

# Accurate Remaining Range Estimation for Electric Vehicles

Joonki Hong, Sangjun Park, Naehyuck Chang  
Dept. of Electrical Engineering  
KAIST

[joonki@cad4x.kaist.ac.kr](mailto:joonki@cad4x.kaist.ac.kr)

# Outline

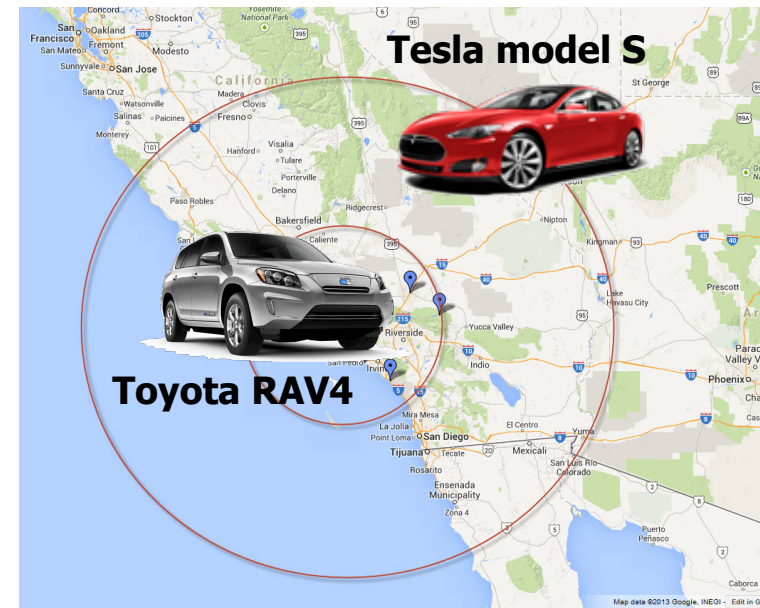
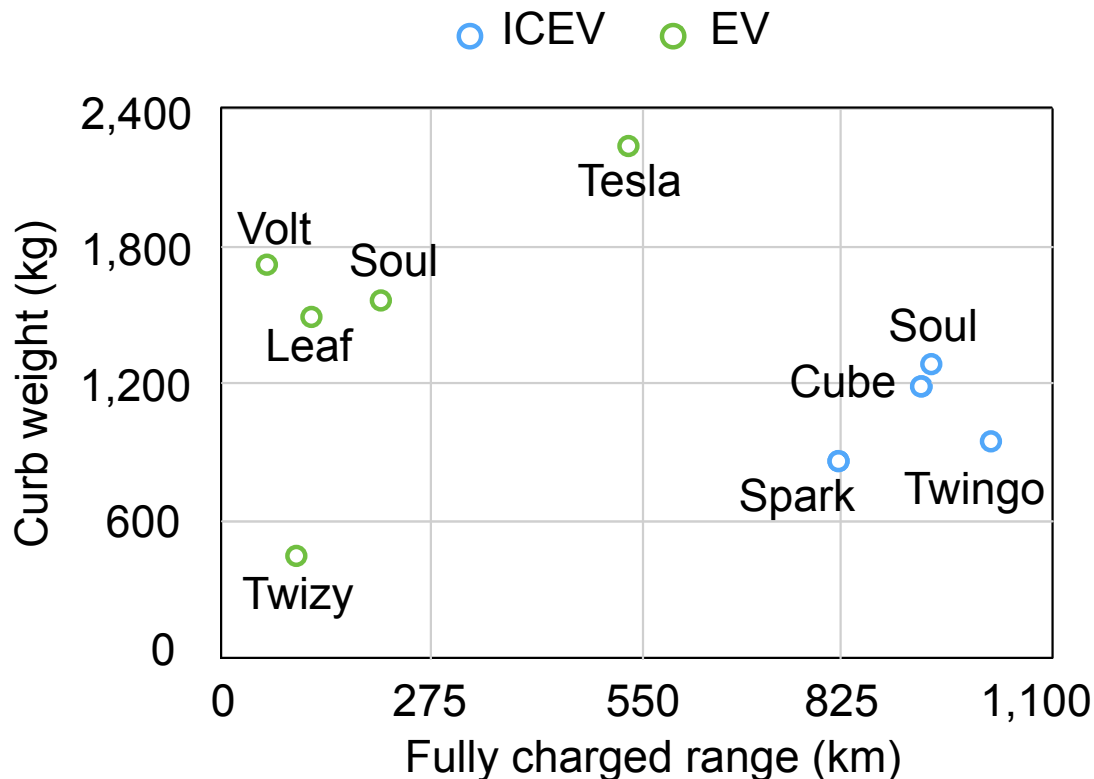
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100

- **Motivation: Remaining range estimation**
- Related works
- Our framework
- Experiment
- Conclusion



# Fully Charged Ranges of EV

- Electric vehicles are emerging with their great advantages, but EV drivers suffer from the short driving range
- EV have 5X shorter fully charged ranges than that of ICEV (Internal Combustion Engine Vehicles)



# Range Anxiety

- Range anxiety is the fear that a vehicle may not have sufficient energy to reach its destination
- The range anxiety comes from the uncertainty of the remaining range
- Modern fuel gauges show the remaining range but it's only based on the driving history (past fuel consumption)



# Range Anxiety in EV

- Most of the electric vehicle drivers always suffer from the range anxiety
  - Limited EV charging facilities, long charging time
  - Running out of battery while driving gives the same inconvenience as the vehicle breakdown



# Range Anxiety in EV

- The statistics says that most of the EV drivers attempt only 70% of the estimated driving range with confidence
- The range anxiety in EV make the effective driving range of the EV even shorter
- Efforts to mitigate range anxiety
  - More EV charging facility, higher density batteries, fast charging, and range extender
  - Above solutions are time consuming or high cost



**Rav4 EV**  
**112 km**   **160 km**



**Model S**  
**300 km**   **420 km**



**Twingo**  
**1000 km**

# Paper Contribution

- In this paper, we provide accurate range estimation
- It mitigates the uncertainty of the driving range alleviates the range anxiety
- It restores the reserved range and extend the effective driving range
- Same effect of extended range without increasing the battery capacity

**Case 1**



**Case 2**



# Outline

133

134

204

327

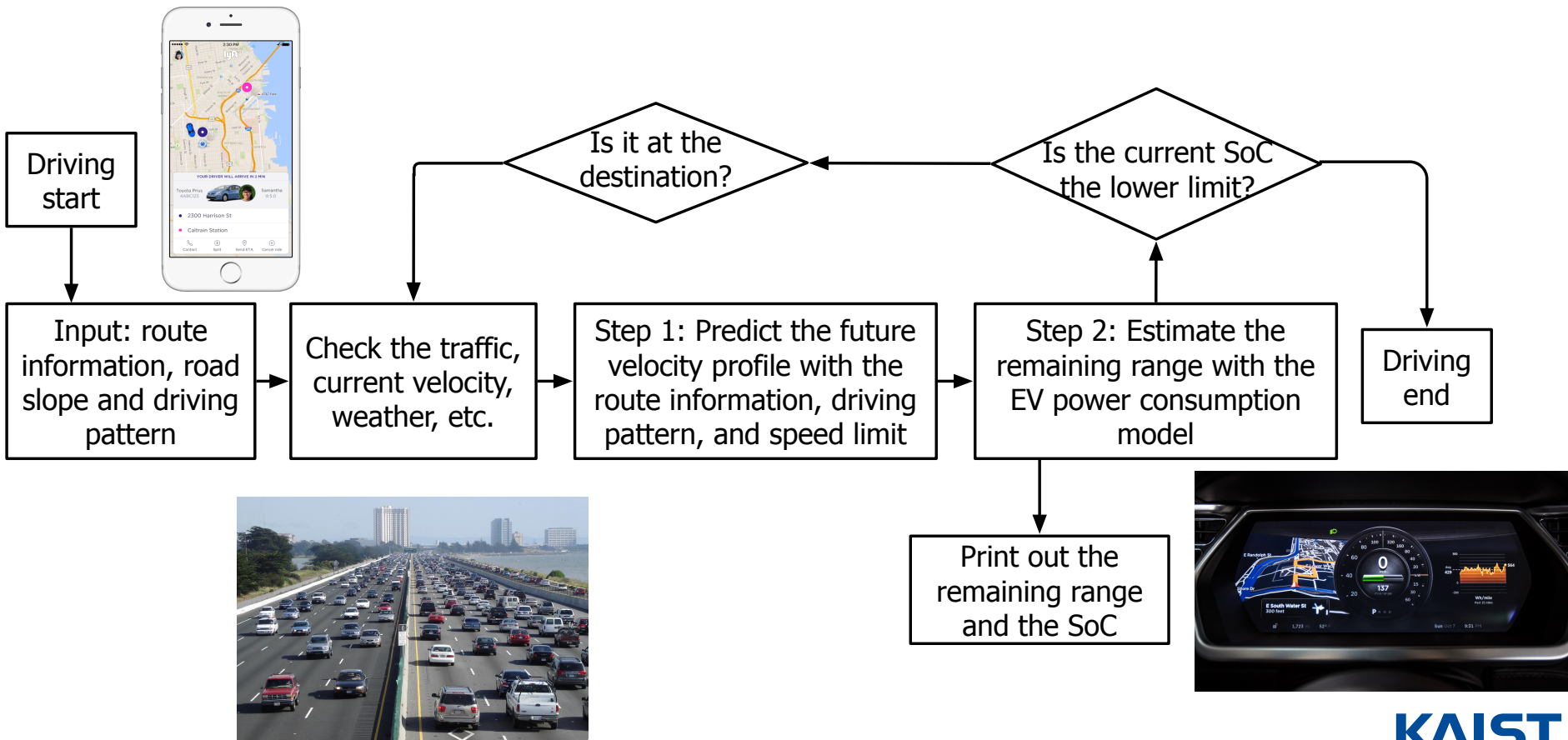
- Motivation
- **Related works**
  - **History based RR**
  - **Model based RR**
- Our framework
- Experiment
- Conclusion





