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# HyperFeel: An Efficient Federated Learning Framework Using Hyperdimensional Computing

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**Haomin Li (Speaker)**

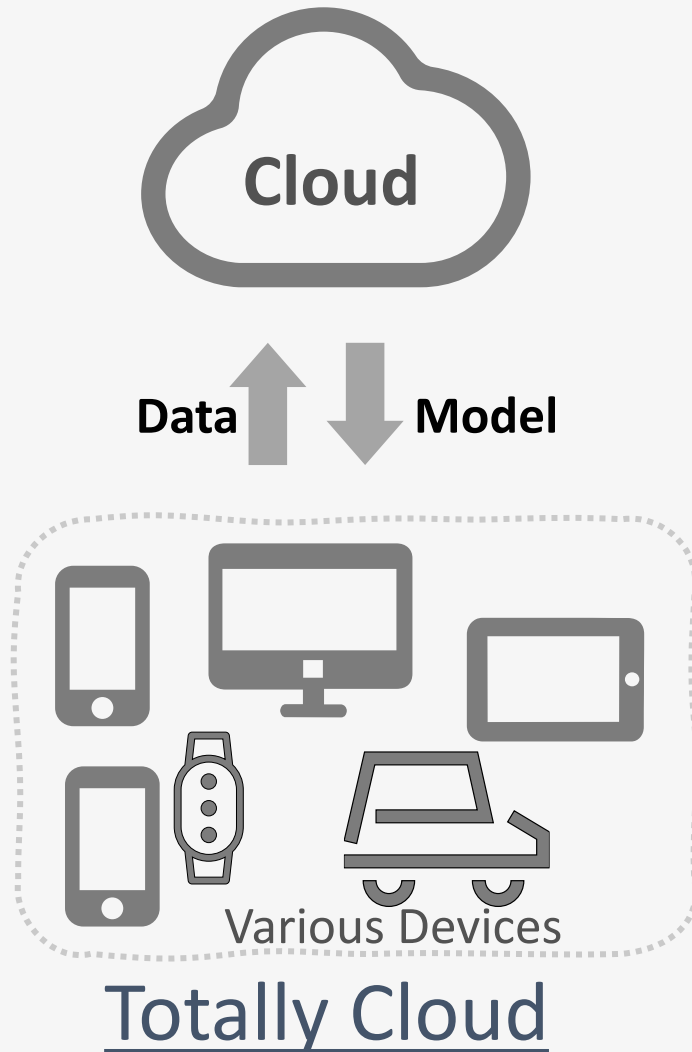
Fangxin Liu, Yichi Chen, and Li Jiang\*

