



A Unified Framework Processing False Paths and Multi-cycle Paths in Static Timing Analysis

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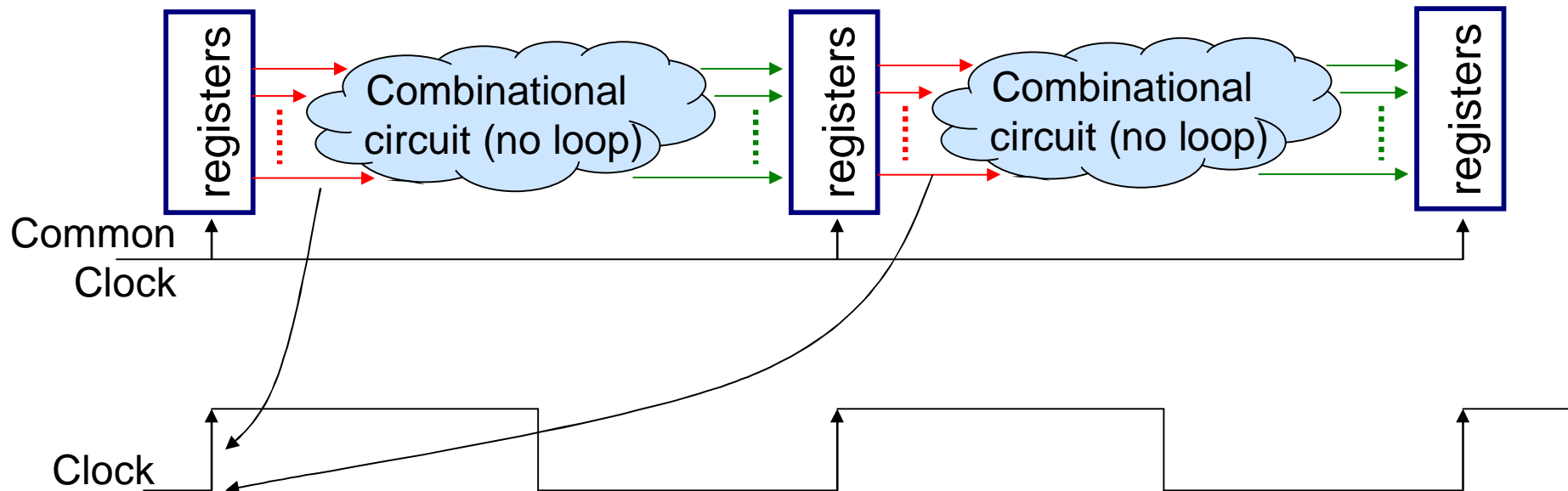


Outline

- **Background and Problem Statement**
 - Static Timing Analysis (STA)
 - False Paths and Multi-cycle Paths
 - Previous Works on False Paths
- **Our Contributions**
 - Unified Framework: Rules and Rule Sets
 - Rule Collection Minimization: Extension of our Previous Work ^[4]
- **Experimental Results**
- **Conclusions**

Overview of STA [1]

- Formulate combinational circuits between latches into graphs, $G = \{V, E\}$



Overview of STA (cont)

- Dynamic programming

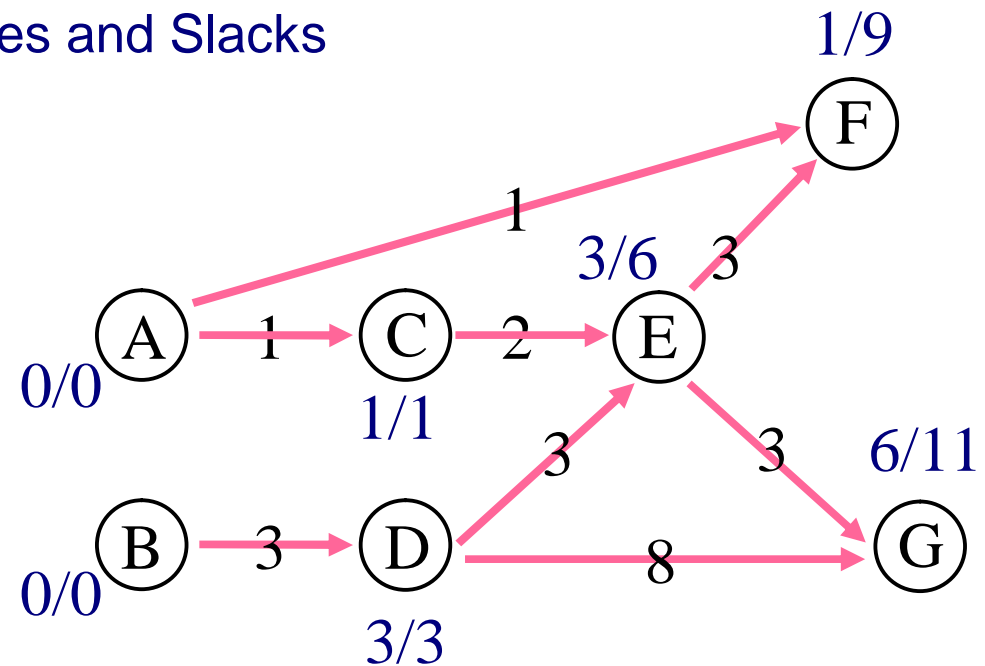
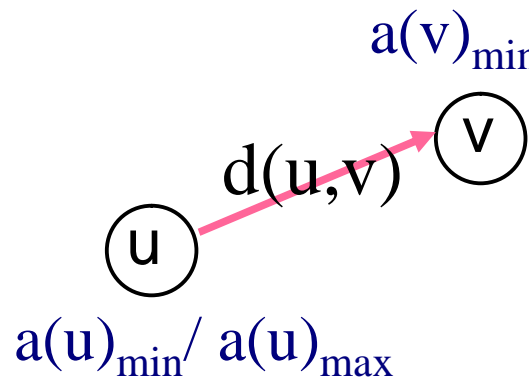
- One forward sweeping: longest/shortest paths

- $a(v)_{\min} = \min(a(u)_{\min} + d(u,v))$, $a(v)_{\max} = \max(a(u)_{\max} + d(u,v))$

