

# Constrained Global Scheduling of Streaming Applications on MPSoCs

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# Synchronous data flow (SDF) preliminaries

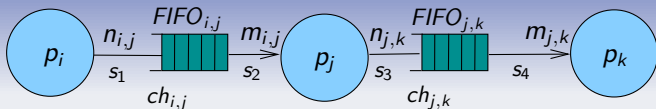


Figure: An example streaming application in SDF model.

- Process, channel, FIFO, and the “synchronous” name
- Computation  $T = [t_{C,i}, t_{C,j}, t_{C,k}]$  and storage  $\Gamma = [\gamma_{i,j}, \gamma_{j,k}]$
- Consistency, e.g.,  $r_i \cdot n_{i,j} = r_j \cdot m_{i,j}$  in  $ch_{i,j}$ ; avoid auto-concurrency

# Architecture model

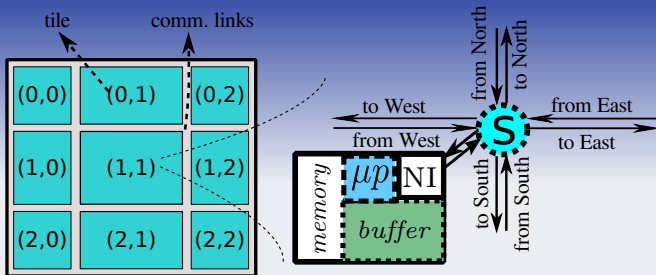


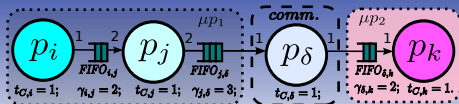
Figure: A  $3 \times 3$  regular 2-D mesh MPSoC architecture.

- Each tile consists of a processor ( $\mu p$ ), an application *memory*, a token *buffer*, and a network interface (NI).
- Hard real-time NoC infrastructure: switches (*s*) and links.

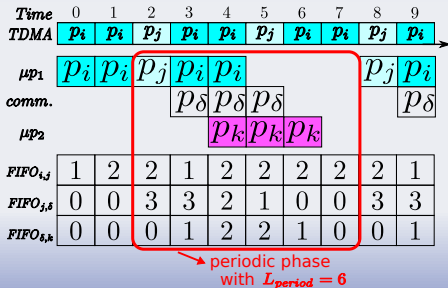
**Problem statement:** the analysis of routing, scheduling, and buffer properties, based a **fixed** allocation from processes to tiles.

# Motivation – different scheduling schemes

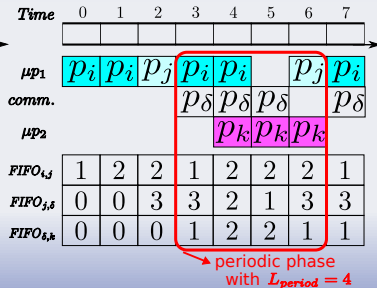
(0) Application allocated onto buffer constrained dual-processor.



(1) TDM scheduling scheme.



(2) Throughput optimized scheduling.



- OH in TDM-like schemes causes sub-optimal: throughput vs. buffer
- Contributions:** **compu. & comm.** global scheduling for MPSoCs

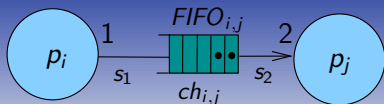
# Outline

- 1 Related Work
- 2 Constraint based Analysis
- 3 Experimental Results
- 4 Conclusion

# Related Work

- **Heuristic** scheduling of **task graphes** on distributed systems with comm. protocols optimization [Eles et al., TVLSI '00];
- For SDF models, to construct heuristic periodic admissible parallel schedules (PAPS) on multi-processors [Lee and Messerschmitt, 1987a], **without** constraints on buffers and throughput.
- Stuijk et al. [DAC '07] propose a mapping and **TDMA/list** scheduling design flow for throughput constrained SDF applications on MPSoCs, which is argued about the OH and lacking of global optimization on performance metrics.
- Inspiring work: **model-checker** determines the minimal deadlock-free buffer of SDF models (**no computation constraints**) [Geilen et al., DAC '05]; Liu et al. [RTSS '08] use **SAT-solver** to explore the mapping and scheduling of homogeneous SDF (**HSDF**) models on multi-processors to **maximize** application throughput.

