

Obstacle-Aware Longest Path using Rectangular Pattern Detouring in Routing Grids

Jin-Tai Yan, Ming-Ching Jhong and Zhi-Wei Chen



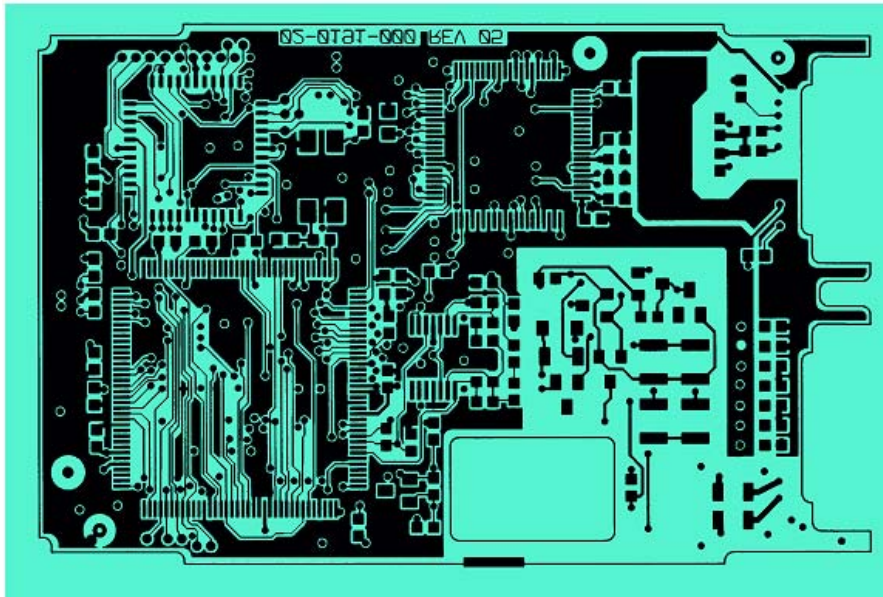
**Department of Computer Science
& Information Engineering
Chung Hua University, Taiwan**

Outline

- Introduction
- Problem Formulation
- Rectangular Pattern Detouring
- Obstacle-Aware Longest-Path in Routing Grids
- Experimental Results
- Conclusions

Introduction

- More than thousands of pins are involved in modern PCBs.
- Routing methods are complex under various design constraints, ex: length matching, coupling control...etc.
- Physical “obstacles” on PCB
 - Component mounting pads: DIP / SMD
 - Pre-route predictions: analog / TTL design reservation



Motivation & Contributions

- The length controllability of a net decides
 - Routing delay of the net
 - Ability to meet the length-matching constraint
- An effective generation for the longest path gives
 - Grid-based global routing for a single net in PCB
 - Consideration of obstacles on PCB
 - Use of Rectangular pattern detouring for the reduction of the routing time

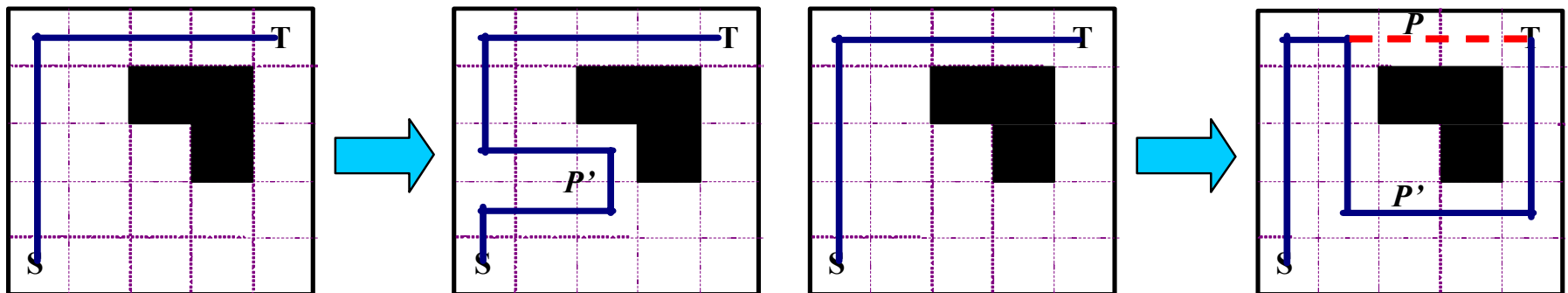
Preliminary

- Routing path

- Two grids are specified as the locations of the start and target terminals, **S** and **T**
- A **path** connects **S** and **T** by using horizontal or vertical segments and passes each available grid at most once
- The **length** of a connecting path is defined as the number of passed grids in the routing path