**Shanghai Jiao Tong University**

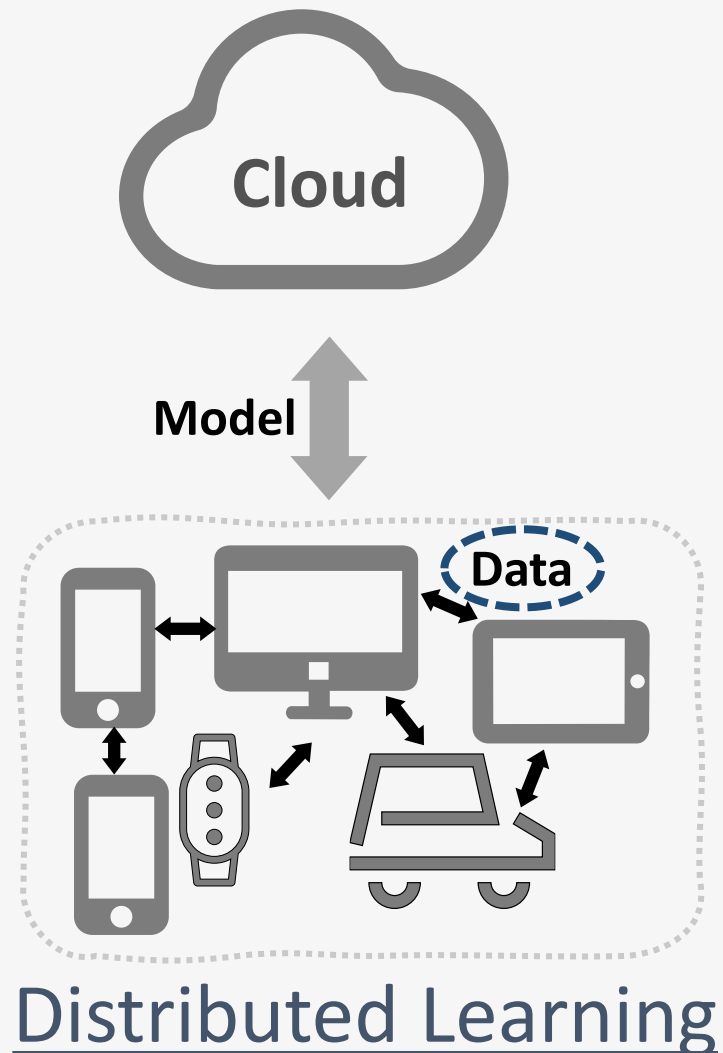
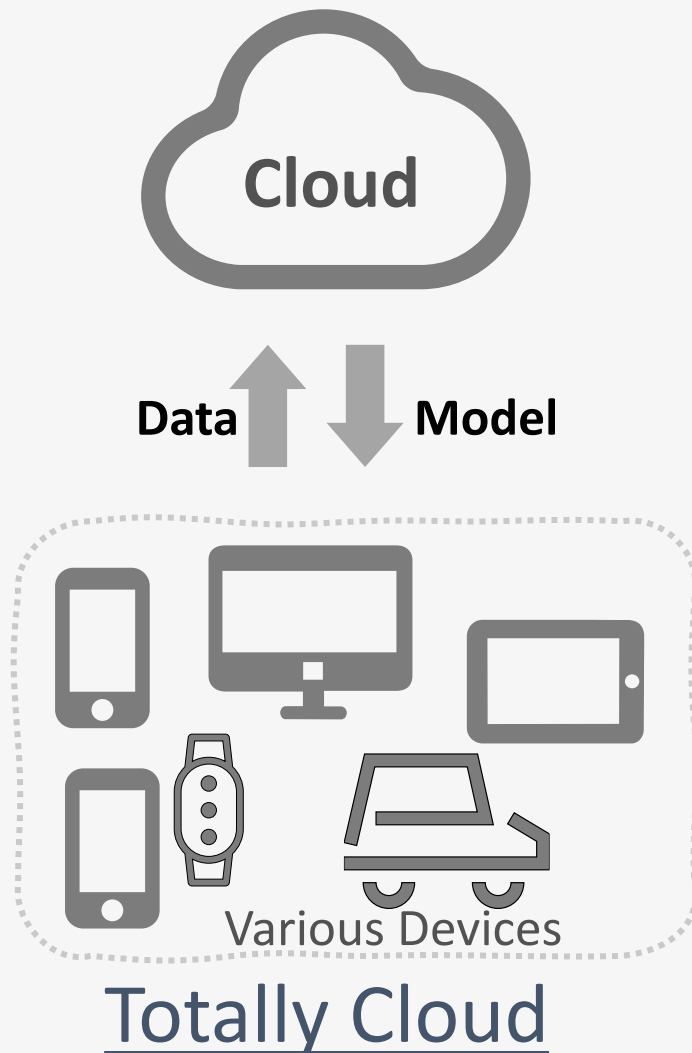
# Outline

- ④ Background and motivation
- ④ Proposal: Efficient Federated Learning Framework Using Hyperdimensional Computing
- ④ Design and implementation details
- ④ Experimental results
- ④ Conclusion