- General delay bounds, $h \leq \text{delay}(\text{path}) \leq s$

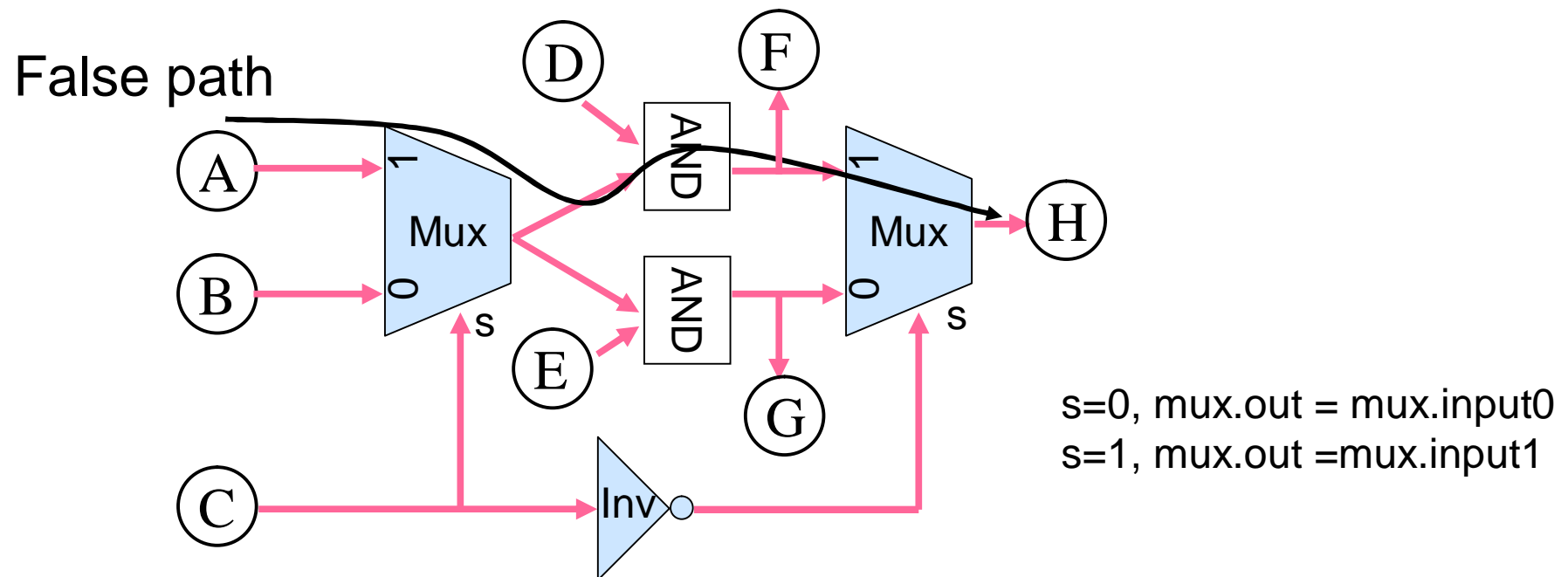
- One backward sweeping

- Required arrival times and Slacks



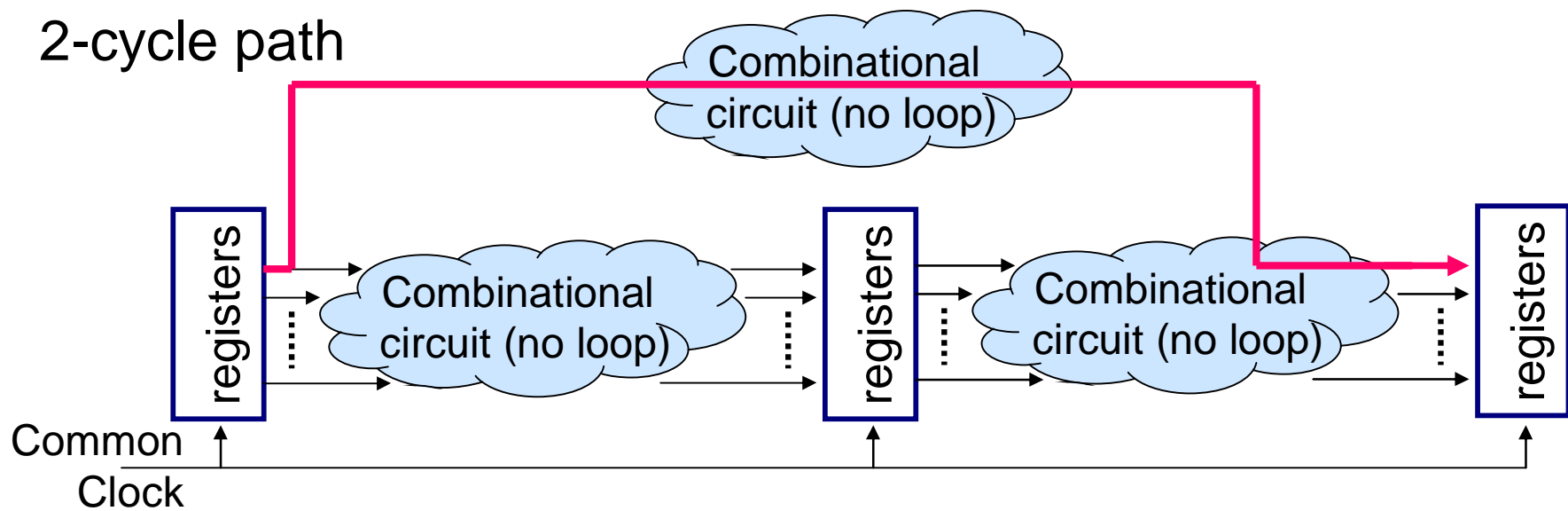
False Paths

- A path not logically realizable.



Multi-cycle Paths

- A path signals propagate longer than one cycle.





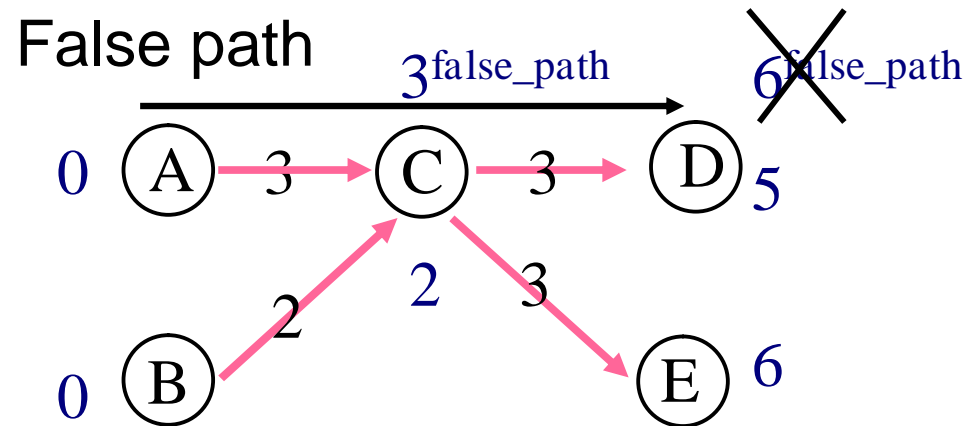
Statement of Problem

Given a set of false paths and multi-cycle paths

- remove false path timing, and compute multi-cycle path slacks with multi-cycle required time in linear time.