- Flip operations for path detouring

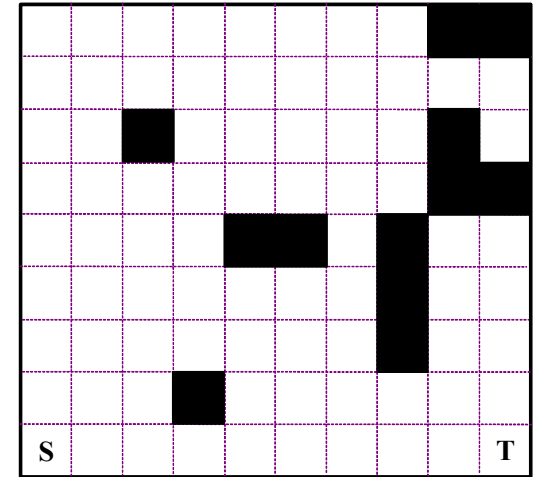
- **R-flip**: A partial path can be detoured by using adjacent routing grids and inserting a detouring path, P'
- **C-flip**: A partial path, P , can be replaced by using another partial path, P' , where the length of P' is larger than that of P



Problem Formulation

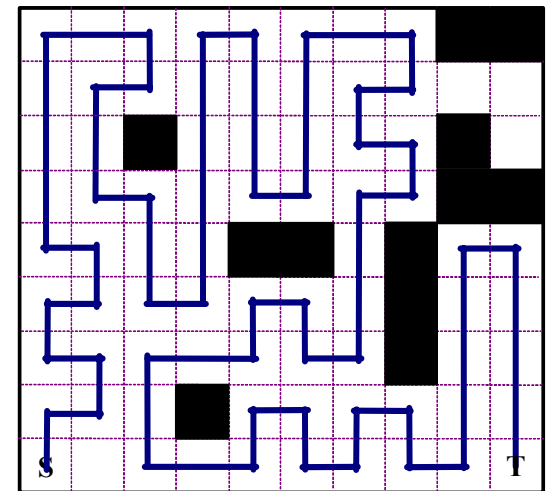
[Input]

- A single routing layer in routing grids
- A start terminal, **S**, and a target terminal, **T**, in **m** \times **n** routing grids
- A set of obstacles



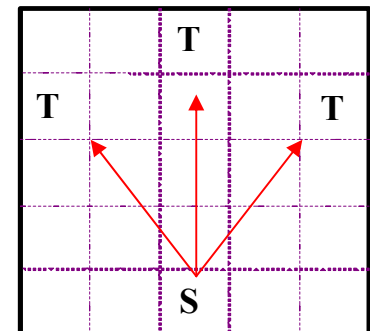
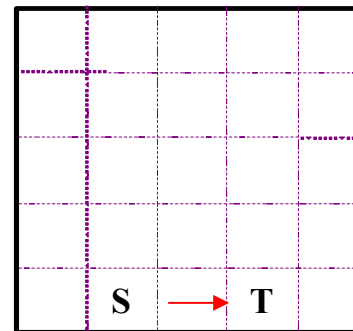
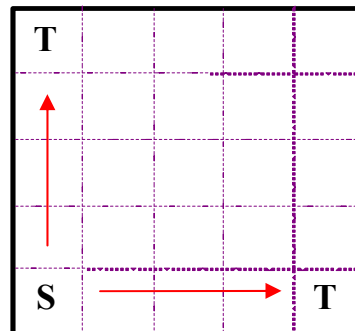
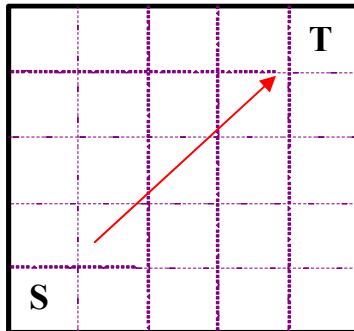
[Output]

- The longest path that passes the available routing grids from **S** to **T**



Rectangular Pattern Detouring

- Given a set of $m \times n$ routing grids without any obstacle, all the possible detouring results are considered as follows:
 - Both S and T are located on corners
 1. (Cond. I) In different sides
 2. (Cond. II) In the same side
 - S and T are located on boundaries but not on corners
 1. (Cond. III) In the same side
 2. (Cond. IV) In different sides