# Event Models [Zhu et al., DATE '09]



time tag	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
$p_i$	1	1					0				1	1		0	
$p_j$		4	3	2	1			0			4	3	2	1	0
$FIFO_{i,j}$	3	4	4	4	2	2	2	2	2	2	3	4	4	4	2

## Cumulative functions [Cruz1995]:

Arrival function  $R_{i,j}(t) = \sum_0^t s_1$

Service function  $C_{i,j}(t) = \sum_0^t s_2$

Output function  $R'_{i,j}(t) = R_{i,j}(t)$

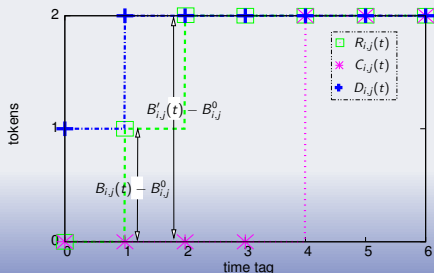
Demand function

$$D_{i,j}(t) = \begin{cases} \sum_0^t s_1 + n_{i,j}, & p_i \text{ computing} \\ \sum_0^t s_1, & p_i \text{ stalling} \end{cases}$$

## Buffer Properties:

Buffer backlog  $B_{i,j}(t)$

Buffer requirement  $B'_{i,j}(t)$



J. Zhu, I. Sander, and A. Jantsch.

Buffer minimization of real-time streaming applications scheduling on hybrid CPU/FPGA architectures.

DATE '09.

# Constraint based analysis

Our declarative scheduling method considers

- Execution semantics of SDF models [Zhu et al., DATE '09]:  
e.g., static token rates, asynchronous buffer
- Resource constraints: binding applications onto target MPSoC platforms
  - application to architecture mapping (be aware)
  - computation scheduling
  - communication routing and flow control
  - performance metrics, e.g., buffer cost and real-time constraints



# Mapping

Mapping decision  $\alpha_{i,\mu p_n}$ : denotes the presence of  $p_i$  on  $\mu p_n$

## Constraint (Single residence)

$$\sum_{\mu p_n \in \mathbf{U}} \alpha_{i,\mu p_n} = 1, \quad \forall p_i \in \mathbf{P} \quad (1)$$

Although mapping is fixed, scheduling needs to be mapping-decision aware

## Constraint (Mapping & scheduling association)

*Sequential execution of processes on each processor, and the mapping and scheduling association:*

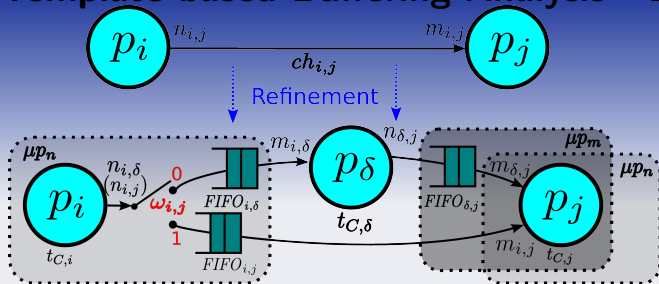
$$\sum_{p_i \in \mathbf{P}} \alpha_{i,\mu p_n} W_j(t) \in \{0, 1\}, \quad \forall \mu p_n \in \mathbf{U}, t \in \mathbb{N}_0 \quad (2)$$

*in which  $W_j(t)$  denotes the **1-0** (computing) status of  $p_j$ .*

$$W_j(t) = \max(L_j(t), L_j(t + \Delta_t)), \quad \forall \Delta_t \in [1, t_{c,j}] \quad (3)$$

$$L_j(t + 1) = \frac{C_j(t + 1) - C_j(t)}{m_{i,j}} \in \{0, 1\}$$

# Template based Buffering Analysis - 1



**Figure:** A template of producer-consumer refinement.  $\omega_{i,j}$  (correlated with  $\alpha$ ) denotes whether  $ch_{i,j}$  is an intra-processor channel.