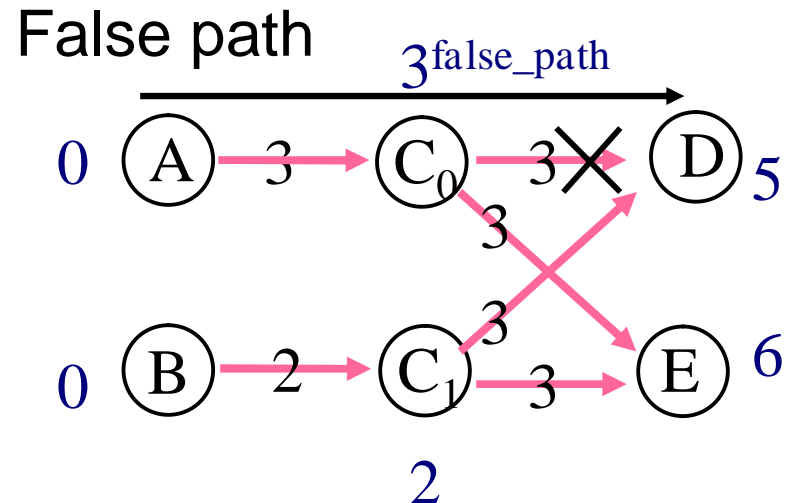
Previous Works on False Paths

- Labeling [2]: remove false path arrival times with tags.



Previous Works (cont)

- Node splitting ^[3] :
 - Create a new node for each tagged timing
 - Remove false paths by edge removal.
 - Minimize #nodes be split.



- Two-direction propagation minimizes #tags ^[4].



Contributions

■ Unified Framework

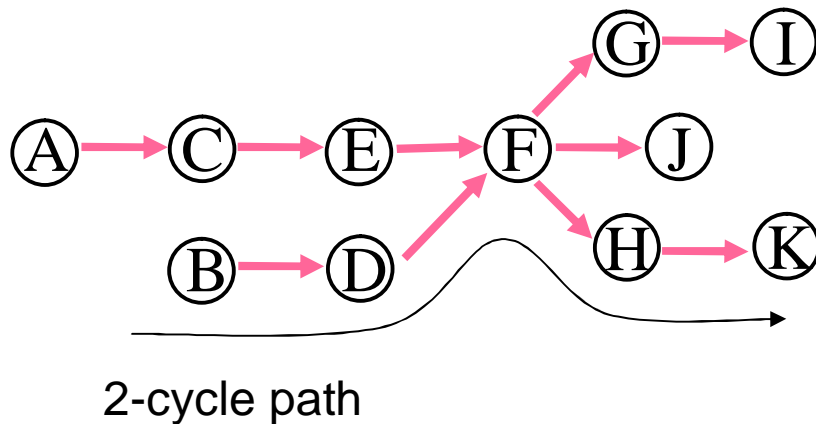
- Represent false paths and multi-cycle paths as Exceptional Rules.
- Follow labeling approach^[2] to deal with false paths and multi-cycle paths.

■ Tag Minimization

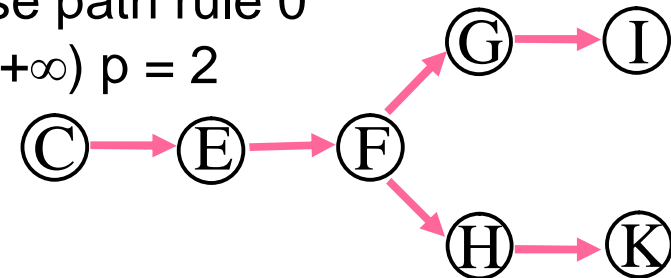
- Follow two-direction propagation^[4] to minimize #tags.
- Minimize #tags = Minimize #distinct arrival times
=> improve analysis efficiency.

Exceptional Rules

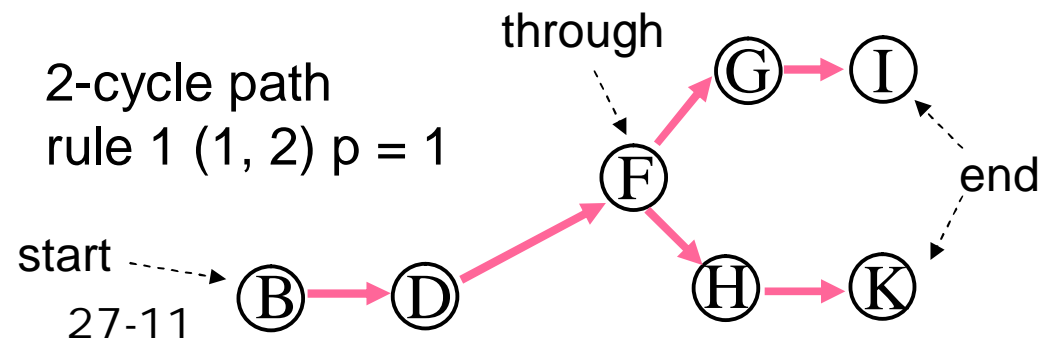
- Rule r
 - $G_r = \{V_r, E_r\}$, sub graph
 - Delay bounds (h_r, s_r) , $h_r \leq \text{delay}(\text{path}) \leq s_r$.
 - Rule priority p
- Rule sets through an edge, $I(u, v)$
- Rule sets from and to vertex v , $F(v)/T(v)$



