90	2.56	9.91	1.56
c2670	15 (175)	49.71	1.98	14.12	3.41	14.43	2.37
c3540	20 (232)	74.74	2.72	19.93	5.79	19.95	3.61
c5315	40 (457)	154.41	1.90	39.95	3.94	39.91	2.46
c7552	34 (417)	132.08	2.71	33.04	5.10	33.74	3.39

		STSizing (Section V)					
		CONV		SEQ		STC	
circuit	I_{max} [mA] (W/L)	I [mA]	$T_{wakeup}(ns)$	I [mA]	$T_{wakeup}(ns)$	I [mA]	$T_{wakeup}(ns)$
c432	10 (116)	9.04	2.03	9.04	2.03	9.04	2.03
c880	14 (165)	23.53	1.99	13.28	3.86	13.98	2.15
c1355	9 (105)	13.96	1.29	8.52	3.04	8.75	1.49
c1908	10 (116)	9.91	1.74	9.91	1.74	9.91	1.74
c2670	15 (175)	33.62	2.05	14.97	4.03	14.92	2.41
c3540	20 (232)	33.90	3.22	19.93	7.17	19.97	3.62
c5315	40 (457)	89.42	2.13	37.22	5.24	39.51	2.58
c7552	34 (417)	88.59	2.89	31.40	5.43	33.63	3.46

Conclusion

- Mode transition noise should be limited for a reliable system
- Peak value of discharging current depends on sleep transistor size
- **Sleep transistor size can be reduced by using worst delay path aware approach**
- Reduced sleep transistor size **reduces the peak value of discharging current**
- To meet the constraint of mode transition noise, **clustering method of sleep transistors** is proposed using **UCP formulation**

Thank you

Input Vector Formulation

- The quantity to be minimized

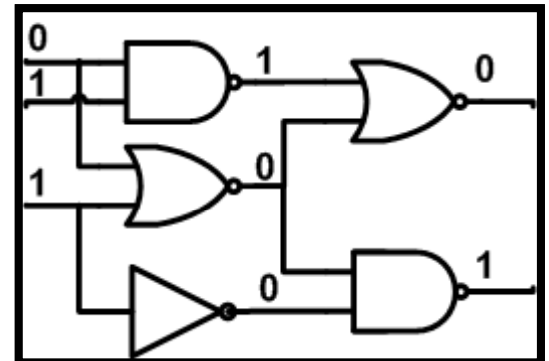
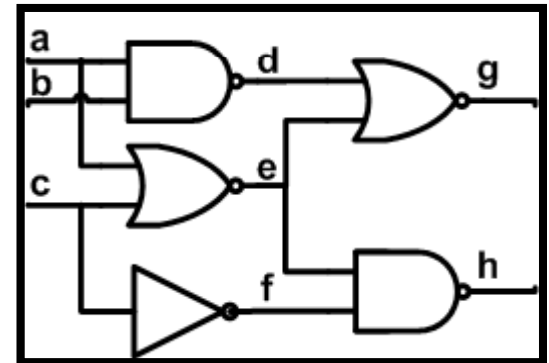
$$Q = \sum_{n_i \in \text{gates}} \# \text{fanout}(n_i) \cdot VDD \cdot \gamma(n_i)$$

- SAT formulation with Pseudo Boolean expression

- $c_1 l_1 + c_2 l_2 + \dots \leq T$

- c_i , T is constant

- l_i is literal of Boolean decision variables of SAT solver



CNF expression

$$\begin{aligned} &(a+d) \cdot (b+d) \cdot (\bar{a} + \bar{b} + \bar{d}) \cdot \\ &(\bar{a} + \bar{e}) \cdot (\bar{c} + \bar{e}) \cdot (a + c + e) \cdot \\ &(c+f) \cdot (\bar{c} + \bar{f}) \cdot \\ &(\bar{d} + \bar{g}) \cdot (\bar{e} + \bar{g}) \cdot (d + e + g) \cdot \\ &(e+h) \cdot (f+h) \cdot (\bar{e} + \bar{f} + \bar{h}) = 1 \end{aligned}$$

Cost function

$$\text{Min} \{ d + 2e + f + g + h \}$$

Solution:

Input vector : $a = 0, b = 1, c = 1$
of 1 : 2