Some constraints on FIFOs can be formalized, e.g.,

## Property (Buffer usage)

The FIFO usages of  $FIFO_{i,\delta}$  at time tag  $t$  is denoted as  $B_{i,\delta}(t)$ :

$$B_{i,\delta}(t) = D_{i,\delta}(t) - \neg\omega_{i,j}(C_{i,\delta}(t) - B_{i,\delta}^0) - \omega_{i,j}(C_{i,j}(t) - B_{i,j}^0) \quad (4)$$

in which  $B_{i,\delta}^0(t)$  is the initial data tokens.

## Template based Buffering Analysis - 2

Different FIFOs on the same tile can be implemented as either disjoint or shared buffer partitions.

### Property (Buffer cost $\gamma_{Sum'}$ – disjoint partition)

$$\gamma_{Sum'} = \sum_{i,j,\delta} (\omega_{i,j} \gamma_{i,j} + \neg \omega_{i,j} (\gamma_{i,\delta} + \gamma_{\delta,j})), \quad \forall p_i, p_j \in \mathbf{P} \quad (5)$$

$$\text{where } \gamma_{i,j} \geq B_{i,j}(t), \gamma_{i,\delta} \geq B_{i,\delta}(t), \gamma_{\delta,j} \geq B_{\delta,j}(t), \quad \forall t \in \mathbb{N}_0$$

in which  $\gamma_{i,j}$ ,  $\gamma_{i,\delta}$ , and  $\gamma_{\delta,j}$  denote the sizes of FIFOs in the template.

### Property (Buffer cost $\gamma_{Sum''}$ – shared partition)

$\gamma_{Sum''}$  is the sum of the shared buffer space on individual tiles.

$$\gamma_{Sum''} = \sum_n \gamma_{tile_n} \quad (6)$$

$$\text{where } \gamma_{tile,n} \geq \sum_{i,j} (a_{i,\mu p_n} B_{i,\delta}(t) + a_{j,\mu p_n} B_{\delta,j}(t) + a_{i,\mu p_n} \omega_{i,j} B_{i,j}(t))$$

The total buffer cost  $\gamma_{Sum'} \geq \gamma_{Sum''}$ .

# Routing and flow control - 1

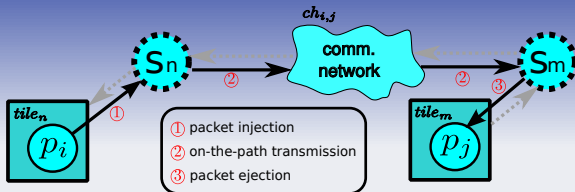


Figure: Three phases to route a packet in inter-tile channel  $ch_{i,j}$ .

- Assuming deterministic X-Y routing on NoC, routing decisions are in  $\beta^r$  and  $\beta^c$  on **rows** and **columns** with corresponding constraints.
- In hard-real time NoC (contention-free), a packet (data token) reserves a circuit switching before the transmission finishes, e.g., in  $\mathcal{A}etheral$  [Goossens et al., '05 IEEE Des. Test].

## Routing and flow control - 2

- Different application flows sharing the same NoC links are scheduled temporally to avoid contention in: packet injection (see Eq. 7), ejection, and inter-tile traffic flow (for rows of links see Eq. 8)

### Constraint (Contention-free traffic flow scheduling)

$$\sum_i \alpha_{i, \mu p_n} W_\delta(t) \in \{0, 1\}, \quad (7)$$

$$\sum_{i,j} \beta_{ch_{i,j}, l_k}^r W_\delta(t) \in \{0, \pm 1\}, \quad \sum_{i,j} |\beta_{ch_{i,j}, l_k}^r| W_\delta(t) \in \{0, 1, 2\}, \quad (8)$$

$$\forall p_i, p_j \in \mathbf{P}, \mu p_n \in \mathbf{U}, t \in \mathbb{N}_0$$

with  $W_\delta(t)$  to denote the data transmission **1-0** (working or idle) status on NoC modeled by  $p_\delta$ .

## Real-time constraints

The efficient execution means the streaming services are delivered on-demand to the end-user, neither too fast nor too slow.

### Constraint

*(Application output throughput) After some start-up time period  $\tau_0$  ( $\tau_0 > 0$ ) with no stable output tokens, a specified output throughput  $\rho_{out}$  should be sustained at the application sink process  $p_j$ .*

$$C_j(\tau_0 + k \cdot L_{period}) - C_j(\tau_0) = k \cdot J \cdot r_j \cdot m_{i,j}, \forall k \in \mathbb{N}_0 \quad (9)$$

*Empirically,  $L_{period} = \lceil \frac{J \cdot r_k \cdot m_{i,j}}{\rho_{out}} \rceil$ ,  $J \in \mathbb{N} \setminus \{\infty\}$ , in which  $J$  is incremental and leads to an valid  $L_{period}$ .*

Furthermore, throughput is guaranteed by periodic phase checking.