False path rule 0
 $(-\infty, +\infty)$ $p = 2$

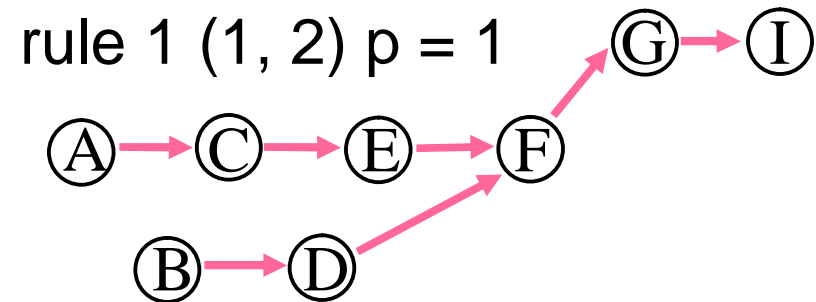
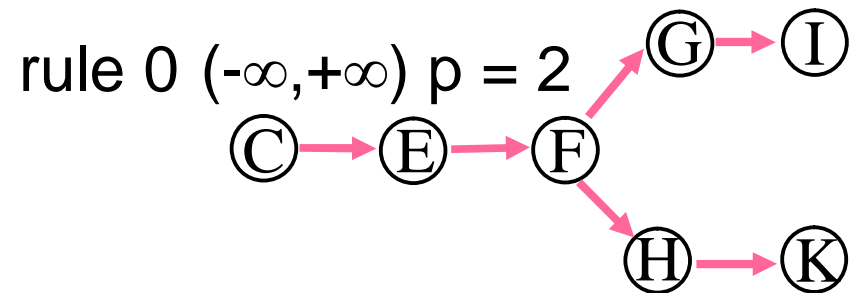
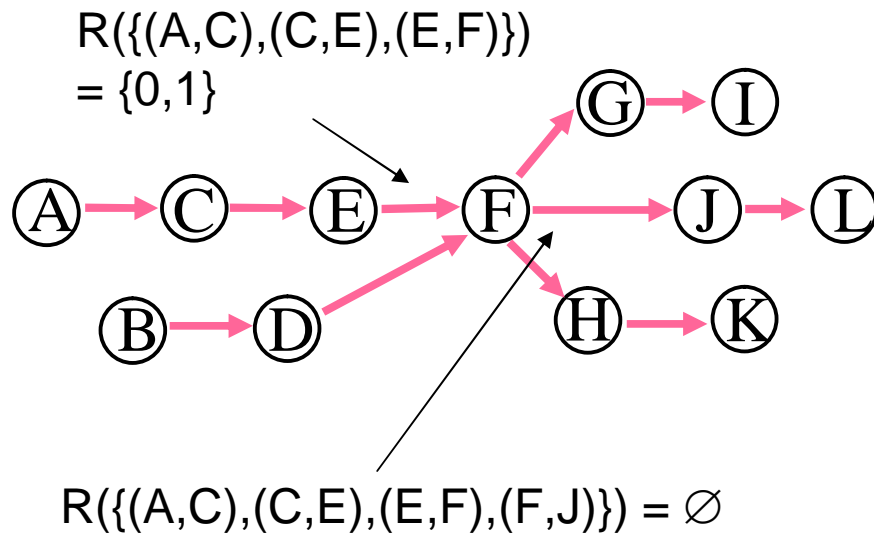


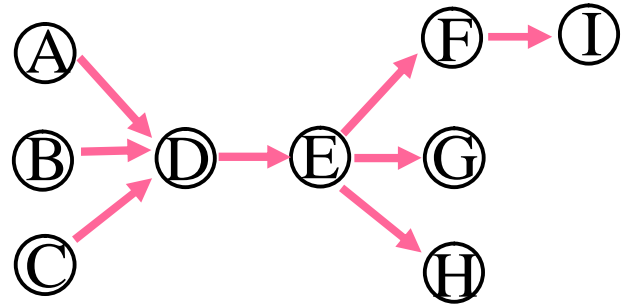
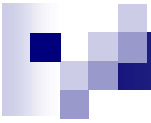
2-cycle path
 rule 1 $(1, 2)$ $p = 1$



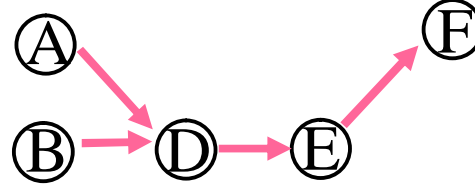
Use Rule Sets as Timing Tags^[2]

- Prefix path p^- at vertex v from PI to v
- **Prefix Rule Set** $R(p^-)$ contains rule r iff p^- belongs to false paths or multi-cycle paths specified by r .





