

Evaluation of Runtime Monitoring Methods for Real-Time Event Streams

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Jan. 21. 2015

Overview

- 1 Motivation
- 2 Background
- 3 Comparison
 - Comparison based on standard arrival curves
 - Comparison based on complex arrival curves
- 4 FPGA evaluations
- 5 Summary

Outline

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Motivation

Real-time system at runtime

Why real-time system needs to be monitored?

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Monitor is used to guarantee the system runtime behaviors

What monitors do?

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What monitors do?

- System events are monitored
- Violation is reported by the monitor

Subject of this paper

State-of-art

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- Dynamic counters (Kai et.al, 2011)

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Contributions

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- Analyzed the differences of dynamic counters and l -repetitive function

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- Developed a new approach to apply dynamic counters to monitor periodic-burst events

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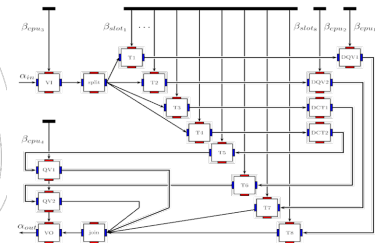
Contributions

- Analyzed the differences of dynamic counters and *l*-repetitive function
- Developed a new approach to apply dynamic counters to monitor periodic-burst events
- Prototyped hardware implementations on FPGA and presented FPGA resource usage

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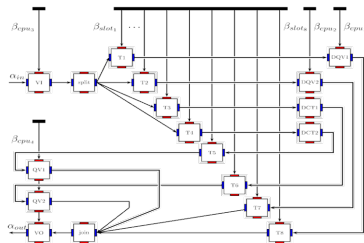
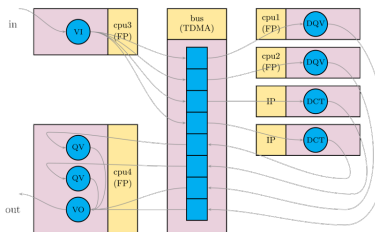
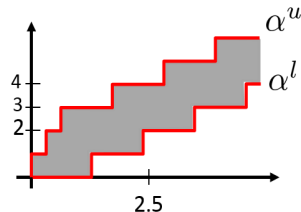
Biao Hu



The corresponding RTC-MPA model

Arrival Curve (Modular Performance Analysis)

Arrival curve: Event stream model,
 $\alpha^l(t-s) \leq R[s, t] \leq$
 $\alpha^u(t-s), \forall t \geq s \geq 0$, where
 $R[s, t]$ denote the number of events
in the time interval $s \leq \tau < t$.



System view of the M-JPEG

The corresponding RTC-MPA model

Distance Function (Compositional Performance Analysis)

Minimum/maximum distance function

The minimum distance function $d^{\min}(n)$ specifies the minimum distance between $n + 1$ consecutive events in an event stream.

The maximum distance function $d^{\max}(n)$ specifies the maximum distance between $n + 1$ consecutive events in an event stream.

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An example: periodic events with jitter

Arrival Curve

- (a) *Upper Arrival Curves* : $\alpha^u(\Delta) = \lfloor \frac{\Delta + J}{\delta} \rfloor$
- (b) *Lower Arrival Curves* : $\alpha^l(\Delta) = \max\{0, \lfloor \frac{\Delta - J}{\delta} \rfloor\}$

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Distance Function

- (a) *Minimum Distance Functions* : $d^{\min}(n) = \max\{0, n \cdot \delta - J\}$
- (b) *Maximum Distance Functions* : $d^{\max}(n) = n \cdot \delta + J$

Dynamic counter

Assumption

Any monotonous and time-invariant arrival curve can be conservatively approximated as the minimum on a set of staircase functions with the form $\alpha_i^u(\Delta) = N_i^u + \lfloor \frac{\Delta}{\delta_i} \rfloor$.

$$\forall \Delta \in \mathbb{R}_{\geq 0} : \alpha^u(\Delta) \geq \min_{i=1..n} (\alpha_i^u(\Delta))$$

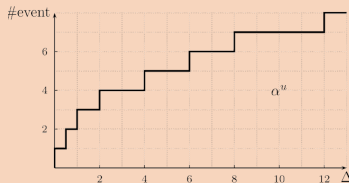
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Method: one dynamic counter is responsible for monitoring one staircase function