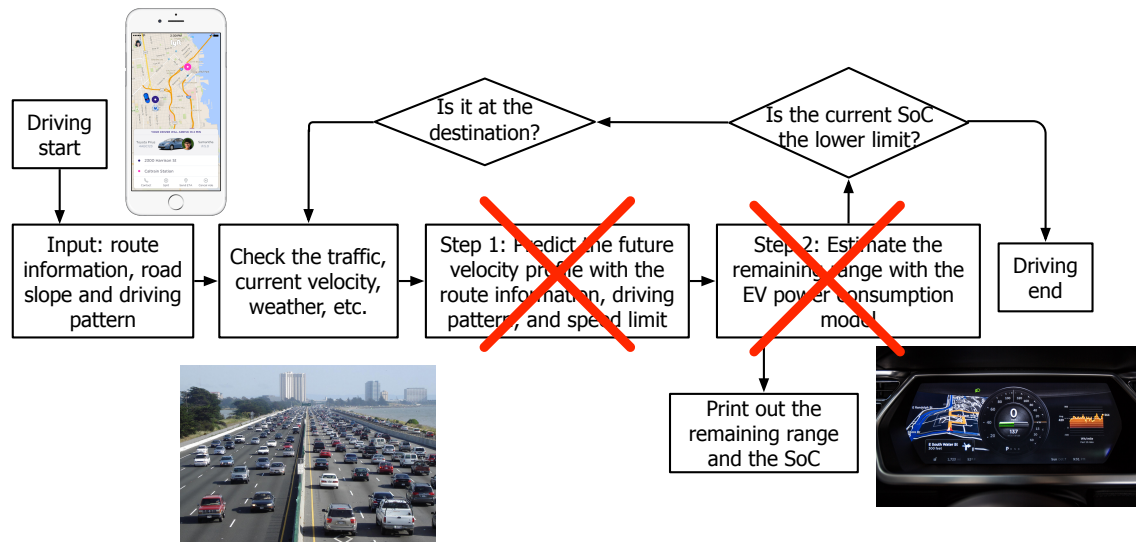
# RR Estimation Framework

- The general remaining range framework can be simplified as following figure



# History Based RR

- History based remaining range estimation assumes the future power consumption is the same as the past power consumption



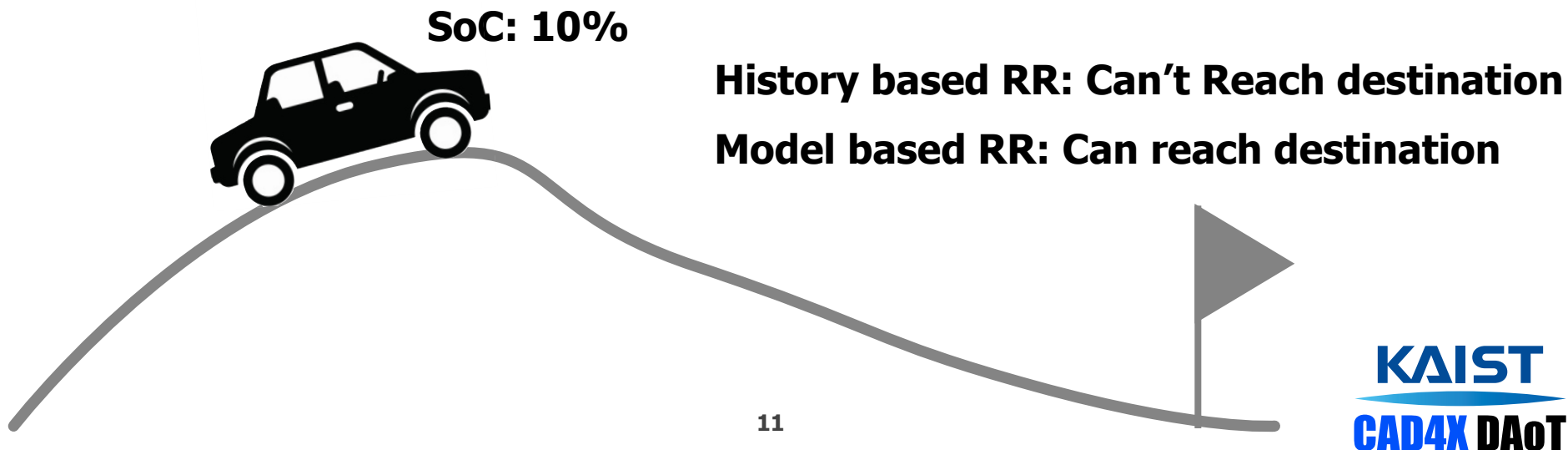
$$\hat{\bar{p}}_{future}(x) \approx \bar{p}_{past}(x)$$

- Some works used regression based algorithm to improve the estimation accuracy

$$\hat{\bar{p}}_{future}(x) = \hat{y}(x) * \bar{p}_{Long}$$

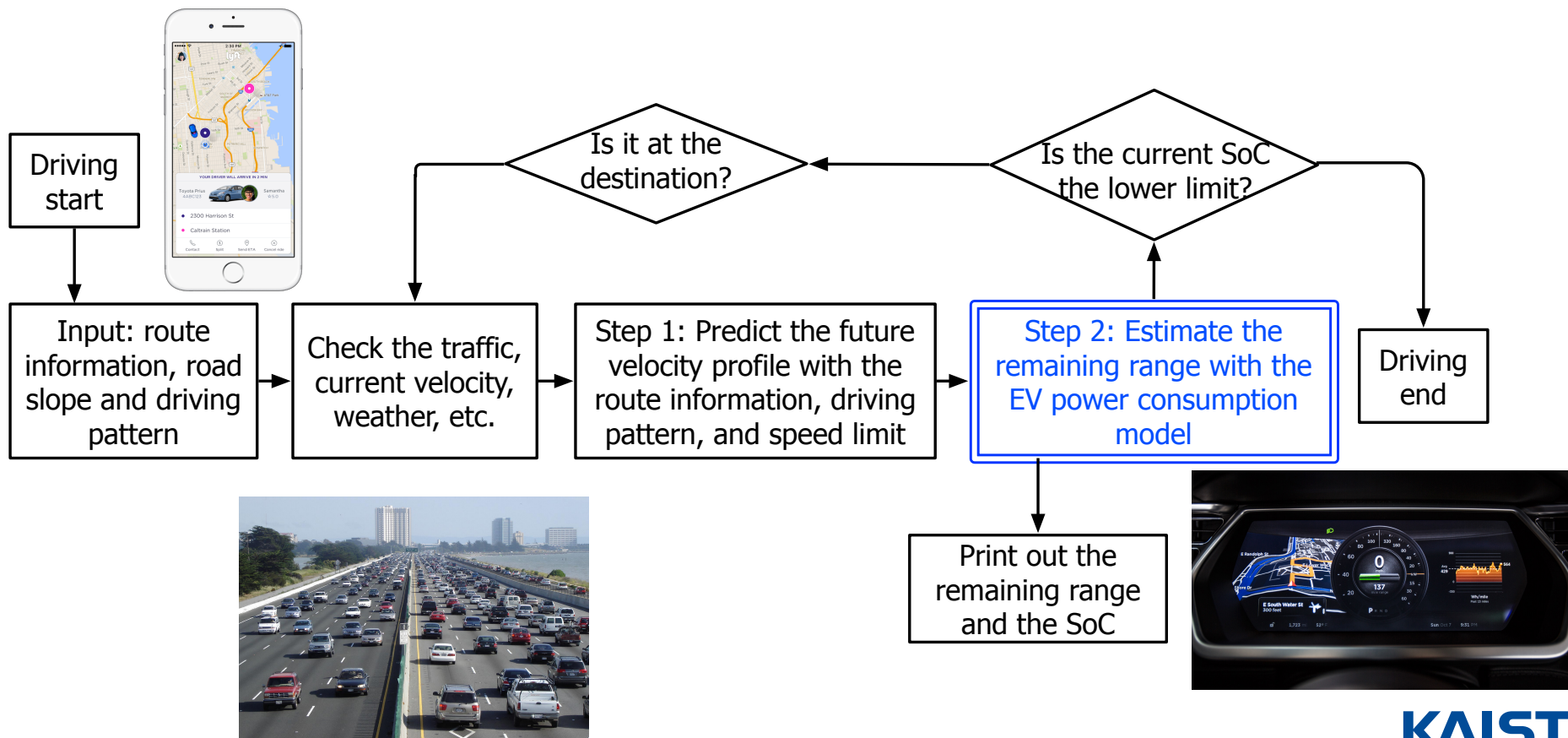
# Model Based RR

- Model based remaining range estimation is naturally more accurate than the history based estimation
- There are some works about the model based range estimation
- They focused on predicting the future driving profile, but left the power model simplified



# Paper Contribution

- In this paper, we focus on an accurate EV power model to achieve an accurate remaining range estimation



# Outline

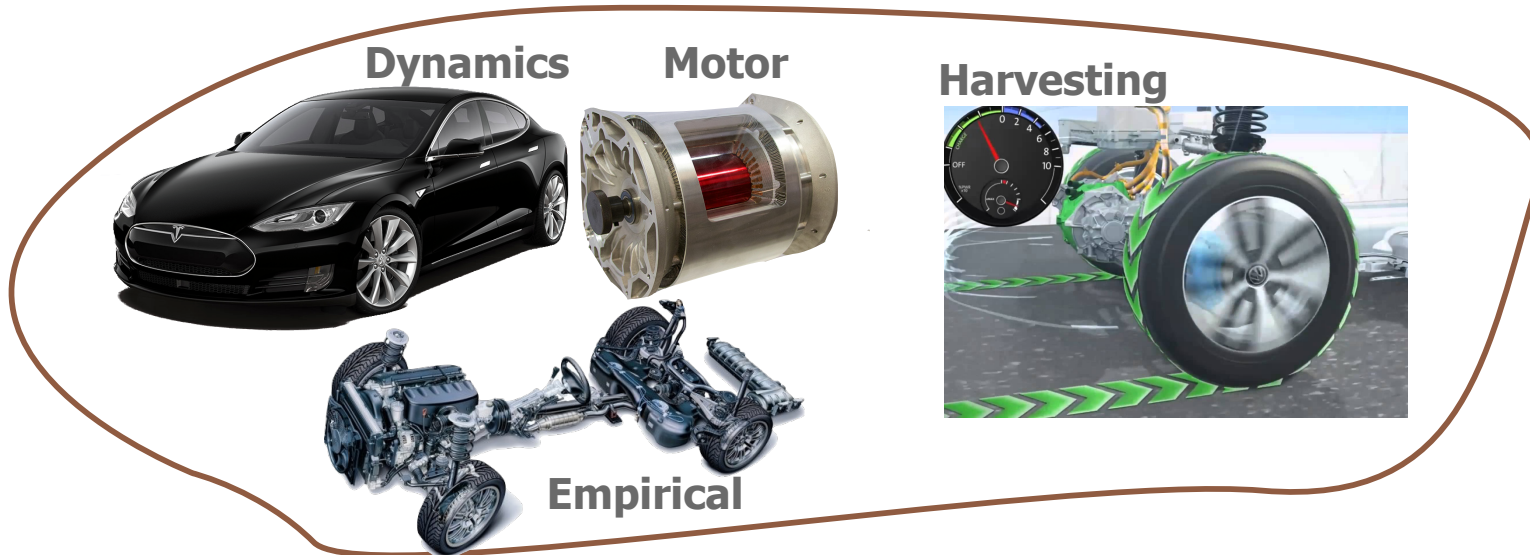
- Motivation
- Related works
- **Our framework**
  - **Remaining range estimation**
  - **EV power model**
- Experiment
- Conclusion