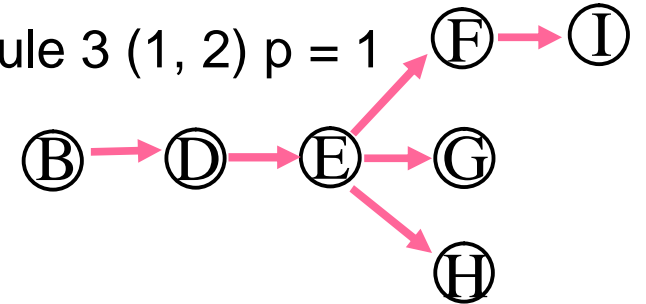
rule 1 $(-\infty, +\infty)$ $p = 2$



rule 2 $(-\infty, +\infty)$ $p = 2$



rule 3 $(1, 2)$ $p = 1$

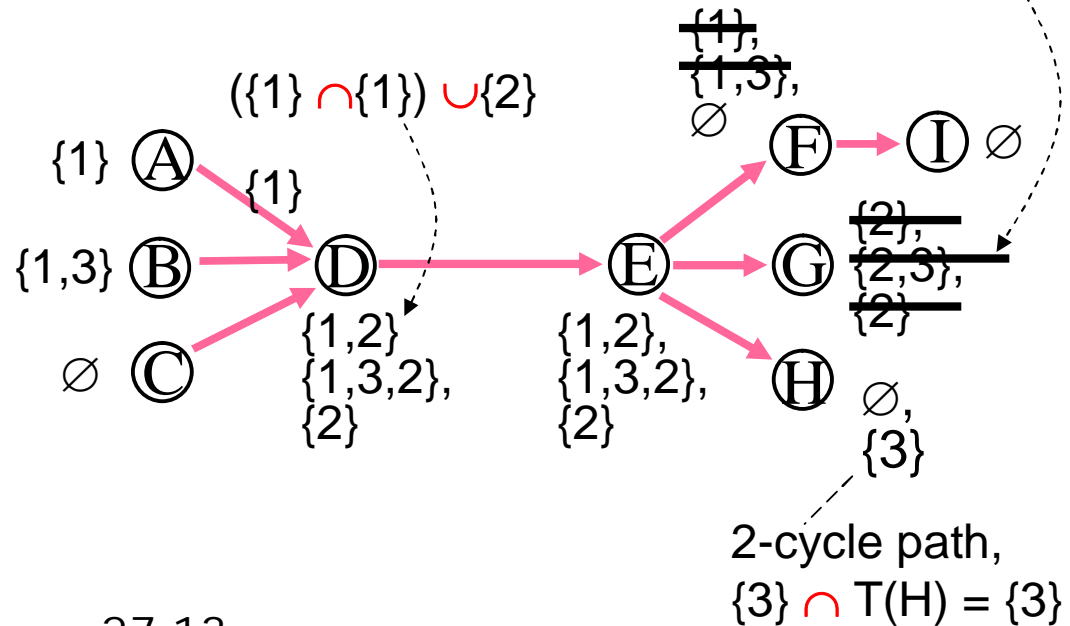


False paths,
 $\{2,3\} \cap T(G) = \{2,3\}$,
 rule 2 dominates

Rule sets

Compute Rule Sets in Forward Sweeping:

- 1) Primary inputs $\Rightarrow R(p-) = F(v)$
- 2) $R(p-)' = (R(p-) \cap I(u,v)) \cup F(v)$
- 3) $R(p-)' \cap T(v) \neq \emptyset \Rightarrow$
 rule $r \in R(p-)' \cap T(v)$ with highest priority dominates



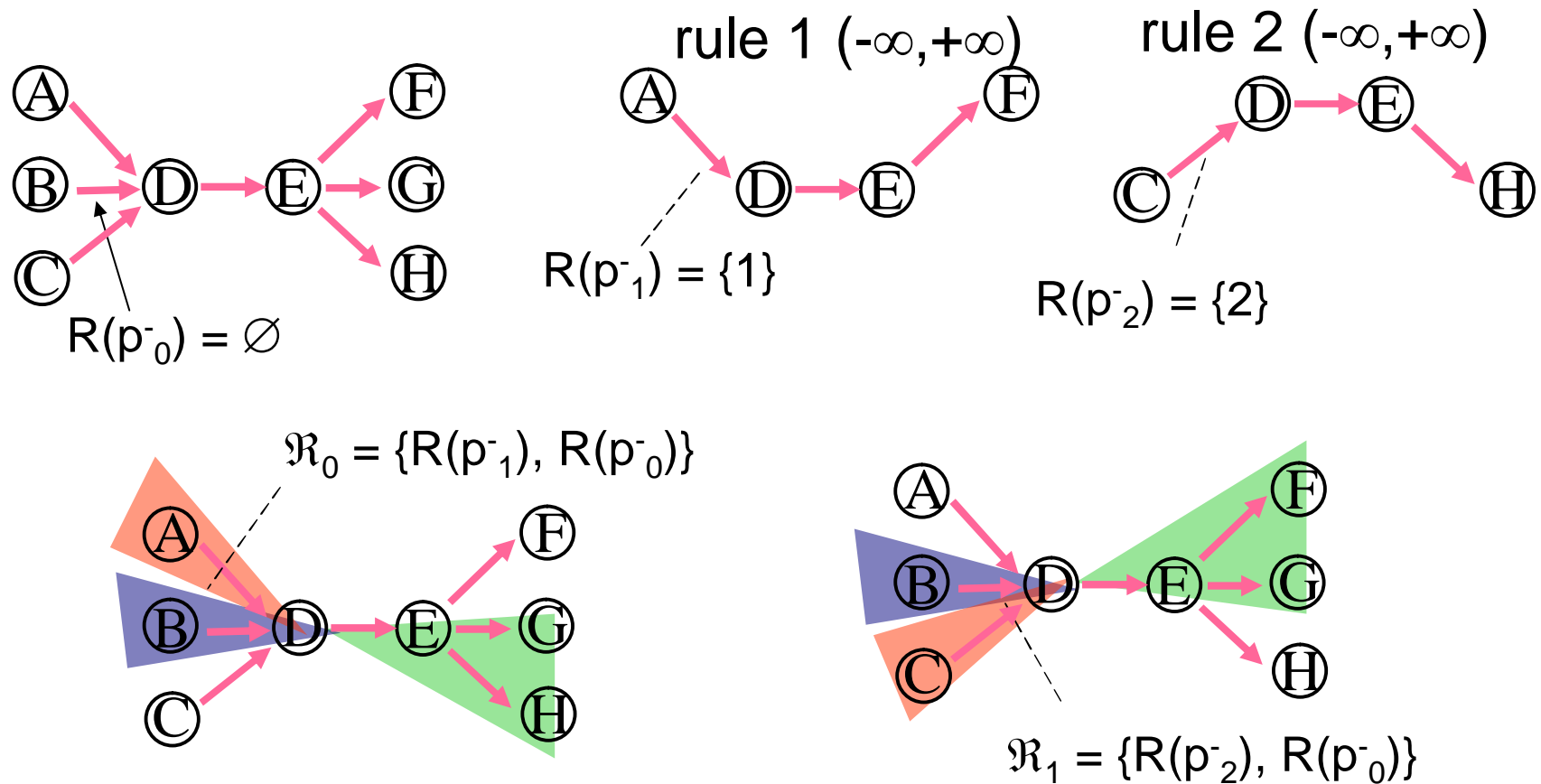


Tag Minimization

- When there are a large number of false paths and multi-cycle paths,
 - ☹ Too many tagged timings=>Slow Timing Analysis
- Tag Minimization
 - Follow two-direction propagation [4].
 - Expand to multi-cycle paths.