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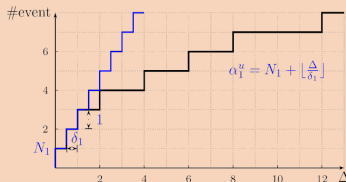
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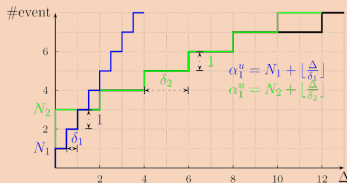
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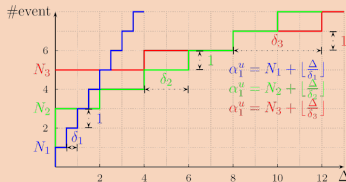
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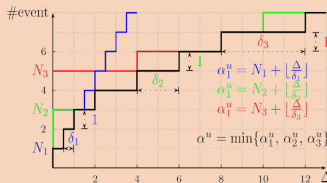
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- $DC_2 \leftrightarrow \alpha_2$
- $DC_3 \leftrightarrow \alpha_3$
- $\min(DC_1, DC_2, DC_3) \leftrightarrow \min(\alpha_1, \alpha_2, \alpha_3)$



l -repetitive function

Definition

A l -repetitive function is a special minimum distance function that

$$\text{satisfies: } d(n) = \begin{cases} d_n(\text{given}), & n \leq l, \\ \max_{\omega \in [1, l]} (d(\omega) + d(n - \omega)), & n > l. \end{cases}$$

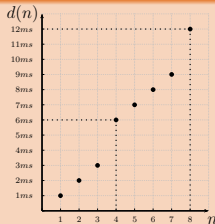
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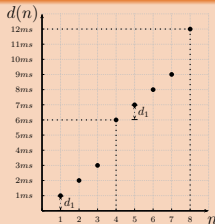
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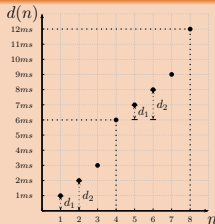
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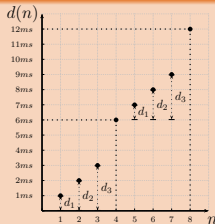
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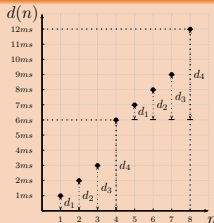
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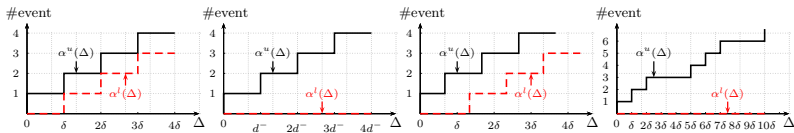


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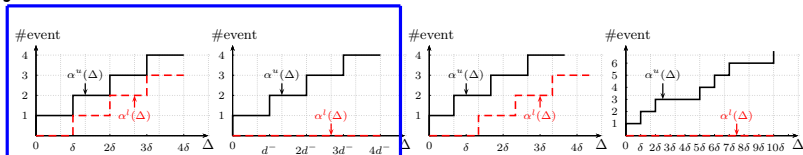
Standard arrival events (Richter et al., 2003)

Periodic events, Sporadic events, Periodic events with jitter, Periodic burst events.



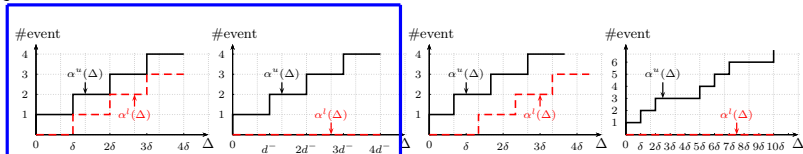
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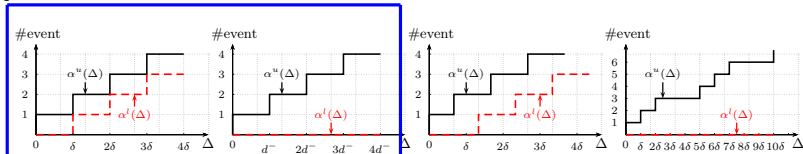