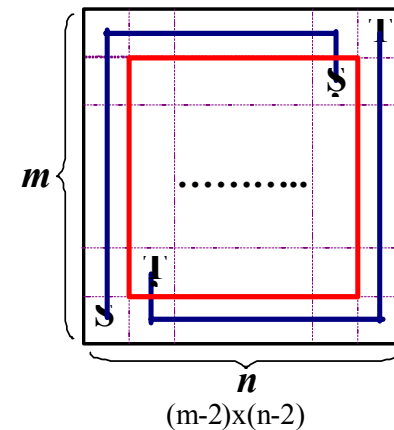
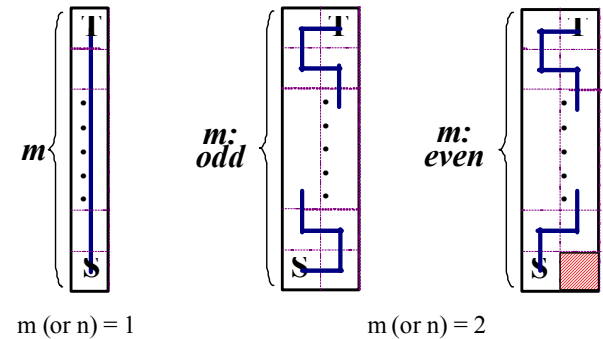
Cond. I: Corners in Different Sides

If (m or $n = 1$) \rightarrow straight path

If (m or $n = 2$) \rightarrow snaking path

If (m and $n \geq 3$)

- $m \times n$ routing grids for corners in different sides
 - Two L-type routing paths, and
 - $(m-2) \times (n-2)$ routing grids for corners in different sides

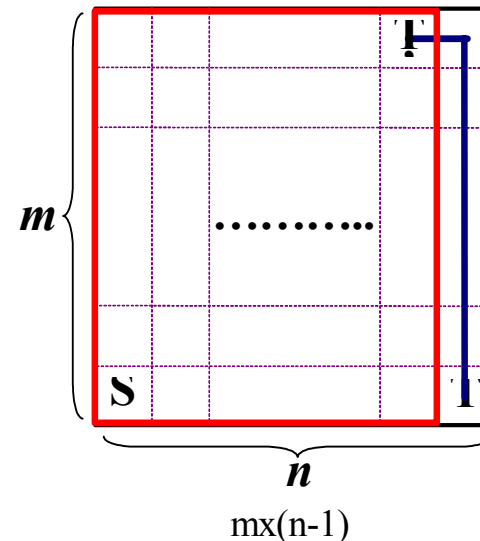


Detouring Length	#Unreachable grids	Conditions
mn	0	(1) m or n is odd
$mn-1$	1	(1) m and n are even

Cond. II: Corners in the Same Side

If ($n \geq 2$)

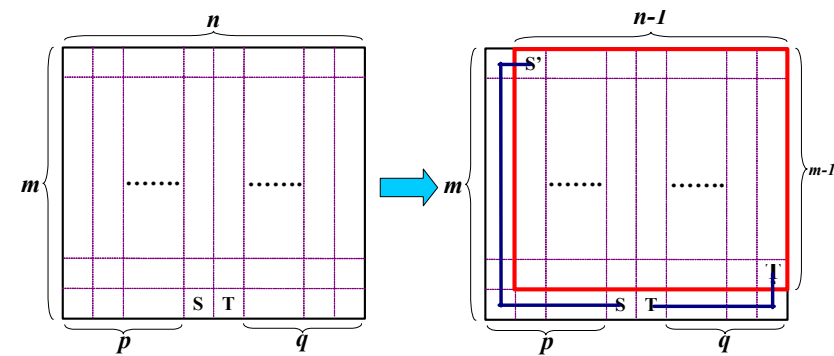
- $m \times n$ routing grids for corners in the same side
 - One L-type routing path, and
 - $m \times (n-1)$ routing grids for corners in different sides



Detouring Length	#Unreachable Grids	Conditions
mn	0	(1) (m is odd) or (n is even)
$mn-1$	1	(1) (m is even) and (n is odd)