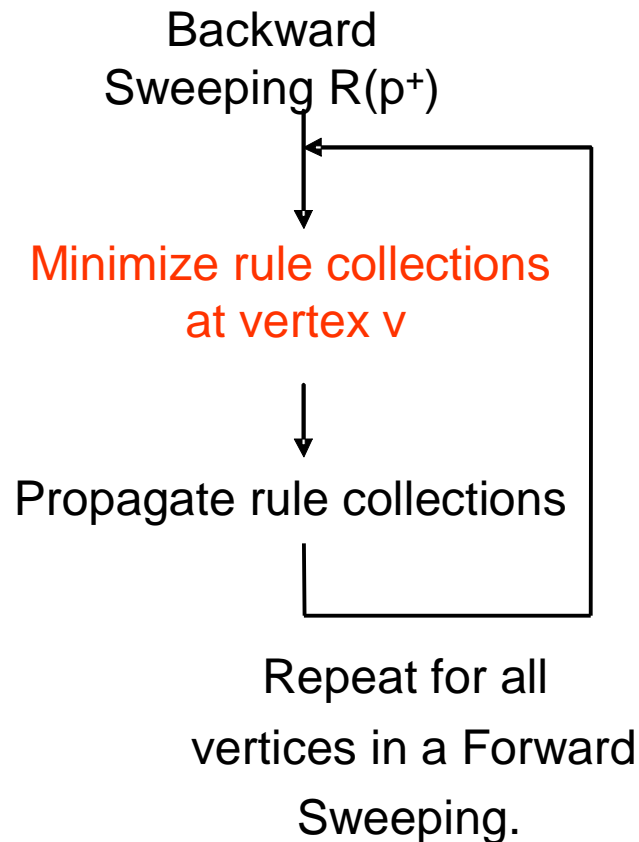
Basic idea of tag minimization

- Tags can be merged when timing information can be shared.



Rule Collection Minimization

Flow



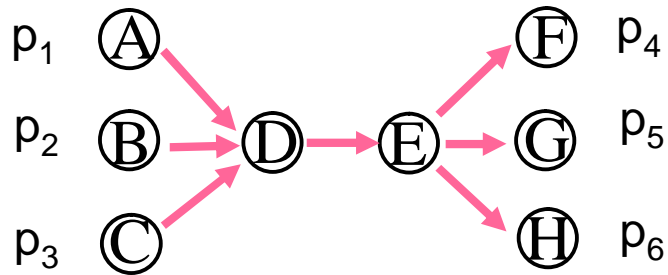
Minimization at vertex v

Construct non-false paths attached with setup times and hold times

Devise timing shifting to align setup times and hold times

Cover distinct non-false path times with rule collections

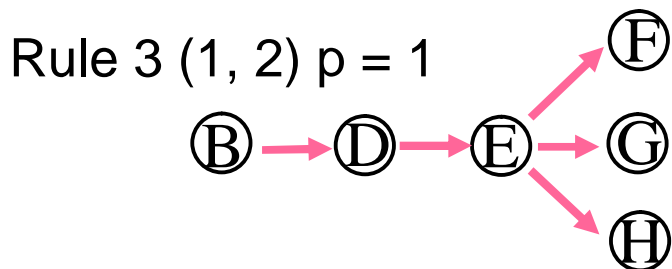
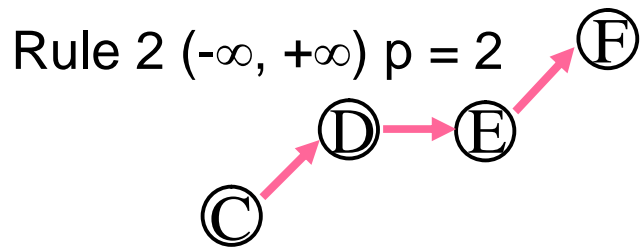
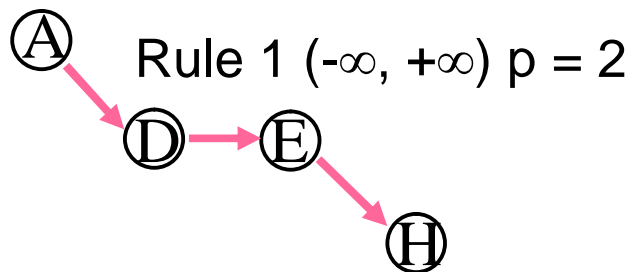
Intersections and Bipartite Graph



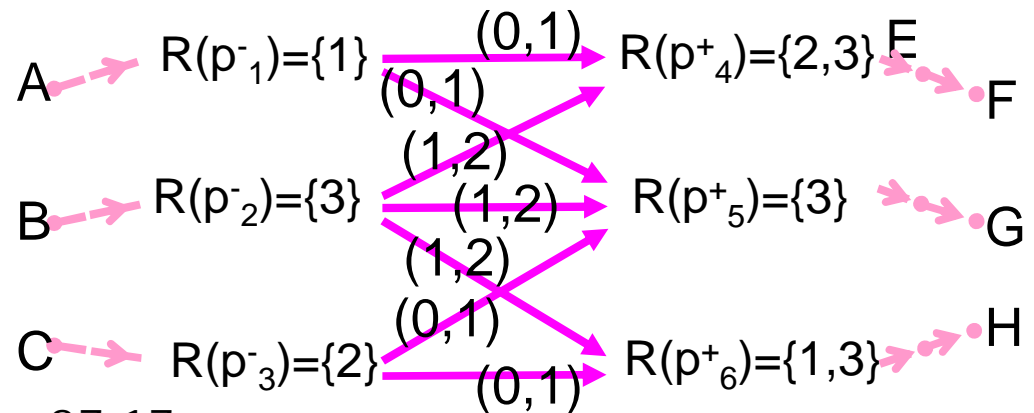
$r \in R(p^-) \cap R(p^+) \iff$ a path governed by r

Intersect $R(p^-)$ and $R(p^+)$ at vertex D

| $R(p^-) \backslash R(p^+)$ | $R(p^+_4) = \{2,3\}$ | $R(p^+_5) = \{3\}$ | $R(p^+_6) = \{1,3\}$ |
|----------------------------|-------------------------------|--------------------|-------------------------------|
| $R(p^-_1) = \{1\}$ | \emptyset | \emptyset | $\{1\}$ |
| $R(p^-_2) = \{3\}$ | $\{3\}$ | $\{3\}$ | $\{3\}$ |
| $R(p^-_3) = \{2\}$ | $\{2\}$ | \emptyset | \emptyset |