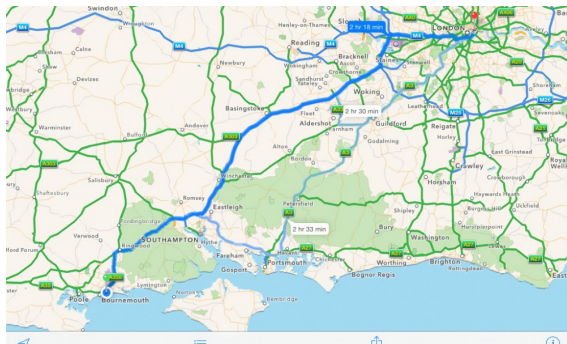
# Proposed Range Estimation

- We start with a basic assumption that the future driving profile is given

## EV Power Model



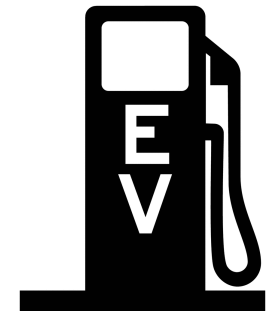
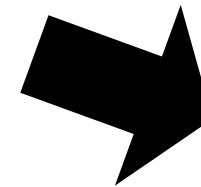
## Future driving profile



## Battery model



## Remaining Range



# Vehicle Dynamics Model

- Widely used vehicle power consumption model

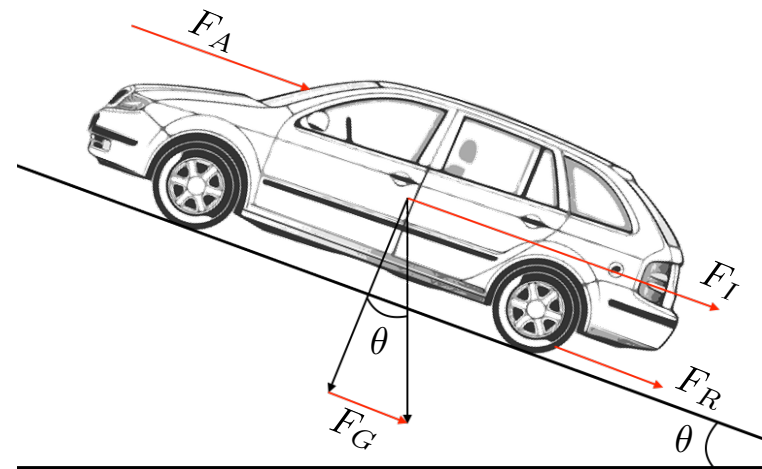
$$\begin{aligned}P_{dynamics} &= F \frac{ds}{dt} = Fv \\ &= (F_R + F_A + F_G + F_I + F_B)v \\ &\approx (F_R + F_G + F_I)v \\ &\approx (\alpha + \beta \sin\theta + \gamma a)mv,\end{aligned}$$

$$F_R(\text{rolling resistance}) \sim C_{rr}W$$

$$F_G(\text{gravitational resistance}) \sim W \sin\theta$$

$$F_I(\text{inertial resistance}) \sim ma$$

$$F_A(\text{aerodynamic resistance}) \sim \frac{1}{2}\rho C_d A v^2$$



# Proposed Advanced Dynamics Model

- Motor efficiency actually differs dynamically according to the operating status

$$\eta = \frac{P}{P + k_i\omega + k_w\omega^3 + k_cQ^2 + C}$$

$F_i$  (Iron and friction loss)  $\sim k_i\omega$

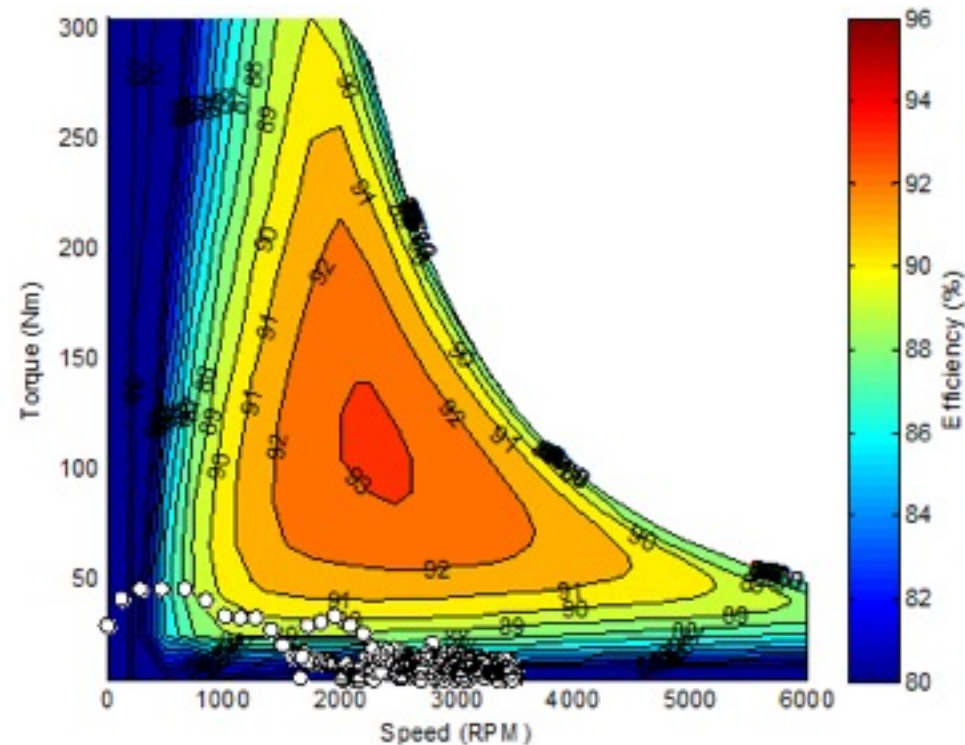
$F_w$  (Windage loss)  $\sim k_w\omega^3$

$F_c$  (Copper loss)  $\sim k_cQ^2$

Constant loss  $\sim C$

$$T = P/v = (\alpha + \beta\sin\theta + \gamma a)m$$

$$P_{advanced} = Tv + C_0 + C_1v + C_2T^2$$



MAGSOFT corporation

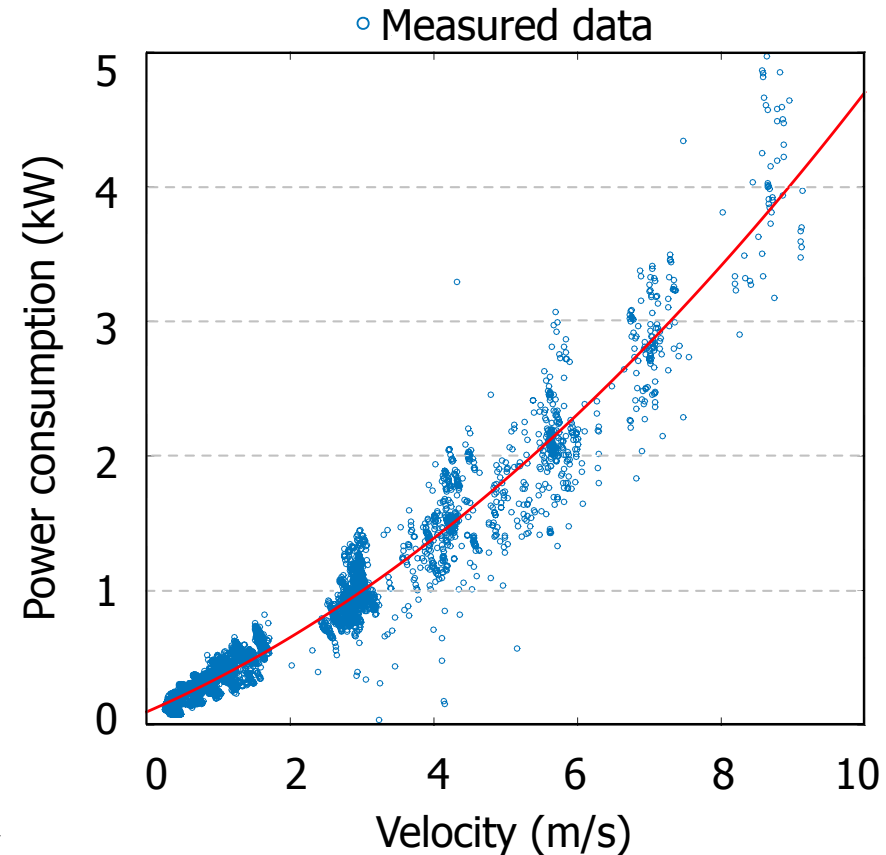


# Proposed Hybrid Power Model

- Advanced dynamics model ignores the drivetrain and ancillary losses in the estimation
- A pilot experiment to verify the adequacy of the advanced dynamics model
- Finally, we propose the **hybrid power model** including the quadratic term from empirical data

$$T = P/v = (\alpha + \beta \sin\theta + \gamma a)m$$

$$P_{\text{hybrid}} = Tv + C_0 + C_1v + C_2v^2 + C_3v^3$$



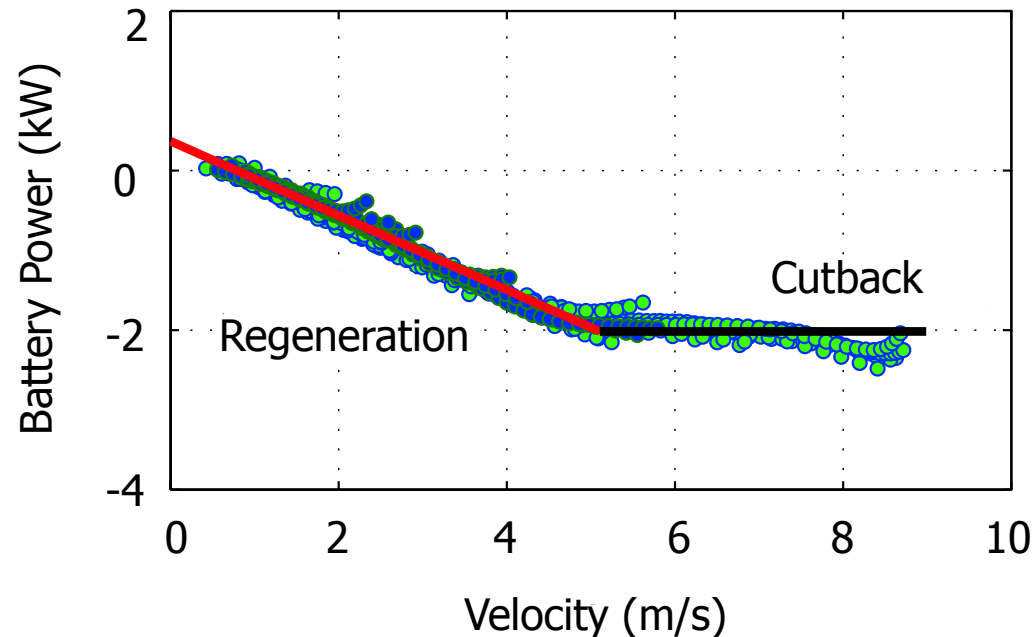
# Regenerative braking model

- One of the most commonly used energy harvesting methods in the EV is regenerative braking
- The regenerative braking comes from the electromagnetic induction

$$P_{induction} \propto \omega$$

- Regenerative power can be modeled as follows

$$\begin{aligned} P_{regen} &= \delta v - \epsilon \\ &= (460.53 \text{ J/m})v - (333.92 \text{ J/s}) \end{aligned}$$