Cond. II: Boundary in the Same Side

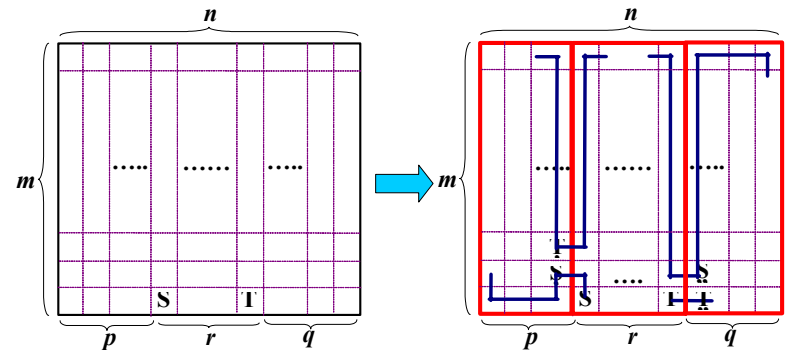
- S and T are located on adjacent grids
 - $p(q)$ are the number of columns on the left(right) sides of S(T)
 - $m \times n$ routing grids for boundary in the same side
 - Two L-type routing paths, and
 - $(m-1) \times (n-1)$ routing grids for corners in different sides



Detouring Length	#Unreachable Grids	Conditions
mn	0	(1) m or n is even
$mn-1$	1	(1) m and n are odd

Cond. II: Boundary in the Same Side

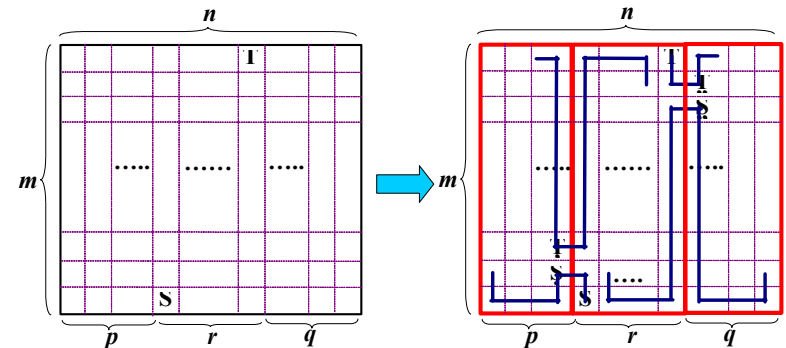
- S and T are not located on adjacent grids
 - $p(q)$ are the number of columns on the left(right) sides of S(T); r is the number of columns between S and T
 - $m \times n$ routing grids for boundary in the same side
 - $m \times r$ routing grids for corners in the same side
 - $m \times p$ and $m \times q$ routing grids for boundary in the same side



Detouring Length	#Unreachable Grids	Conditions
mn	0	(1) m and r are even (2) (m is odd) and (p and q are even)
$mn-1$	1	(1) (m is even) and (r is odd) (2) (m is odd) and ($p + q$ is odd)
$mn-2$	2	(1) m , p and q are odd