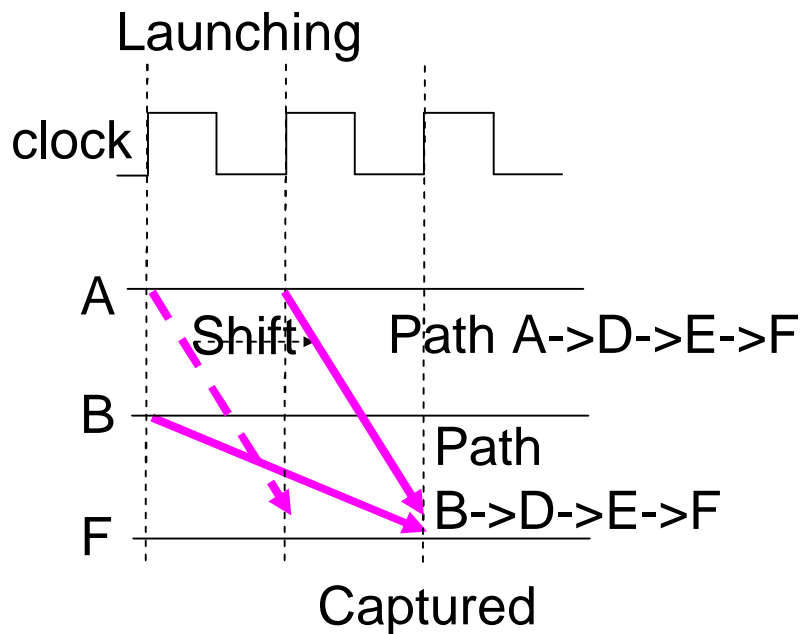


Bipartite graph at D



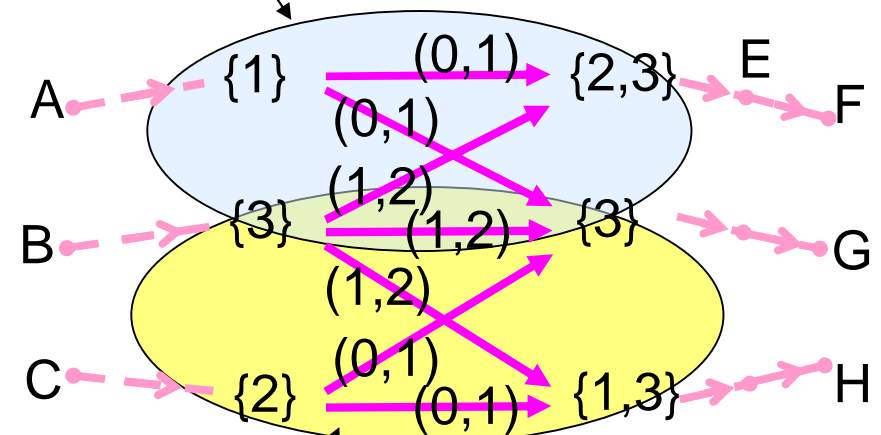
Time Shifting and Biclique Covering [5][6]

Align setup and hold times of two paths.



biclique 1 :

$$\mathfrak{R}_1 = \{R(p_1^-)^{+1}, R(p_2^-)\} = \{\{1\}^{+1}, \{3\}\}$$



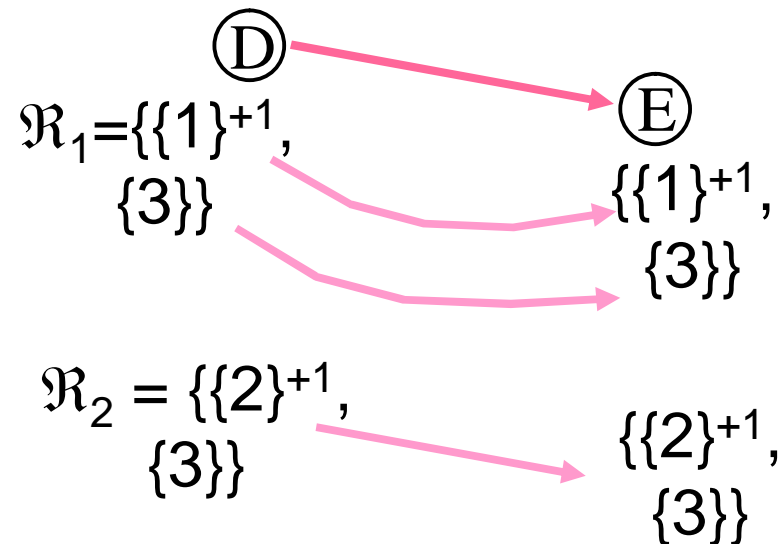
biclique 2 :

$$\mathfrak{R}_2 = \{R(p_3^-)^{+1}, R(p_2^-)\} = \{\{2\}^{+1}, \{3\}\}$$

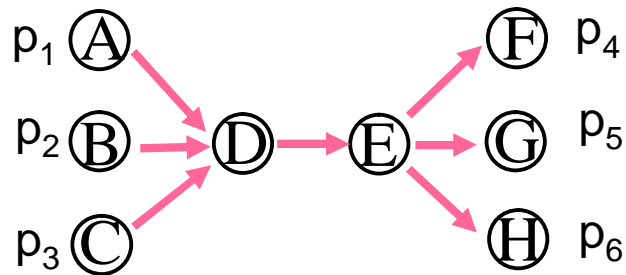
$$\mathfrak{R} = \cup \{R(p_i^-)^{+\Delta_{\text{cycle}}}\}, R(p_i^-) \in \text{biclique}$$

Propagate Rule Collections

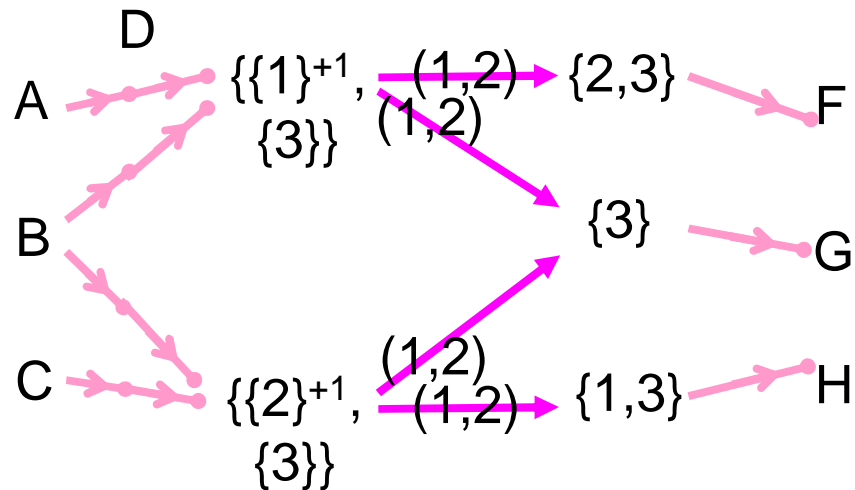
- Propagate **every** rule set $R(p^-) \in \mathfrak{R}(u)$ from vertex u to v
 - Each $R(p^-)' = (R(p^-) \cap I(u, v)) \cup F(v)$.