# Power Models

- Vehicle dynamics model

$$P_{vehicle} = (\alpha + \beta \sin\theta + \gamma a)mv$$

- Advanced dynamics model

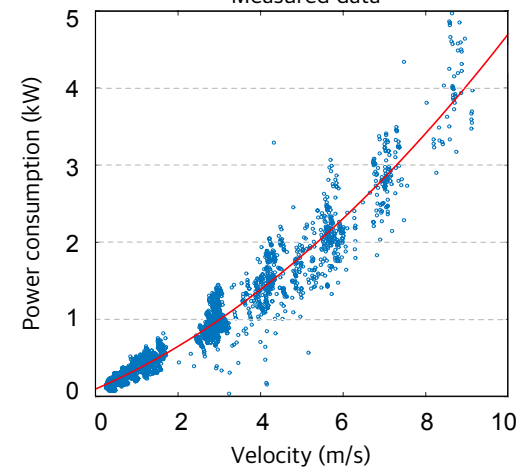
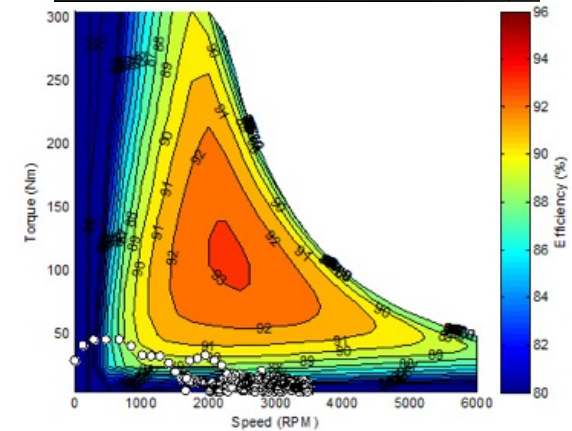
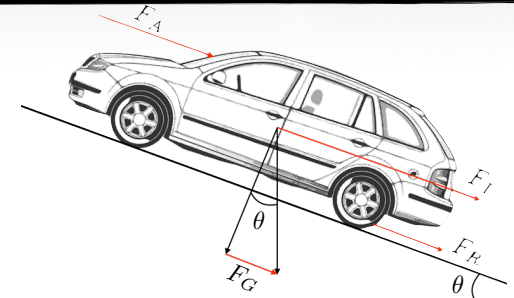
$$T = P/v = (\alpha + \beta \sin\theta + \gamma a)m$$

$$P_{advanced} = Tv + C_0 + C_1v + C_2T^2$$

- Hybrid power model

$$T = P/v = (\alpha + \beta \sin\theta + \gamma a)m$$

$$P_{hybrid} = Tv + C_0 + C_1v + C_2v^2 + C_3T^2$$



# Outline

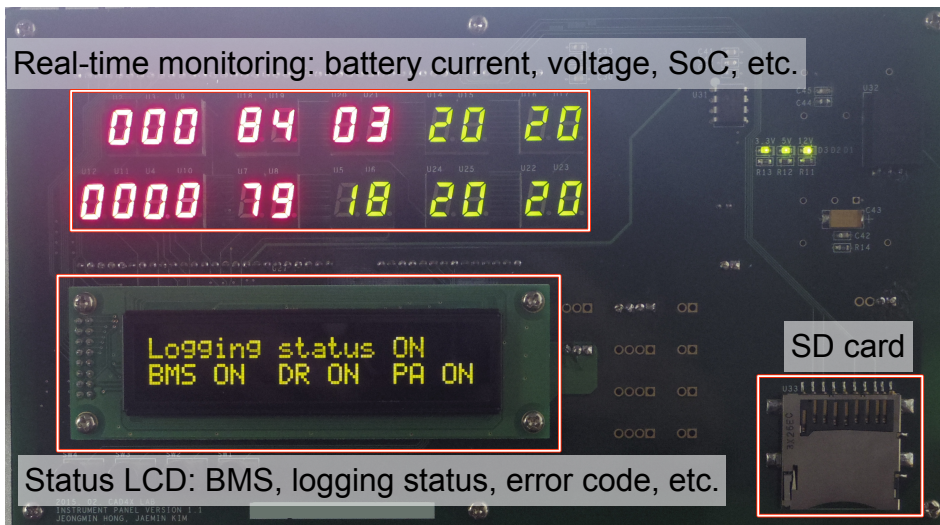
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100

- Motivation
- Related works
- Our framework
- **Experiment**
  - **Power modeling and validation**
  - **Remaining range estimation**
- Conclusion



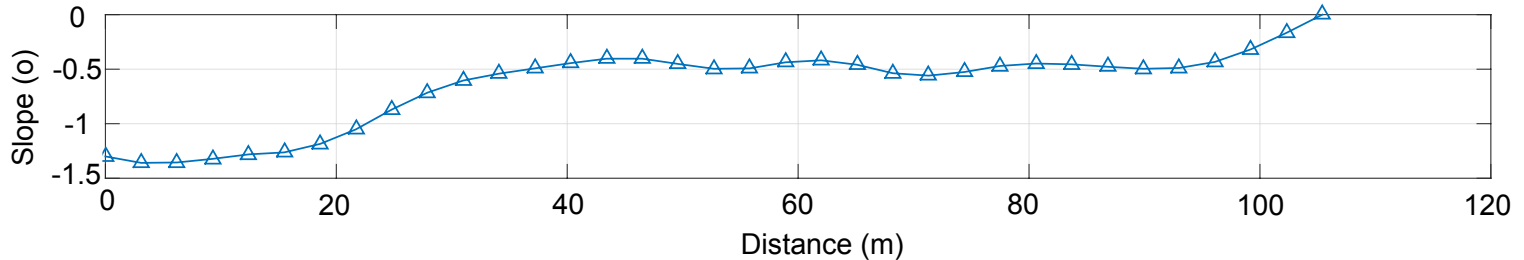
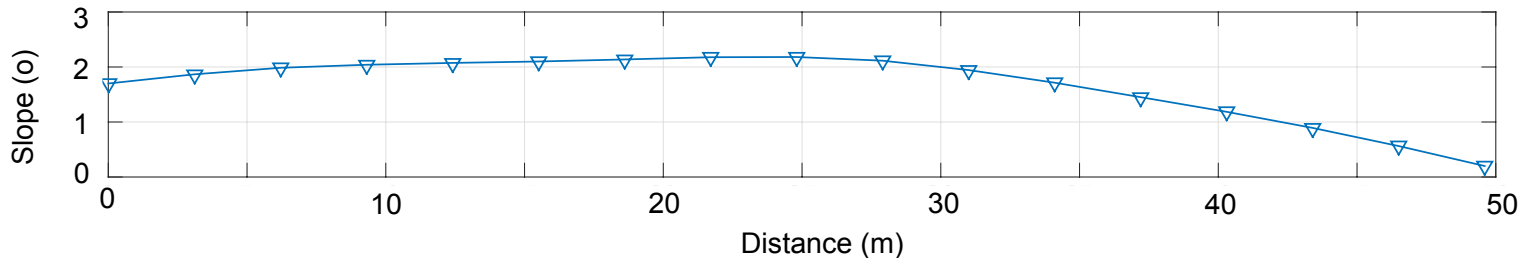
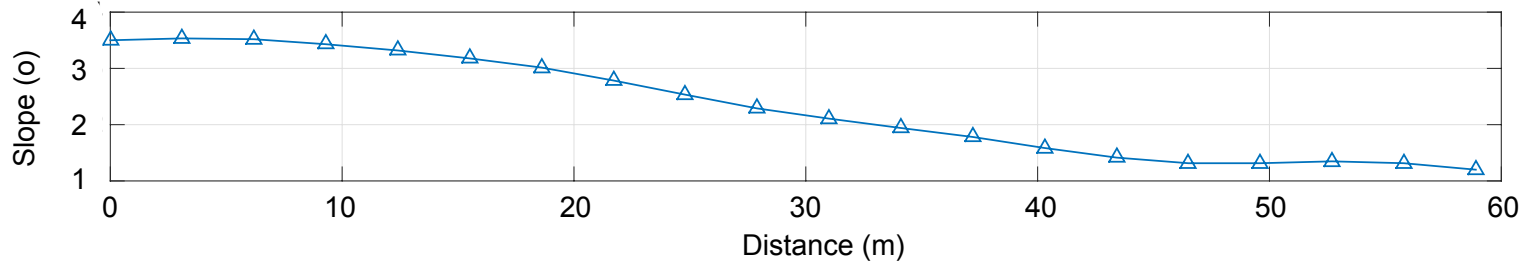
# Specification of the target vehicle

- We use a light-weight custom EV to verify the accuracy of power modeling and remaining range estimation
- Specification
  - Curb weight: 481 kg
  - Maximum velocity: 35 km/h
  - 76.8 V, 48 Ah LiFePO4 battery pack



# Data logging

- We chose a regression based approach for the modeling
- For the model fidelity, we collect 6000s of driving data from various routes



# Power consumption model

- Vehicle dynamics model

$$T = (\alpha + \beta \sin\theta + \gamma a)m,$$

$$P_{dynamics} = Tv$$

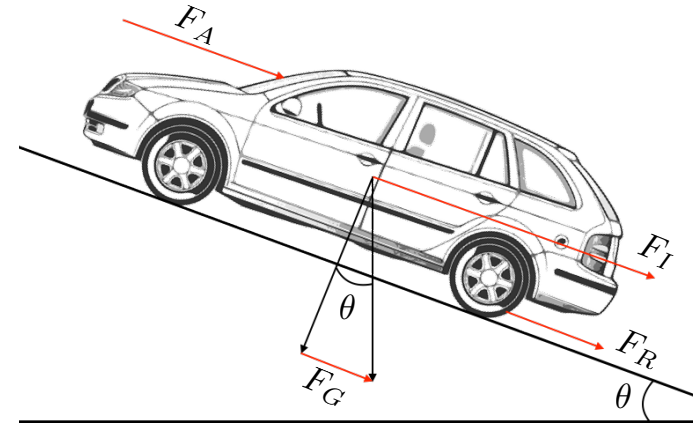
$$\alpha = 0.59, \beta = 12.63, \gamma = 1.46.$$