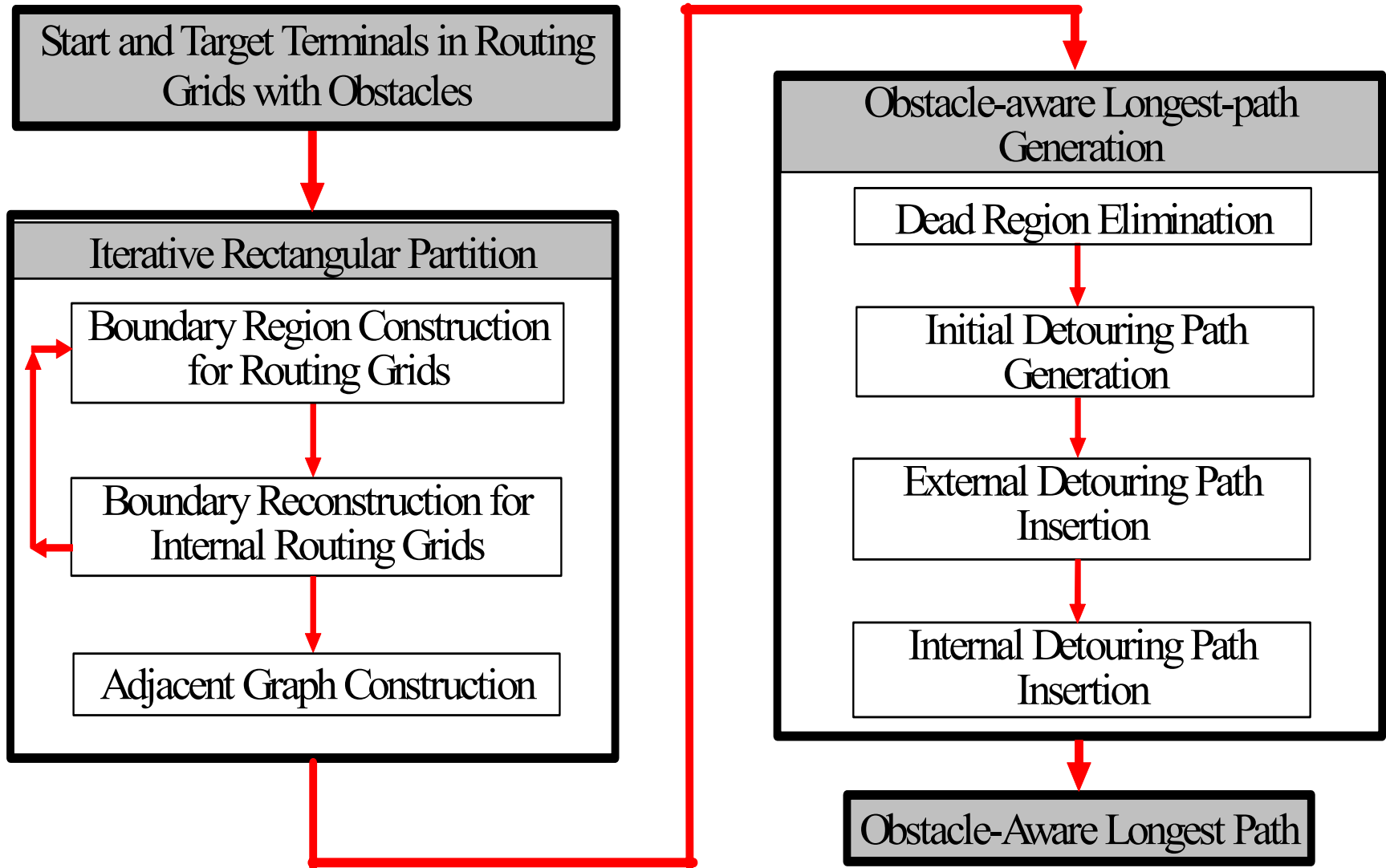
Cond. IV: Boundaries in Different Sides

- S and T are located on opposite sides
 - p(q) are the number of columns on the left(right) sides of S(T); r is the number of columns between S and T
- mxn routing grids for boundaries in different sides
 - mxr routing grids for corners in different sides, and
 - mxp and mxq routing grids for boundary in the same side



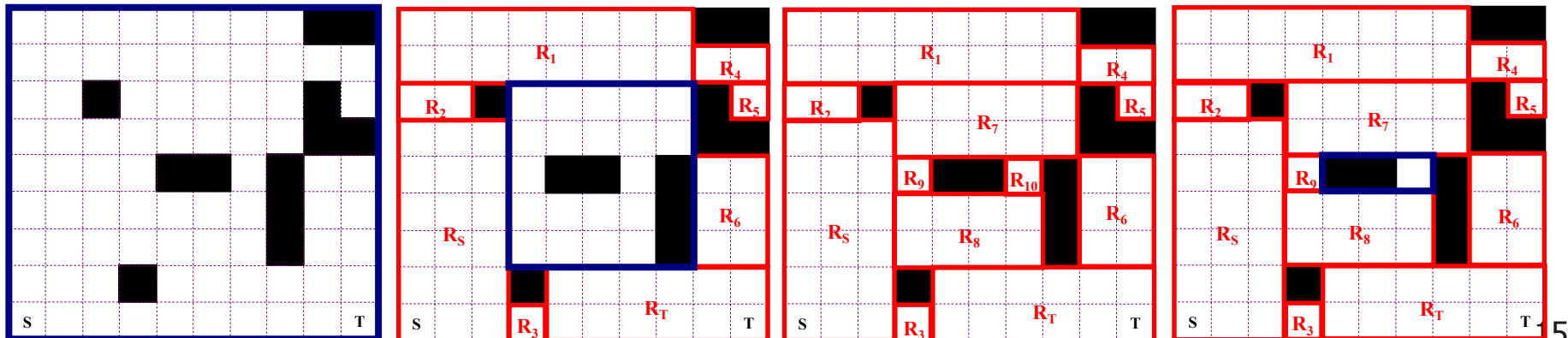
Detouring Length	#Unreachable Grids	Conditions
mn	0	(1) (m is even) and (r is odd) (2) (m is odd) and (p and q are even)
mn-1	1	(1) m and r are even (2) (m is odd) and (p+q is odd)
mn-2	2	(1) m, p and q are odd