Periodic events & Sporadic events

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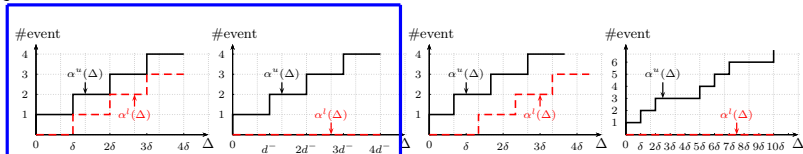
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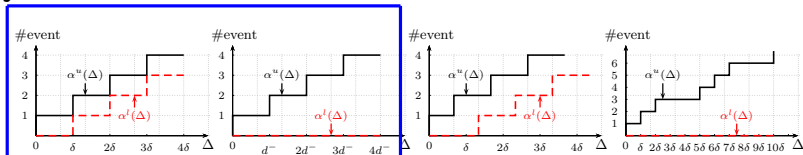
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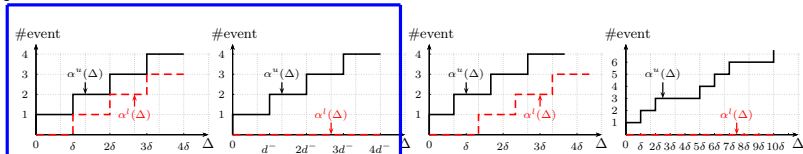
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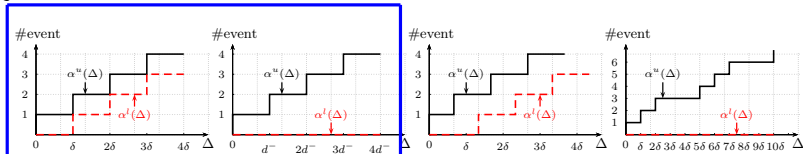
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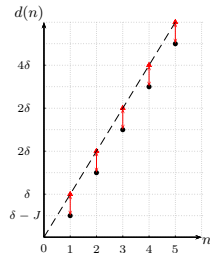
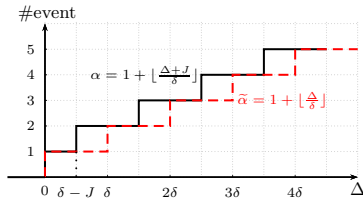
When J is greater than δ , an initial burst N happens.

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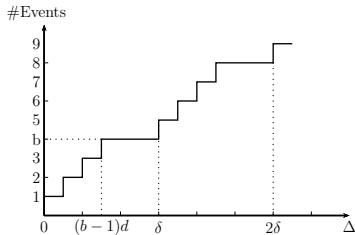
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The jitter always exist when using dynamic counters or l -repetitive function

- 1 Only one dynamic counter
- 2 $l = 1$ for l -repetitive function

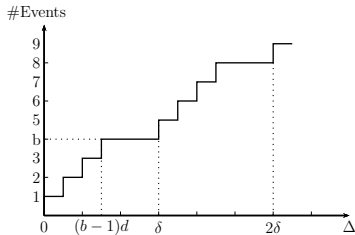
Periodic burst events



Definition

$$\alpha^u(\Delta) = \lfloor \frac{\Delta}{\delta} \rfloor b + \min(\lceil \frac{\Delta - \lfloor \frac{\Delta}{\delta} \rfloor \delta}{d} \rceil, b)$$
 where d is the minimum timing separation, b is the maximum events within an interval δ .

Periodic burst events



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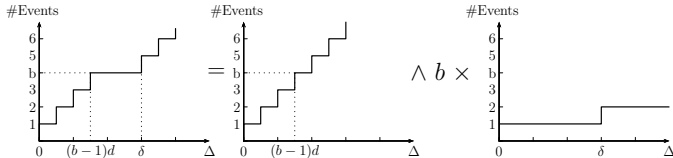
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Monitoring method

- 1 l -repetitive function: $l = b$
- 2 dynamic counters: ?

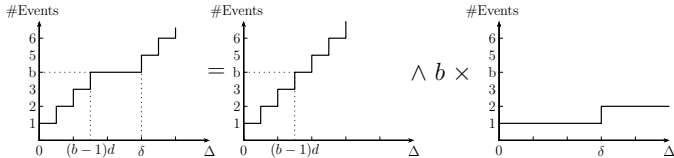
Dynamic counters

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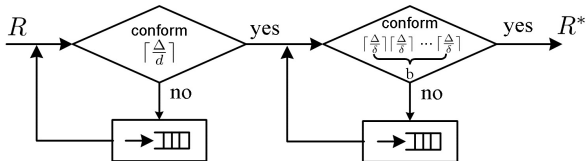


Periodic burst is equivalent to a staircase function with a period d , and the constraint of b staircase functions with a period of δ .