- Advanced vehicle dynamics model

$$P_{advanced} = Tv + C_0 + C_1v + C_2T^2,$$

$$\alpha = 0.33, \beta = 10.70, \gamma = 1.09,$$

$$C_0 = 5.28, C_1 = 118.55, C_2 = 0.0017.$$



# Power consumption model

- Vehicle dynamics model

$$T = (\alpha + \beta \sin\theta + \gamma a)m,$$

$$P_{dynamics} = Tv$$

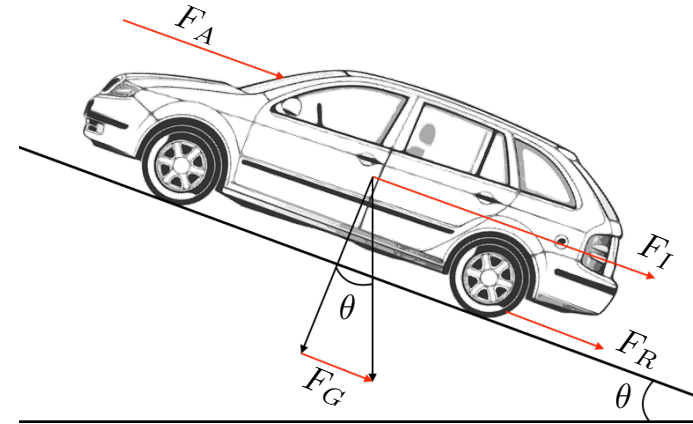
$$\alpha = 0.59, \beta = 12.63, \gamma = 1.46.$$

- Hybrid power model

$$P_{hybrid} = Tv + C_0 + C_1v + C_2v^2 + C_3Q^2,$$

$$\alpha = 0.32, \beta = 10.11, \gamma = 1.08,$$

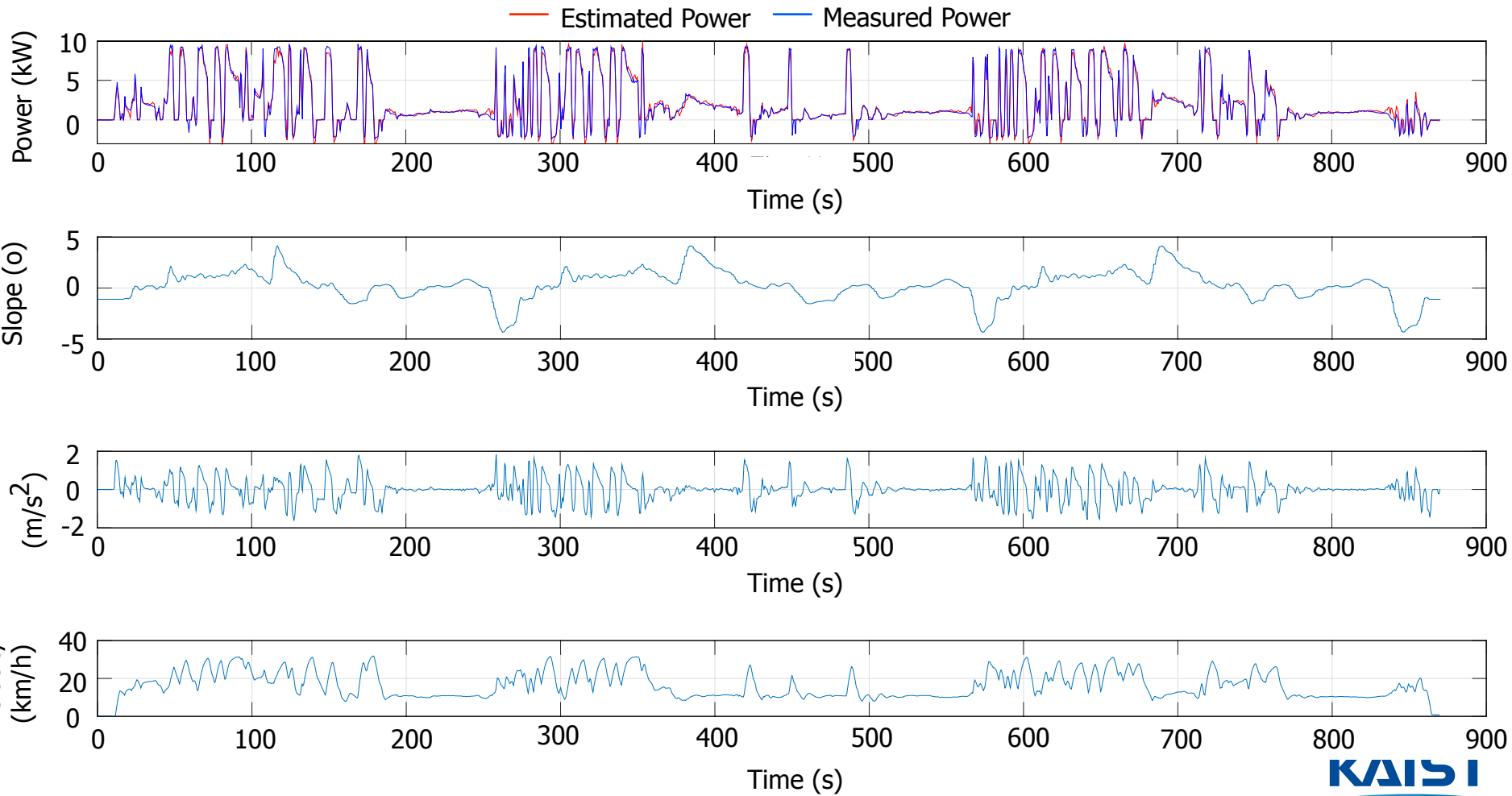
$$C_0 = 5.28, C_1 = 7.39, C_2 = 20.62, C_3 = 0.0019.$$