Design Flow for Obstacle-aware Longest Path Generation



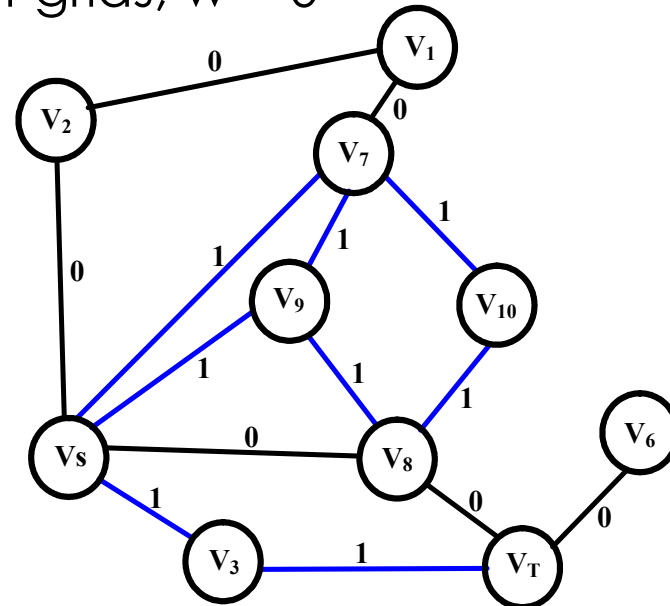
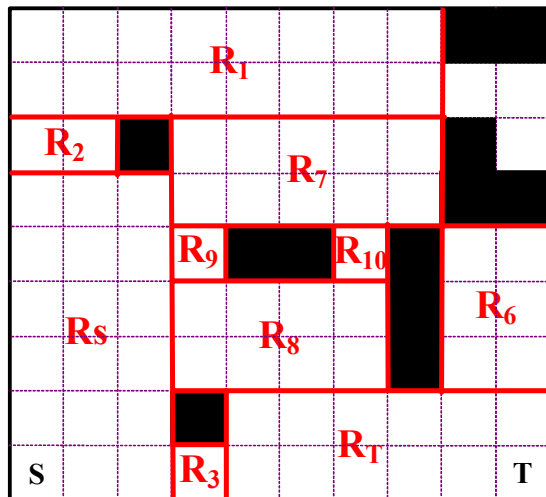
Iterative Rectangular Partition

- Construction of Outer Boundary : Minimum covering rectangular boundaries
- Definition of Corner Grids : the perpendicular sides of any routing grid are
 - Outer boundary / Obstacles / Partitioned regions
- Construction of Rectangular Regions: Maximum rectangular region for corner grids
- Iterative Rectangular Partition
 - Construction of Outer Boundary-> Definition of Corner Grids -> Construction of Rectangular Regions
 - Until all of empty grids are included