Minimization at Vertex E



Bipartite graph at E



Intersections at vertex E

| \mathcal{R} \ $R(p^+)$ | $R(p^+_4)=\{2,3\}$ | $R(p^+_5)=\{3\}$ | $R(p^+_6)=\{1,3\}$ |
|--------------------------------------|--|--------------------------|--|
| $\mathcal{R}_1 = \{\{1\}^+, \{3\}\}$ | $\{\emptyset^+, \{3\}\}$ | $\{\emptyset^+, \{3\}\}$ | $\{\{1\}^+, \{3\}\}$ |
| $\mathcal{R}_2 = \{\{2\}^+, \{3\}\}$ | $\{\{2\}^+, \{3\}\}$ | $\{\emptyset^+, \{3\}\}$ | $\{\emptyset^+, \{3\}\}$ |

Setup and hold times Conflict
 => Path Timing is not shared
 => Produce no edge



Correctness

If multi-cycle path rules satisfy:

- sub graph G_r are from primary inputs to primary outputs of graph G

Timing analysis with rule collections as timing tags

- Computes slacks of non-false paths, and the multi-cycle path slacks are computed using multi-cycle required times.

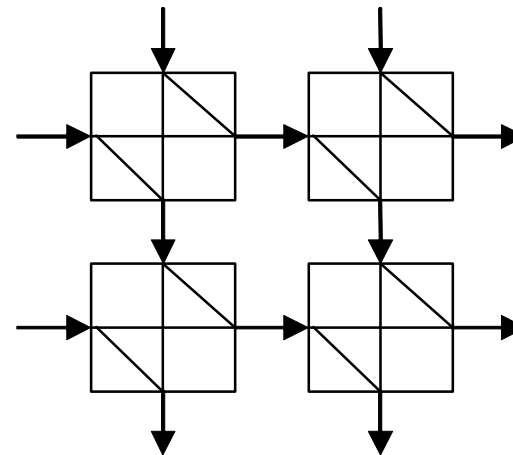


Complexity

- n : the number of vertices in graph
- k : total number of edges in false paths and multi-cycle paths
- $t(v)$: the number of tags at vertex v is $O(k)$
- Run time of minimization at v is $O(k^3)$
- Total run time is $O(nk^3)$

Experiments on Artificial Cases

- 100×100 cell **mesh**.
- Each cell with 2 inputs, and 2 outputs.
- Randomly produced rule.
- Each G_r with 2-4 PIs, 2-4 POs, and 6000 edges.
- $(h_r, s_r) = (1, 2)$ or $(-\infty, +\infty)$



$$\%imp = \frac{\# \text{ prefix rule set } R(p^-) - \# \text{ rule collection } \mathcal{R}}{\# \text{ prefix rule set } R(p^-)}$$



Experimental Results

| #rules | # Prefix Rule set $R(p^-)$ | #Rule collection $\mathfrak{R}(p^-)$ | %imp | CPU(s) |
|---------|----------------------------|--------------------------------------|--------|--------|
| 9 | 9129 | 8281 | 9.29% | 2 |
| 34 | 77102 | 49321 | 36.03% | 19 |
| 69 | 137581 | 89987 | 34.59% | 44 |
| 88 | 176384 | 97124 | 44.94% | 61 |
| 104 | 209718 | 145484 | 30.63% | 87 |
| average | | | 31.10% | |

Experiments on 4 Industry Cases

| Case | # nets | # rules | | # Prefix Rule Set $\mathcal{R}(p^-)$ | #Rule Collection $\mathcal{R}(p^-)$ | %imp |
|-----------|---------|---------|-------------|--------------------------------------|-------------------------------------|--------|
| | | false | Multi-cycle | | | |
| tdl | 27,555 | 1 | 27 | 9129 | 8281 | 9.29% |
| cq_mod | 38,535 | 2517 | 3181 | 77102 | 49321 | 36.03% |
| pm25c | 325,582 | 7 | 2574 | 137581 | 89987 | 34.59% |
| atml_core | 533,224 | 2 | 2262 | 176384 | 97124 | 44.94% |

Run Time Analysis

| Case | Minimization CPU(s) | STA Run Time | | |
|-----------|------------------------|---|---|------------|
| | | Use Prefix Rule Set $\mathcal{R}(p^-)$ | Use Rule Collection $\mathcal{R}(p^-)$ | %reduction |
| tdl | 2 | 1.2 | 1.2 | 0 |
| cq_mod | 19 | 4.2 | 2 | 52.38% |
| pm25c | 44 | 55.33 | 28.5 | 48.49% |
| atml_core | 61 | 40.33 | 19.5 | 51.65% |
| average | | | | 38.13% |

$$\% \text{reduction} = \frac{\text{STA runtime using } \mathcal{R}(p^-) - \text{STA runtime using } \mathcal{R}}{\text{STA runtime using } \mathcal{R}(p^-)}$$



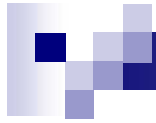
Conclusions

- We propose a framework to unify the false paths and multi-cycle path constraints .
- We use two-direction propagation approach to produce minimized number of tags for false path and multi-cycle paths. .
- The experimental results on 4 industry test cases show that STA run time is reduced by 38.13% in average. The runtime of the minimization is only 61 seconds for the largest case.



References

- [1] R. B. Hitchcock, "Timing Verification and Timing Analysis Program", DAC 1982, pp. 594-604.
- [2] K. P. Belkhale, et. al., "Timing Analysis with known False Sub-Graphs", ICCAD 1995, pp. 736-740.
- [3] D. Blaauw, et. al., "Removing user-specified false paths from timing graphs", DAC 2000, pp. 270-273.
- [4] S. Zhou, B. Yao, H. Chen, Y. Zhu, C.K. Cheng, M. Hutton, et al., "Improving the efficiency of Static Timing Analysis with False Paths", IEEE/ACM Int. Conf. CAD 2005, pp. 527-531.
- [5] J. Orlin, "Containment in graph theory: Covering graphs with cliques", Nederl. Akad. Wetensch. Indag. Math., 39:211-218, 1977.
- [6] H. Muller, "Alternate Cycle-Free Matchings", Order, (7):11-21, 1990.



Thank you!