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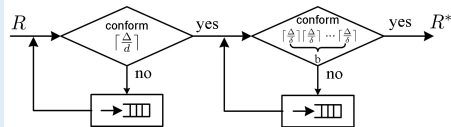


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A case study of monitoring periodic burst by dynamic counters

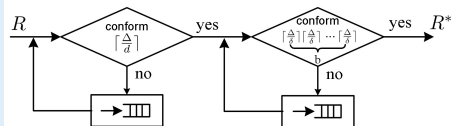
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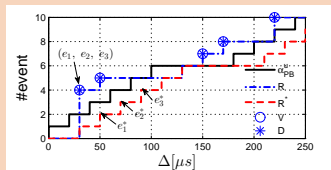
A case simulation: $b = 6$, $\delta = 180$, and $d = 20$

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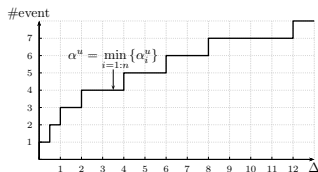


A case simulation: $b = 6$, $\delta = 180$, and $d = 20$



Complex arrival curve of Type 1

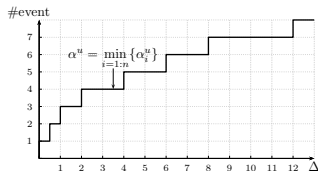
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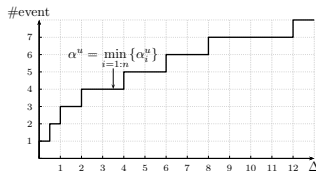


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- 1 Dynamic counters: n counters

Complex arrival curve of Type 1

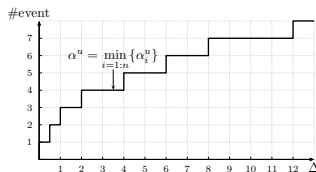


Arrival curve is the minimum of a set of staircase functions, i.e.,

$$\alpha^u = \min_{i=1:n} \{\alpha_i^u\}, \text{ where } \alpha_i = N_i^u + \lfloor \frac{\Delta}{\delta_i} \rfloor \quad (N_i^u < N_{i+1}^u, \delta_i < \delta_{i+1})$$

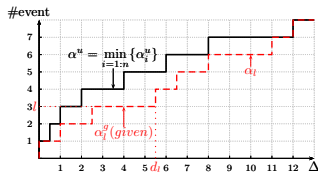
- 1 Dynamic counters: n counters
- 2 l -repetitive function: ?

Complex arrival curve of Type 1



For l -repetitive function

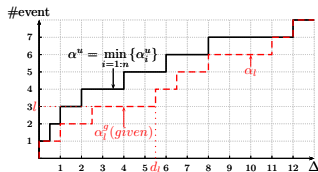
Complex arrival curve of Type 1



For I -repetitive function

- 1 Assume the repetitive segment is α_I^g that is given in the offline analysis. $\alpha_I(\Delta) = \begin{cases} \alpha_I^g(\Delta)(given), & \text{if } \Delta \leq d_I, \\ \alpha_I^g(\Delta - k \cdot d_I), & \text{if } \Delta > d_I. \end{cases}$

Complex arrival curve of Type 1

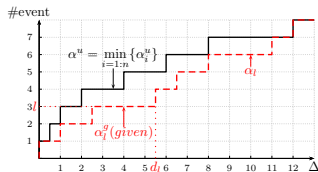


For l -repetitive function

- 1 Assume the repetitive segment is α_l^g that is given in the offline analysis. $\alpha_l(\Delta) = \begin{cases} \alpha_l^g(\Delta)(given), & \text{if } \Delta \leq d_l, \\ \alpha_l^g(\Delta - k \cdot d_l), & \text{if } \Delta > d_l. \end{cases}$

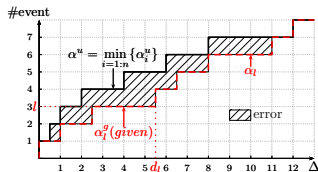
- 2 $\lim_{\Delta \rightarrow +\infty} \{ \min_{i=1..n} \{ \alpha_i(\Delta) - \alpha_l(\Delta) \} = N_x^u + \lfloor \frac{\Delta}{\delta_{max}} \rfloor - \frac{\Delta}{d_l} l \geq 0. \Rightarrow d_l \geq l \cdot \delta_{max}. \}$