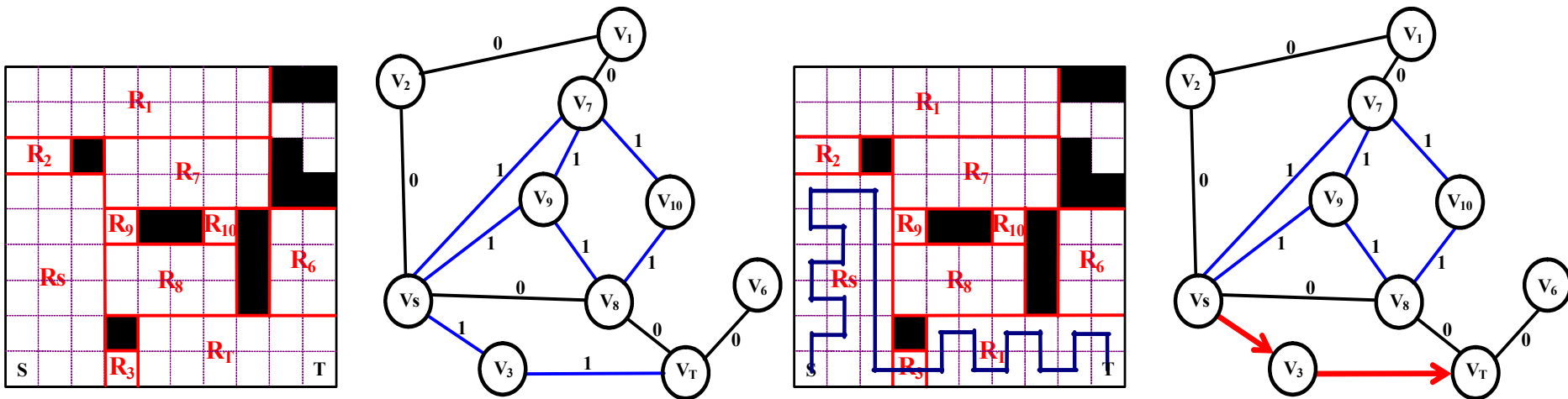
Construction of an Adjacent Graph

- Given a set of partitioned regions, with R_s , R_T and a set of empty regions
- Adjacent graph, $G(V, E)$
 - An undirected edge-weighted graph
 - $v_i, v_j \subseteq V$, represents the partitioned region, R_i
 - $e_{ij}, e_{ji} \subseteq E$, represents the adjacent relation between two partitioned regions, R_i and R_j
 - Edge weight (w)
 - Only an adjacent grid, $w = 1$
 - More than two adjacent grids, $w = 0$



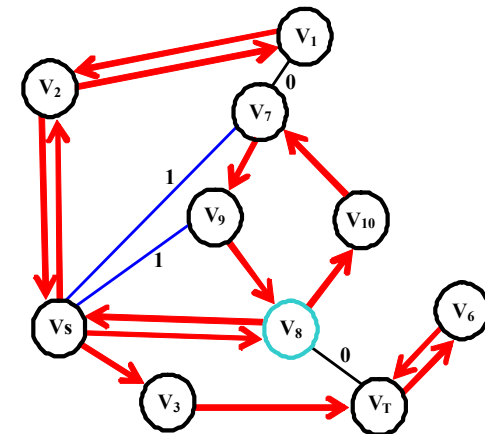
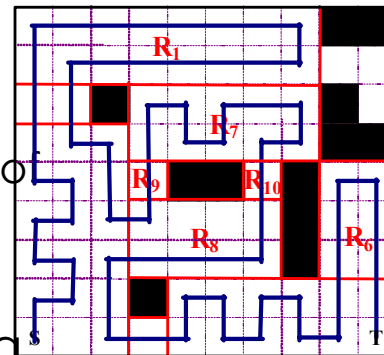
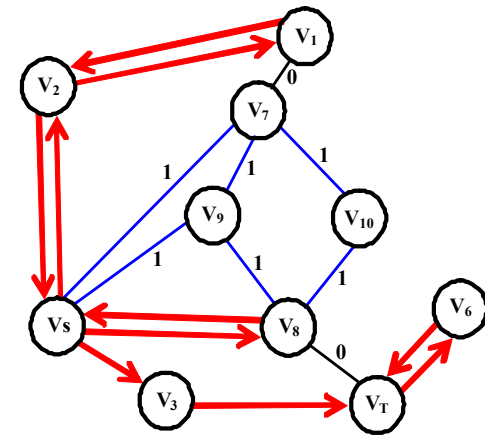
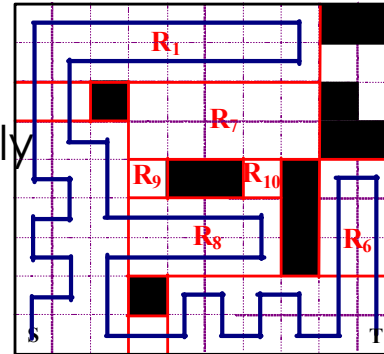
Initial Detouring Path Generation

- Dead region elimination
 - Dead region: v_i is not v_s and v_T , the degree is 1 and the edge weight is 1
 - Elimination of dead regions due to no help for path generation
- Initial detouring path generation
 - Based on breadth-first search and rectangular pattern detouring, the initial detouring path between v_s and v_T is determined
- Reference vertices
 - The vertices in the adjacent graph are covered by the current detouring path