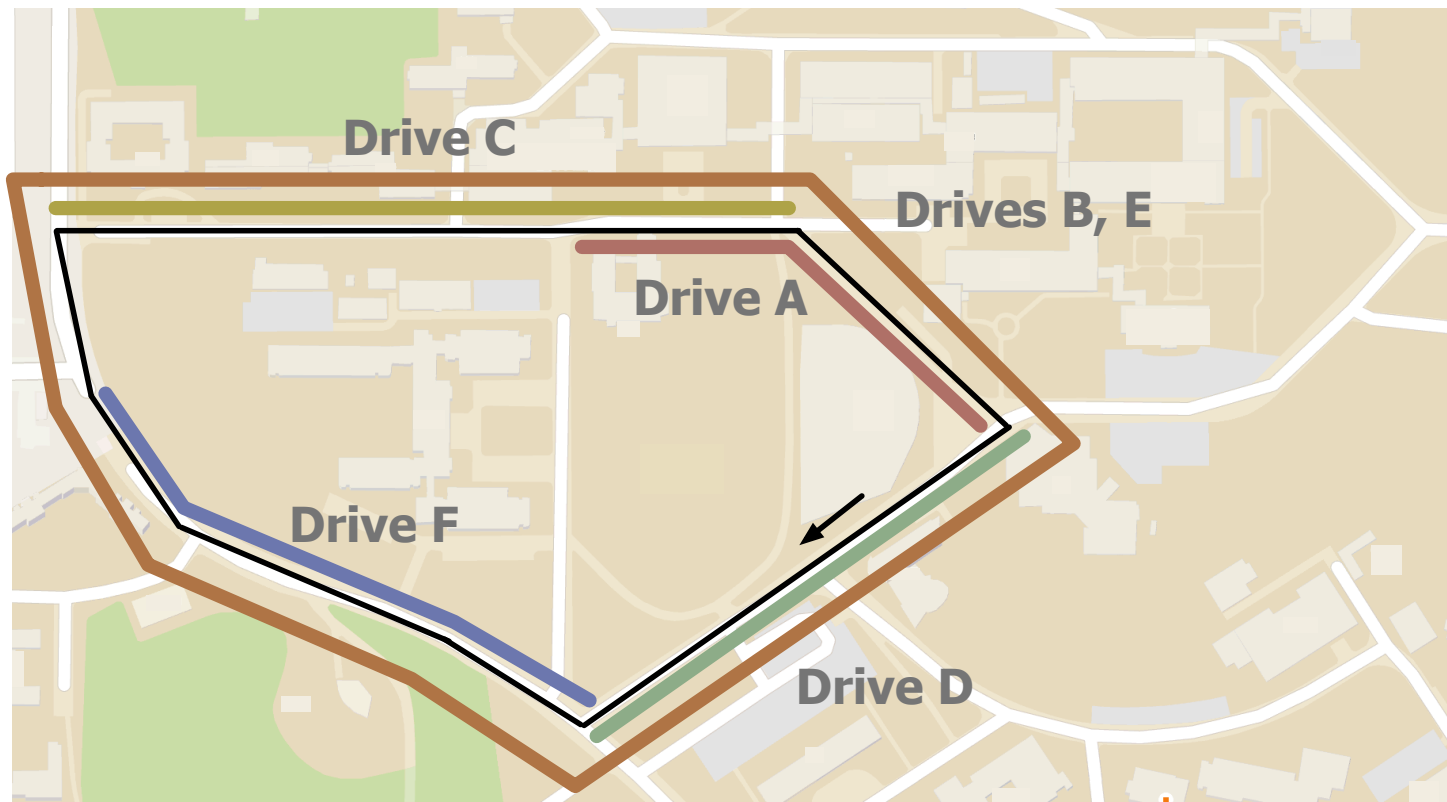
# Model validation result

- Hybrid power model yield only 3.78 % error



# Test bench drives

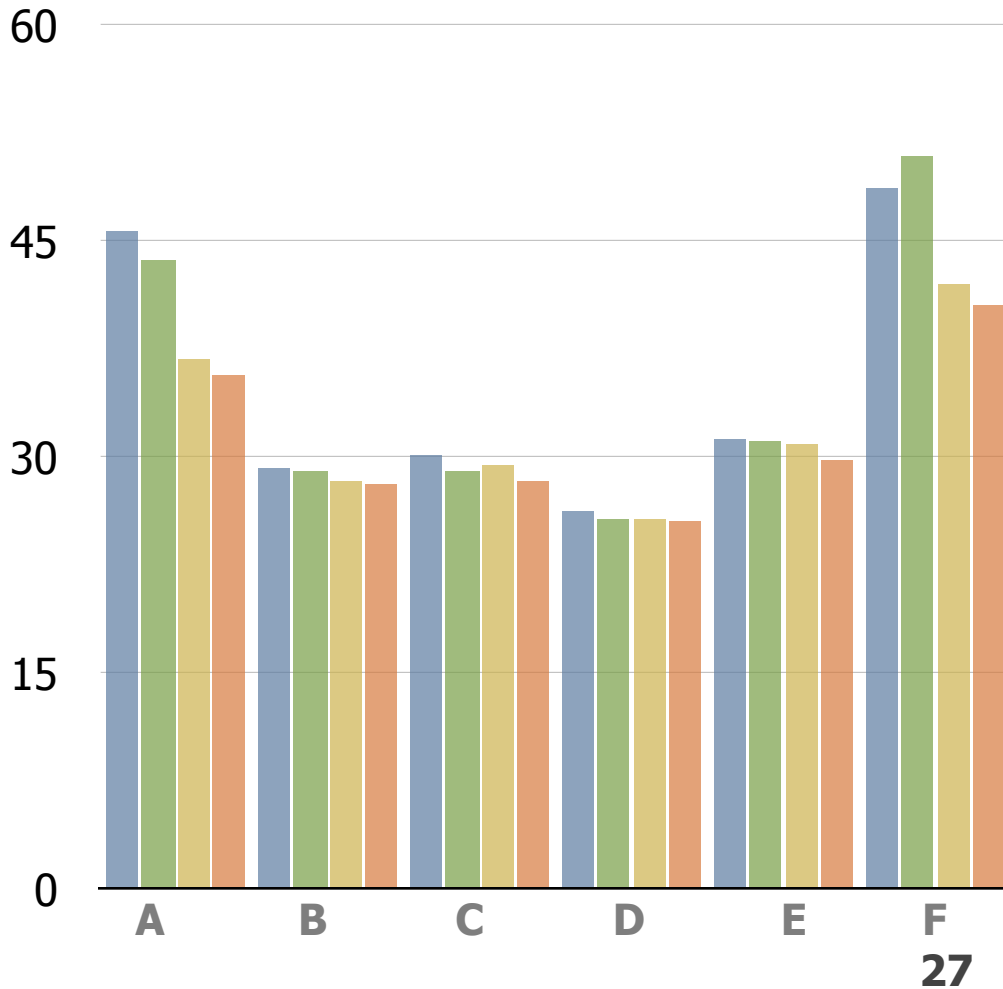
- We perform 6 test bench drives for the remaining range estimation
- Each drives were performed in different driving manner



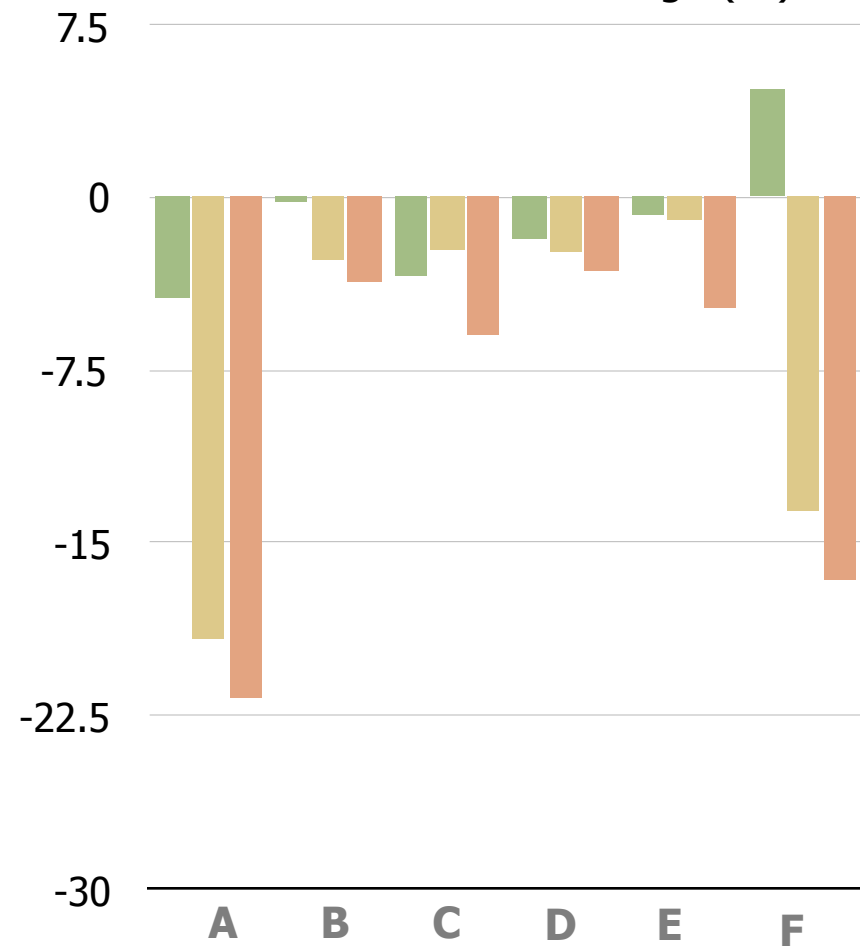
# Remaining range estimation

Measured Hybrid Advanced Dynamics

Measured and estimated range (km)



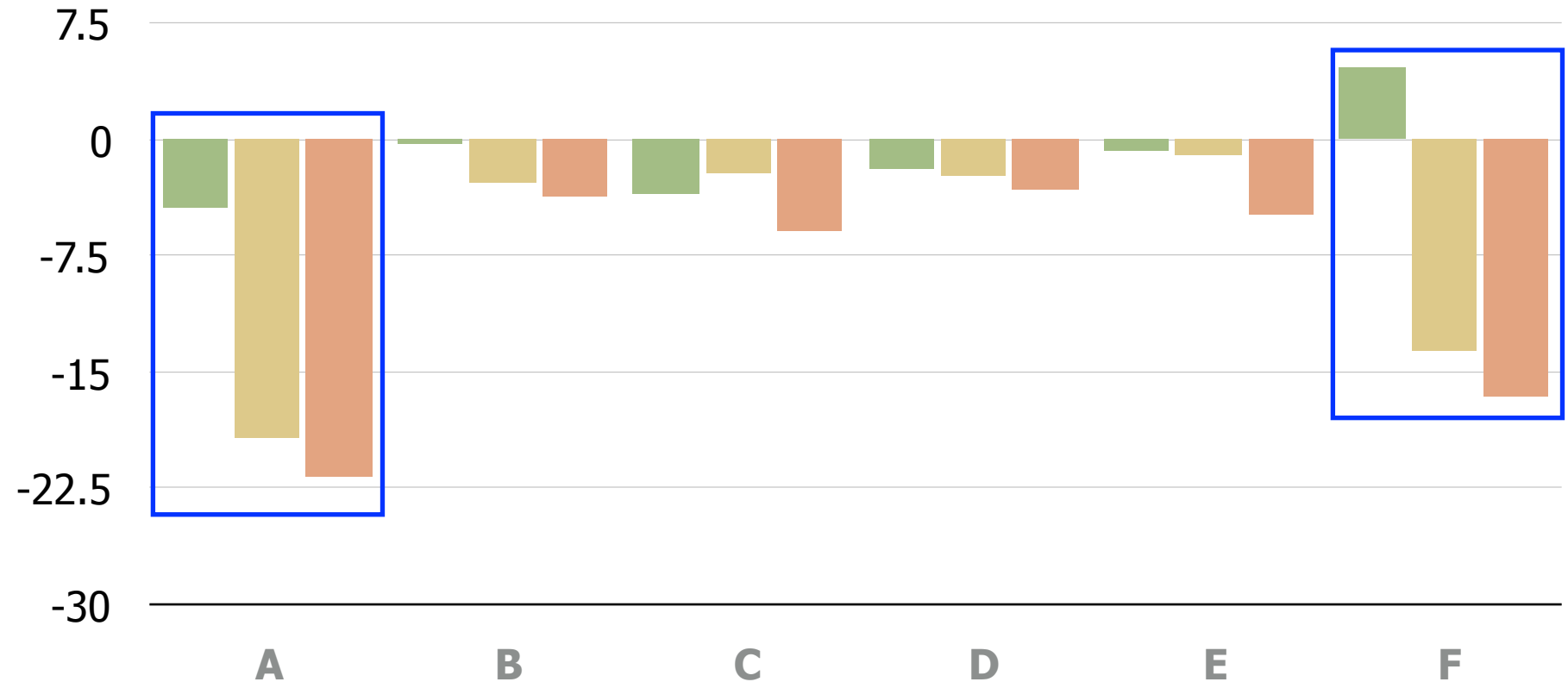
Percentage error between measured and estimated range (%)



# Remaining range estimation

- Drives A and F
  - Speed range: bellow 11.5 km/h
  - Degree range from  $-0.6^\circ$  to  $0.9^\circ$