Complex arrival curve of Type 1



For l -repetitive function

Complex arrival curve of Type 1

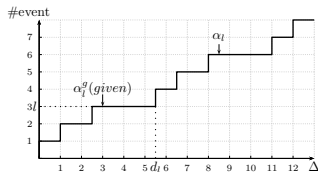


For l -repetitive function

1 Error percent (EP):
$$EP(\Delta) = \frac{\int_0^\Delta (\alpha^u(t) - \alpha^g(t)) dt}{\int_0^\Delta \alpha^u(t) dt}.$$

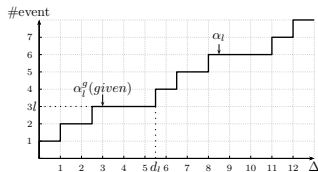
Complex arrival curve of Type 2

Complex arrival curve of Type 2



Arrival curve is segmentally repetitive, and each segment is sub-additive,
i.e., $\alpha_l(\Delta) = \begin{cases} \alpha_l^g(\Delta)(given), & \text{if } \Delta \leq d_l, \\ \alpha_l^g(\Delta - k \cdot d_l), & \text{if } \Delta > d_l. \end{cases}$

Complex arrival curve of Type 2

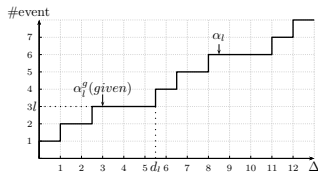


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Complex arrival curve of Type 2

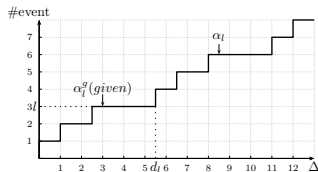


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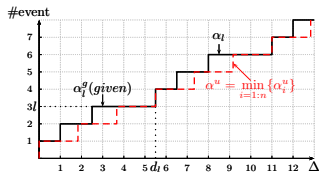
- 1 Dynamic counters: ?
- 2 l -repetitive function: /

Complex arrival curve of Type 2



For dynamic counters

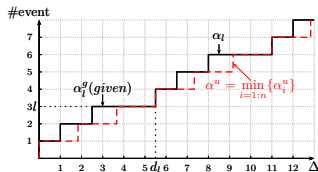
Complex arrival curve of Type 2



For dynamic counters

- 1 Assume a set of staircase functions $(\min_{i=1..n} \{\alpha_i\},$
 $\alpha_i = N_i^u + \lfloor \frac{\Delta}{\delta_i} \rfloor)$ is used to approximate α_l , where
 $\delta_{max} = \max_{i=1..n} \{\delta_i\}.$

Complex arrival curve of Type 2



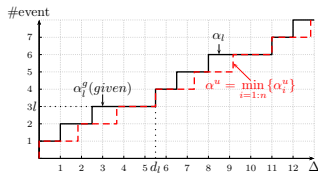
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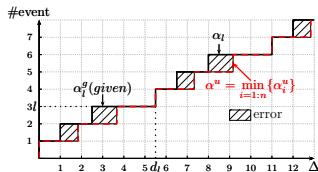
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 $d_l \leq l \cdot \delta_{max}.$

Complex arrival curve of Type 2



For dynamic counters

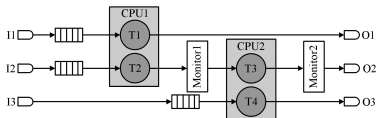
Complex arrival curve of Type 2



For dynamic counters

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$$EP(\Delta) = \frac{\int_0^\Delta (\alpha_l(t) - \alpha^a(t)) dt}{\int_0^\Delta \alpha_l(t) dt}.$$

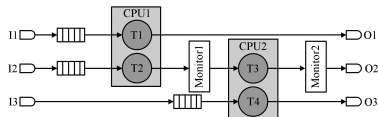
A case study



Specifications

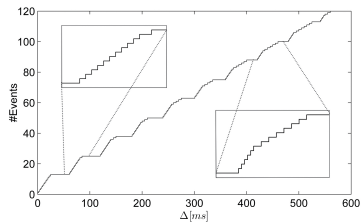
Input Events	I1: periodic ($P = 60ms$) I2: periodic ($P = 5ms$) I3: periodic ($P = [60..110]ms$)
Execution times	T1: $35ms$, T2: $2ms$, T3: $4ms$, T4: $12ms$
scheduling parameters	priority T1: high, priority T2: low priority T3: low, priority T4: high