External / Internal Detouring Path Insertion

- Adjacent relation with reference vertices
 - Adjacent relation can be obtained by using a BFS algorithm
 - $W = "0"$: for a R-flip operation
 - $W = "1"$: for a C-flip operation possibly
- Selection policy
 1. A vertex is included for a R-flip operation, excluded by a C-flip operation
 - Directly involve the vertex for a R-flip operation
 2. A vertex is both included for a R-flip and C-flip operations
 - Choose the results with min. number of unreachable grids
- Internal detouring path
 - The region is generated by running a C-flip operation and routed by running a R-flip operation



Analysis of Time Complexity

Given a set of $m \times n$ routing grids

- Iterative rectangular partition: $O(mn \log(mn))$
 - Sorting the locations of all the obstacles: $O(mn \log(mn))$
 - Selection of all the partitioned regions: $O(mn)$
- Obstacle-aware longest path generation: $O(mn)$
 - Dead region elimination: $O(mn)$
 - Initial detouring path by BFS algorithm: $O(mn)$
 - External / Internal detouring insertions: $O(mn)$

Obstacle-aware longest path generation: $O(mn \log(mn))$

Experimental Results

■ Implementation Environment

- PC: Pentium QuadCore 2.66GHz w/ 2G memory
- Standard C++ language
- Ten tested cases, Data01-Data10, from Y. Kohira, et al.[5]

<i>Circuits</i>	<i>Area</i>	<i>#Grid</i>	<i>#Dead Grids</i>	<i>US Routing</i>		<i>Our Routing</i>	
				<i>Wirelength (#Grid)</i>	<i>Time(s)</i>	<i>Wirelength (#Grid)</i>	<i>Time(s)</i>
<i>Data01</i>	<i>10x9</i>	<i>83</i>	<i>0</i>	<i>80(96.4%)</i>	<i>0.004</i>	<i>82(98.8%)</i>	<i><0.001</i>
<i>Data02</i>	<i>11x13</i>	<i>121</i>	<i>0</i>	<i>119(98.3%)</i>	<i>0.005</i>	<i>119(98.3%)</i>	<i><0.001</i>
<i>Data03</i>	<i>11x13</i>	<i>110</i>	<i>0</i>	<i>107 (97.3%)</i>	<i>0.005</i>	<i>107 (97.3%)</i>	<i><0.001</i>
<i>Data04</i>	<i>11x13</i>	<i>106</i>	<i>0</i>	<i>103(97.2%)</i>	<i>0.005</i>	<i>103(97.2%)</i>	<i><0.001</i>
<i>Data05</i>	<i>11x13</i>	<i>98</i>	<i>0</i>	<i>95(96.9%)</i>	<i>0.005</i>	<i>95(96.9%)</i>	<i><0.001</i>
<i>Data06</i>	<i>11x13</i>	<i>116</i>	<i>0</i>	<i>85(73.3%)</i>	<i>0.005</i>	<i>85(73.3%)</i>	<i><0.001</i>
<i>Data07</i>	<i>11x13</i>	<i>117</i>	<i>0</i>	<i>113(96.6%)</i>	<i>0.005</i>	<i>113(96.6%)</i>	<i><0.001</i>
<i>Data08</i>	<i>11x13</i>	<i>118</i>	<i>0</i>	<i>115(97.5%)</i>	<i>0.005</i>	<i>115(97.5%)</i>	<i><0.001</i>
<i>Data09</i>	<i>20x20</i>	<i>297</i>	<i>21</i>	<i>251(90.9%)</i>	<i>0.010</i>	<i>261(94.6%)</i>	<i>0.002</i>
<i>Data10</i>	<i>70x100</i>	<i>6654</i>	<i>4</i>	<i>6626(99.6%)</i>	<i>4.760</i>	<i>6636(99.8%)</i>	<i>1.181</i>

Conclusions

- PCB Routing,
 - The length controllability of a net decides the routing delay of the net and skew
 - The consideration of obstacles is necessary
- Longest Path Generation
 - Analysis of unreachable grids for rectangular pattern detouring for the reduction of the routing time
 - Based on the rectangular partition in routing grids, an efficient approach is proposed to generate the grid-based longest path for PCB routing
- Experimental Results
 - Compared with US routing, our proposed approach can achieve longer paths for tested examples in less CPU time

Thanks Your Kind Attention!