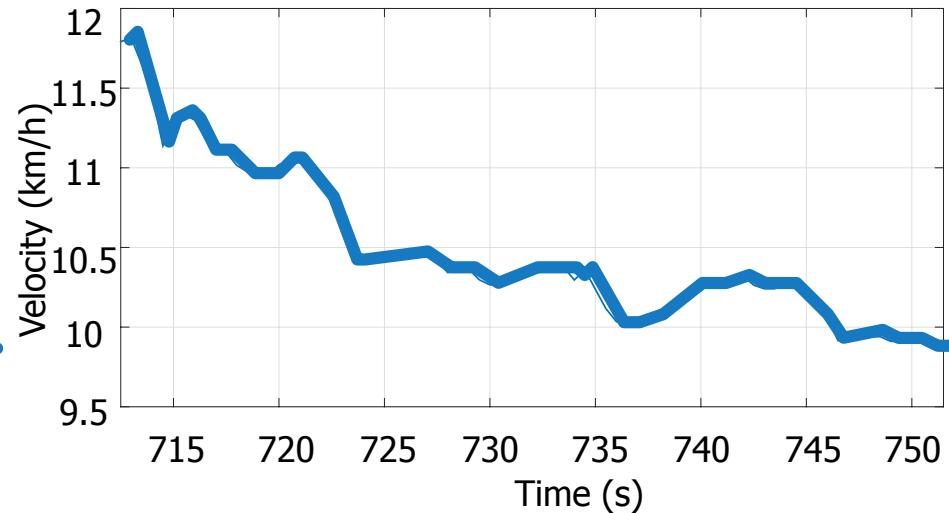
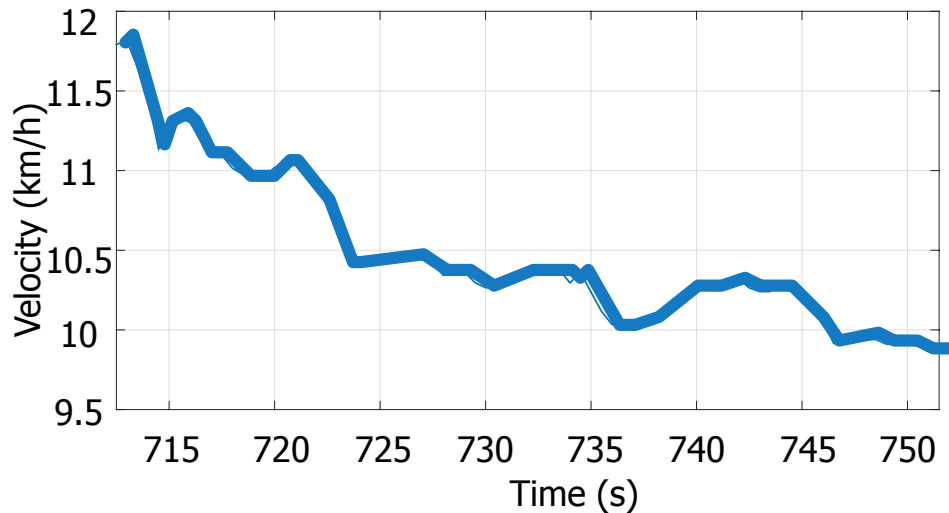
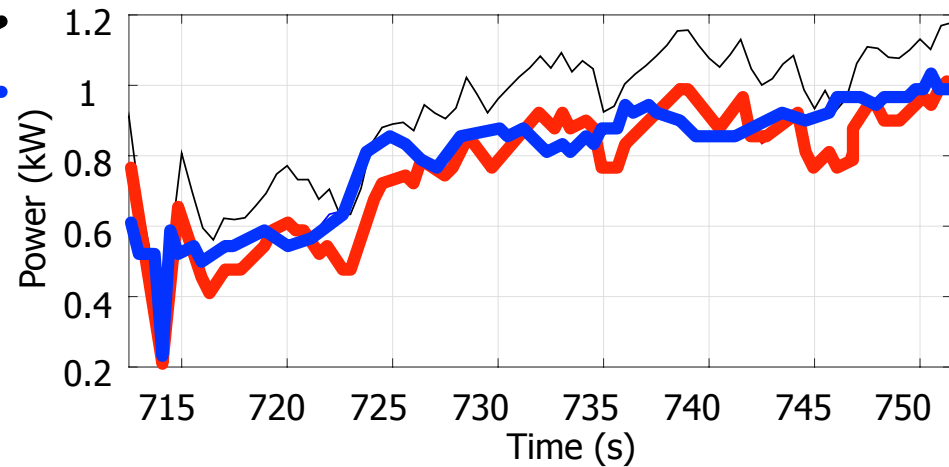
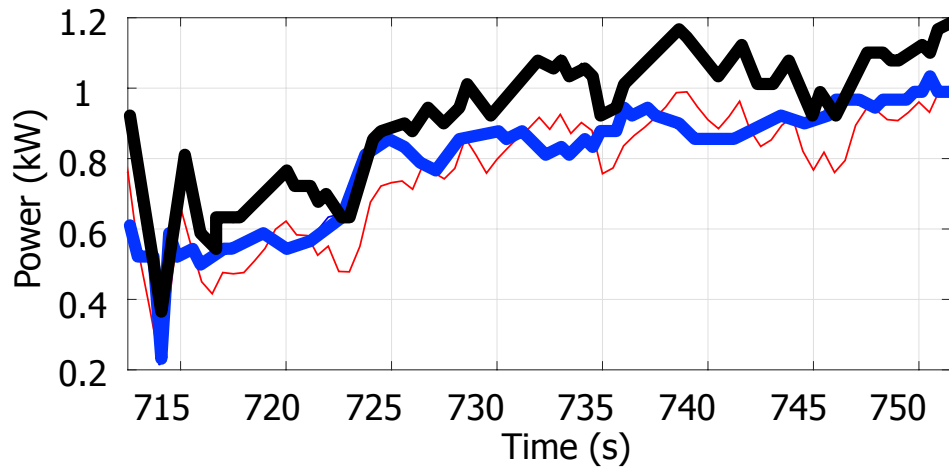
Hybrid   Advanced   Dynamics



# Remaining range estimation

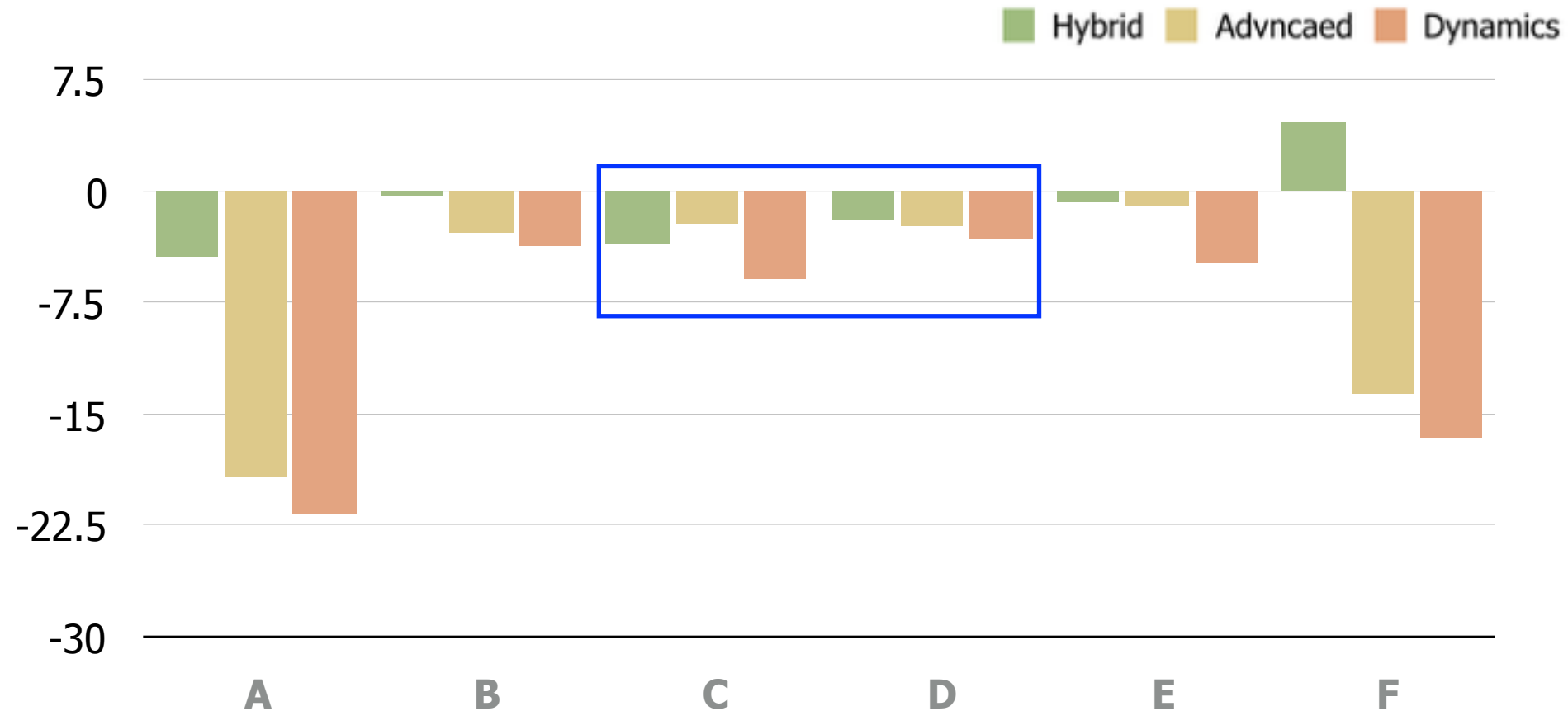
- Drives A and F

Hybrid Advanced Measured



# Remaining range estimation

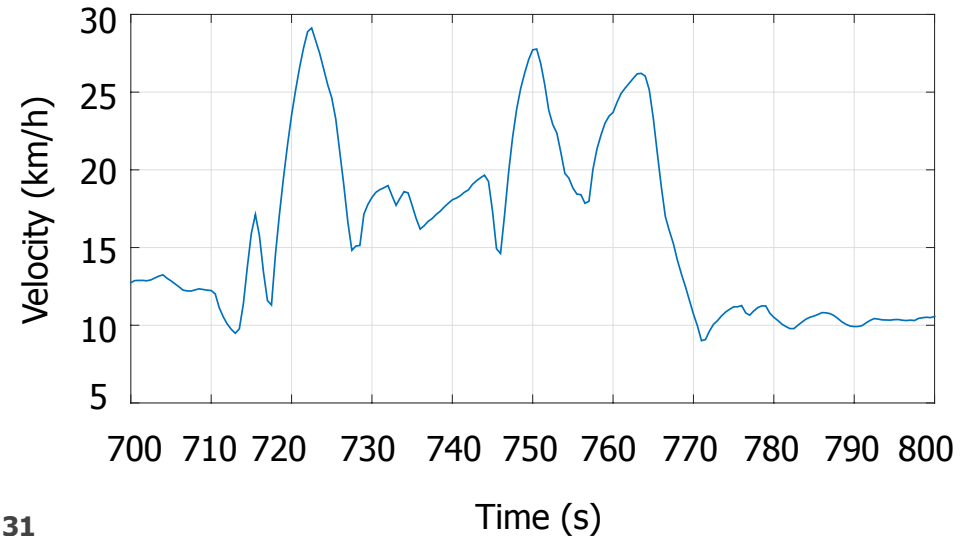
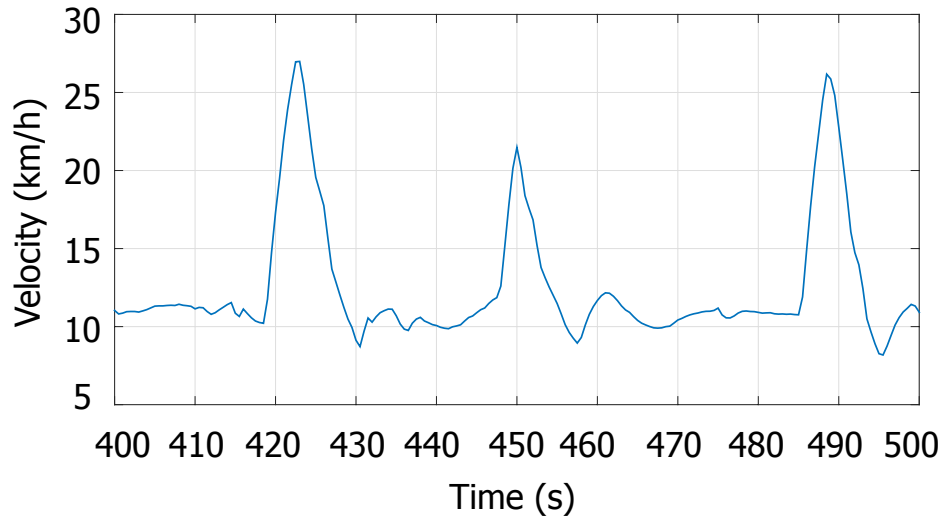
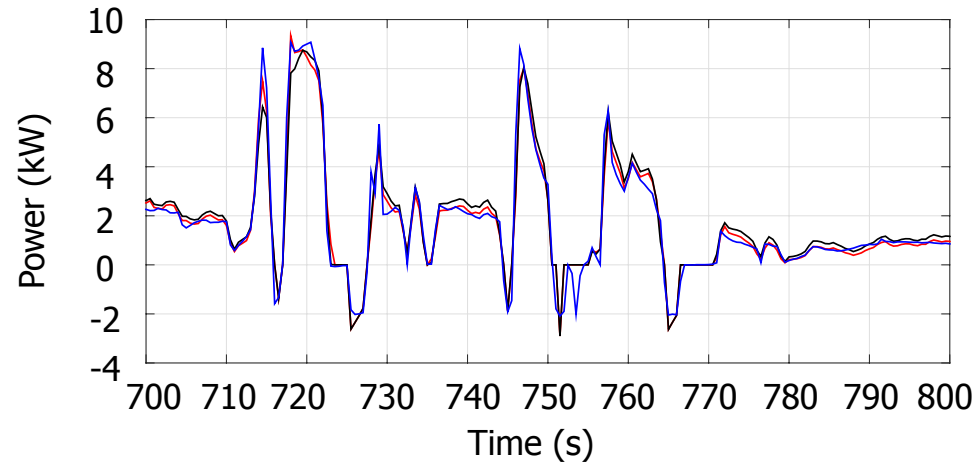
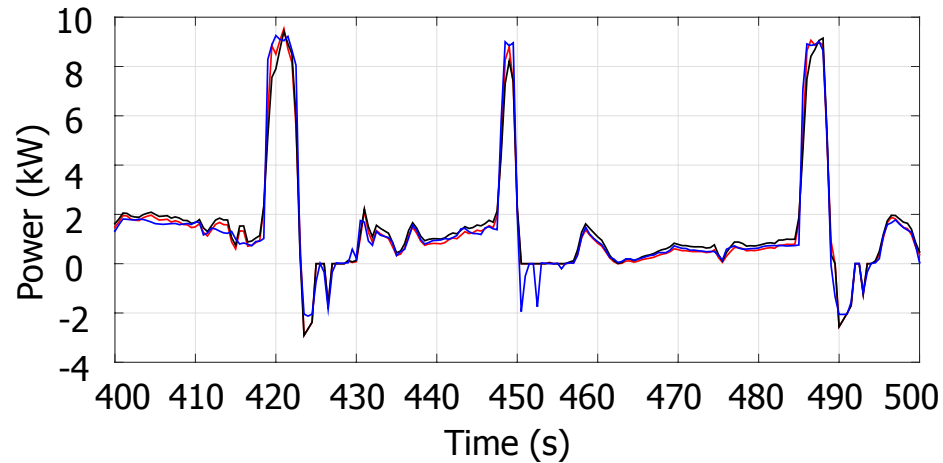
- Drives C and D
  - Speed range: 5 km/h to 32 km/h
  - Degree range:  $-0.6^\circ$  to  $0.85^\circ$