# Constraint programming techniques

- CP (**Gecode**) has been successful to solve NP-complete problems.
- Problems are defined by: variables, domains, and constraints.
- Some efficient modeling techniques in solutions finding:
  - **Redundant variables and constraints.** E.g., redundant mapping decision variables.
  - **Domain and constraints reduction.** E.g., lower bounds for FIFOs, constraints are checked in  $t \in [0, \tau_0 + L_{period}]$  once periodic phase happens.
  - **Branching and exploration.** To construct the search tree, the branching variables are prioritized as follows:  $\gamma_{Sum'}$  ( $\gamma_{Sum''}$ ),  $\gamma_{tile_n}$ , and  $C$ . Empirically, the exploration starts with minimal values for all variables

# Experimental Results - 1

Table: Comparison of scenarios with varying OH. ( $3 \times 3$  platform).

<i>specification</i>				<i>SCP-OH<sup>a</sup></i>		<i>SCP</i>	
<i>app.</i>	<i>#<sup>b</sup></i>	<i>thru. req.</i>	<i>J</i>	$\gamma_{Sum'}(\gamma_{Sum''})$	<i>time<sup>c</sup></i>	$\gamma_{Sum'}(\gamma_{Sum''})$	<i>time<sup>c</sup></i>
<b>Modem</b>	2	3.125e-2	1	- <sup>d</sup>	352	98(45)	3.0e3
	2	1.667e-2	1	98(46)	5.0e3	92(41)	1.4e3
<b>Wireless</b>	2	2.5e-2	1	-	422	121(53)	4.7e4
	2	1.7e-2	1	123(49)	6.4e5	120(48)	1.2e3

<sup>a</sup> 50% OH in computation latency, plus 100% OH in communication latency.

<sup>b</sup> The number of application instances mapped onto platform.

<sup>c</sup> The solutions finding time (*ms*), branched and explored with  $\gamma_{Sum'}$  and  $\gamma$ .

<sup>d</sup> The problem is infeasible.



# Experimental Results - 2

Table: Comparison of scheduling methods ( $2 \times 2$  platform).

specification			PAPS			SCP		
app.	#	thru. req.	J	$\gamma_{Sum}'(\gamma_{Sum}'')$	time	J	$\gamma_{Sum}'(\gamma_{Sum}'')$	time'(time'') <sup>a</sup>
Bipartite	1	1.101e-1	3	510(510)	120	3	36(31)	2.6e3(2.3e5)
	1	1.096e-1	2	352(352)	50	1	36(31)	1.8e3(1.4e5)
	1	1.082e-1	1	194(194)	20	1	36(28)	1.9e3(2.1e5)
Cd2dat	2	2.462e-1	-	-	-	1	68(34)	1.9e3(4.7e4)
	2	1.553e-1	2	2926(1504)	430	1	66(34)	1.8e3(3.3e5)
	2	1.550e-1	1	1472(762)	120	1	66(34)	1.9e3(3.3e5)
H263	2	2.103e-4	-	-	-	1	9512(9506)	9.7e3(2.3e5)
	2	2.102e-4	2	19016(19012)	2.0e5	1	9512(9506)	9.5e3(2.3e5)
	2	2.101e-4	1	9512(9508)	2.4e4	1	9512(9506)	9.2e3(2.1e5)

<sup>a</sup> The solutions finding time (ms) branched and explored with two buffer measurements.

# Conclusions & future work

## Conclusions:

- 1 We present a constraint based global scheduling framework for SDF streaming application on NoC based MPSoCs.
- 2 The global scheduling for both processors computing and communication flow control has been achieved.
- 3 It shows higher predictable application throughput and with minimized buffer cost.

## Future work:

- 1 Caused by the complexity of scheduling, we plan to combine heuristics with our constraint based techniques, e.g., using heuristics to explore the search tree.
- 2 To explore parallel search with multiple threads in *Gecode* on multi-core workstations.

Thanks for your attention!

Questions?