A case study

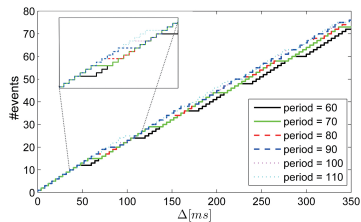


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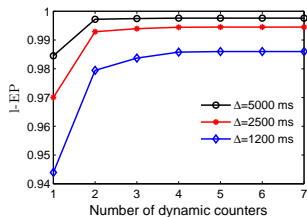


Arrival curve in Monitor 1

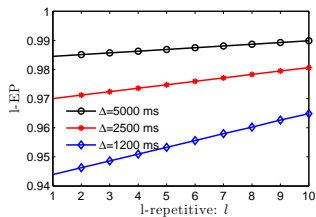


Arrival curve in Monitor 2

A case study

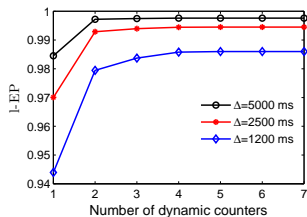


Result in monitor 1 by dynamic counters

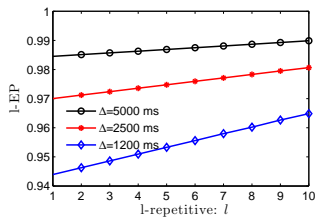


Result in monitor 1 by l -repetitive function

A case study



Result in monitor 1 by dynamic counters



Result in monitor 1 by l -repetitive function

The needed number of dynamic counters or l in repetitive segment with respect to the period of input I_3 .

period [ms]	60	70	80	90	100	110
#DC	13	16	18	21	23	25
l	12	15	17	20	22	24

Outline

- 1 Motivation
- 2 Background
- 3 Comparison
 - Comparison based on standard arrival curves
 - Comparison based on complex arrival curves
- 4 FPGA evaluations
- 5 Summary

Setup

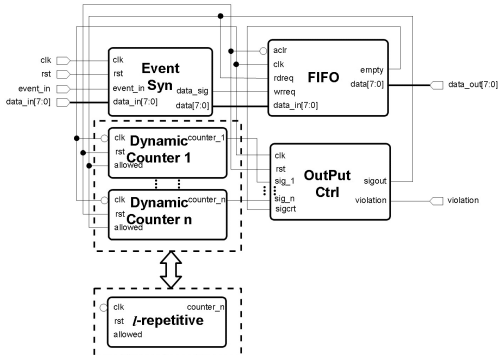
Prototype both approaches in ALTERA Cyclone III EP3C120F780

- Processor frequency: 50 MHz
- Timer bits: 16 bit

Setup

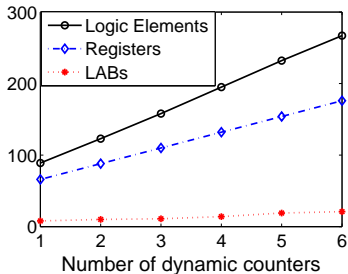
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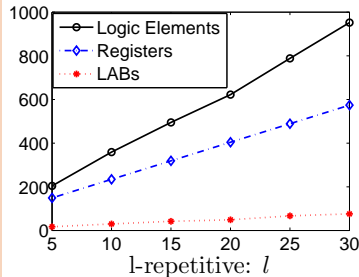


FPGA Resource

Resource usage with the number of dynamic counters or l in l -repetitive function



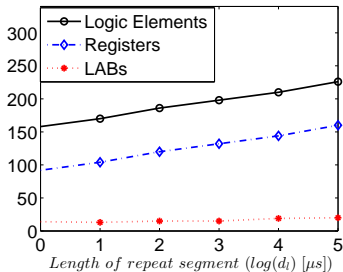
Dynamic counters



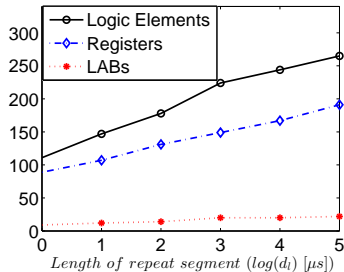
l -repetitive function

FPGA Resource

Resource usage with the length of repetitive segment



Dynamic counters



l -repetitive function

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- 1 Analyzed the difference of dynamic counters monitoring and I -repetitive function monitoring by using standard arrival curves, and two typical complex arrival curves.
- 2 Developed a new monitoring scheme for dynamic counters to monitor periodic burst events
- 3 Prototyped the two monitoring approaches in FPGA, and found resource overhead is more sensitive to the number of dynamic counters, and not sensitive to the length of one repetitive segment.