# Remaining range estimation

- Drives C and D

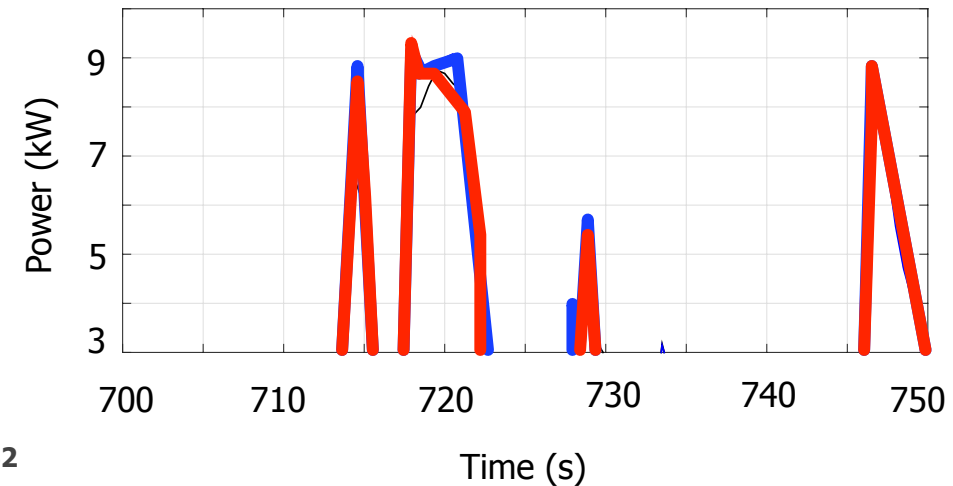
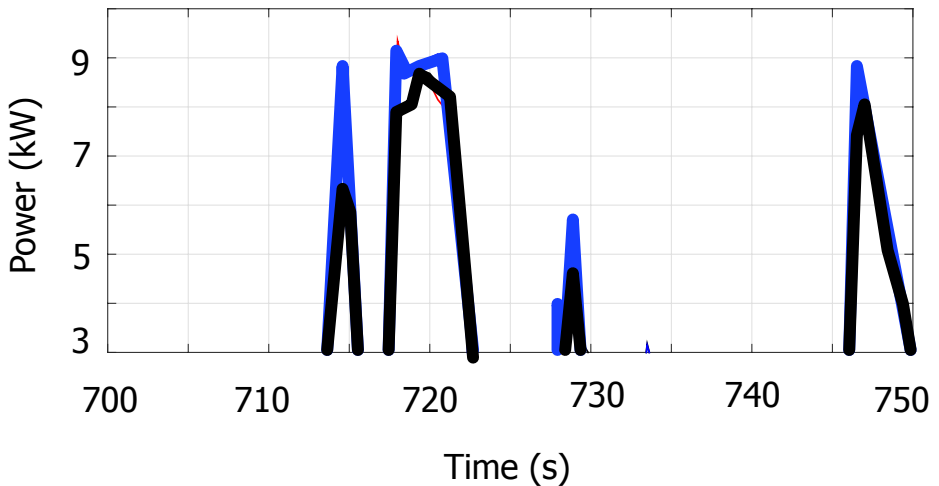
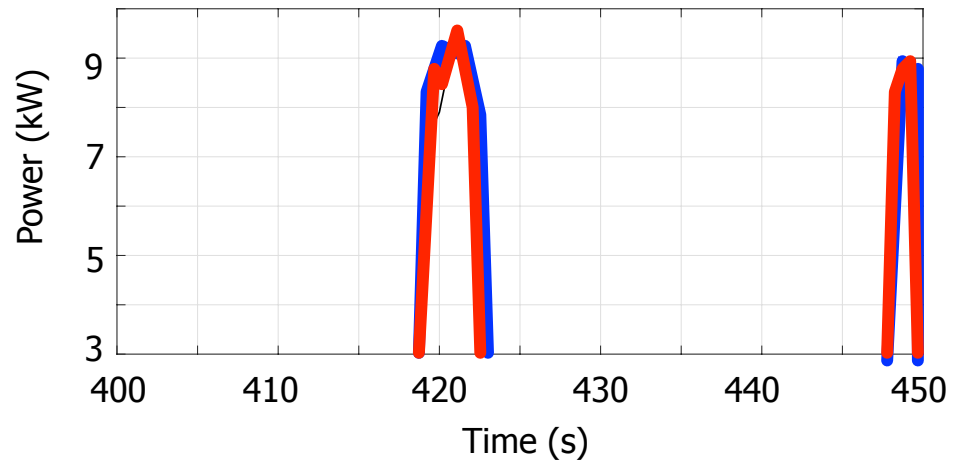
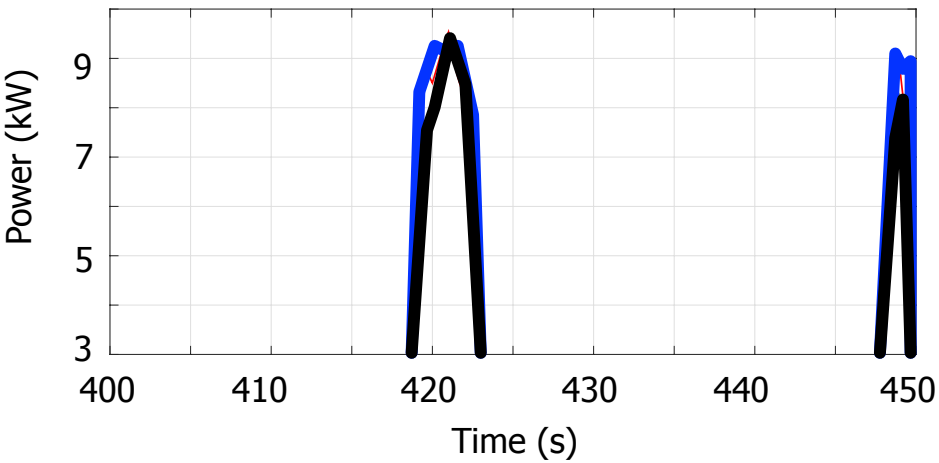
— Hybrid — Dynamics — Measured



# Remaining range estimation

- Closer look at drives C and D

Hybrid Dynamics Measured





# Outline

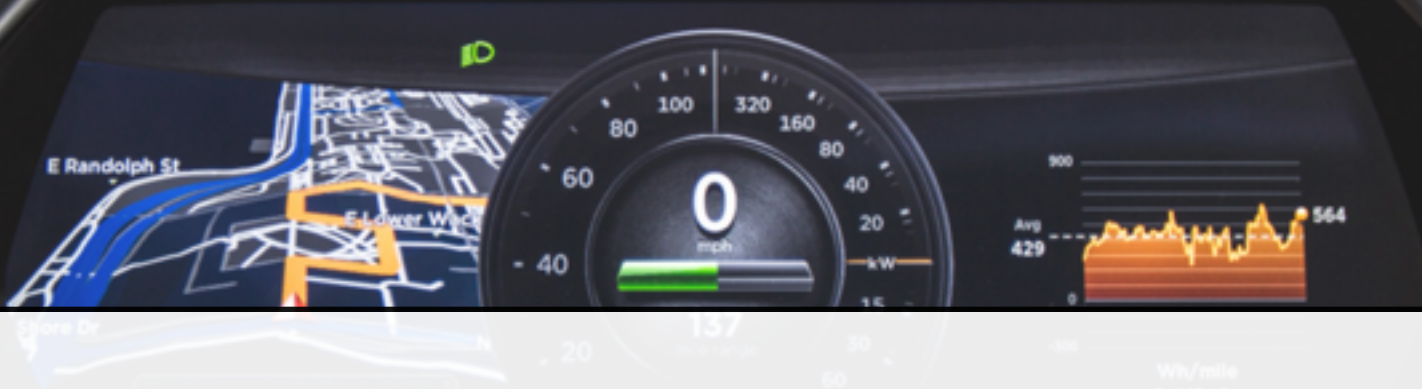
- Motivation
- Related works
- Our framework
- Experiment
- **Conclusions**



# Conclusions

- We achieve higher remaining range accuracy
- The absolute average errors for **hybrid power model**, advanced dynamics model, and vehicle dynamics model are **2.52%**, 6.85%, 9.33% respectively
- The hybrid power model shows increased estimation accuracy not only in the total remaining range, but also in the instantaneous power estimation





**Thanks for your attention!**

137  
21W 0:00 8:21 AM



# High speed custom EV