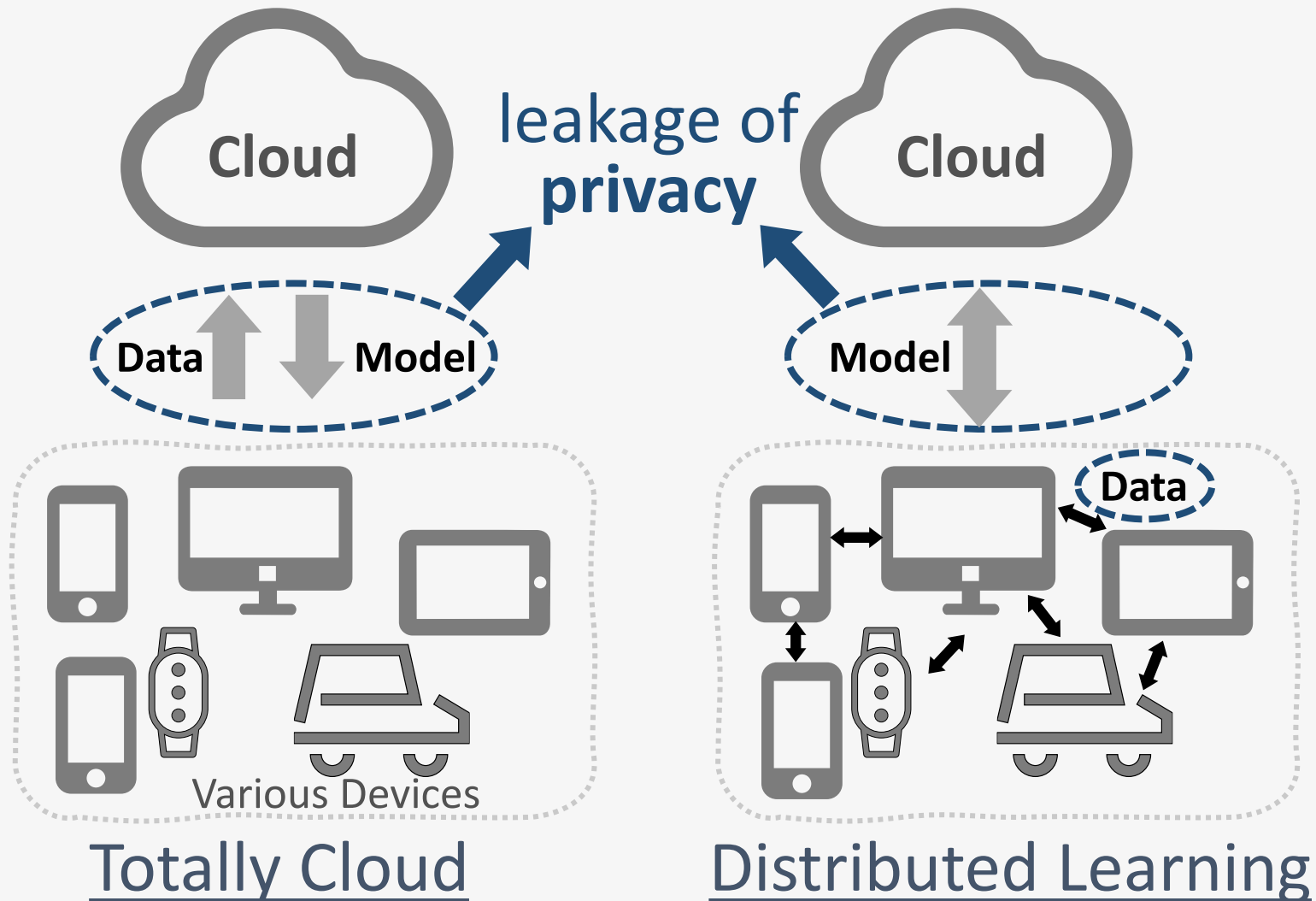
# Federated Learning for Privacy computing



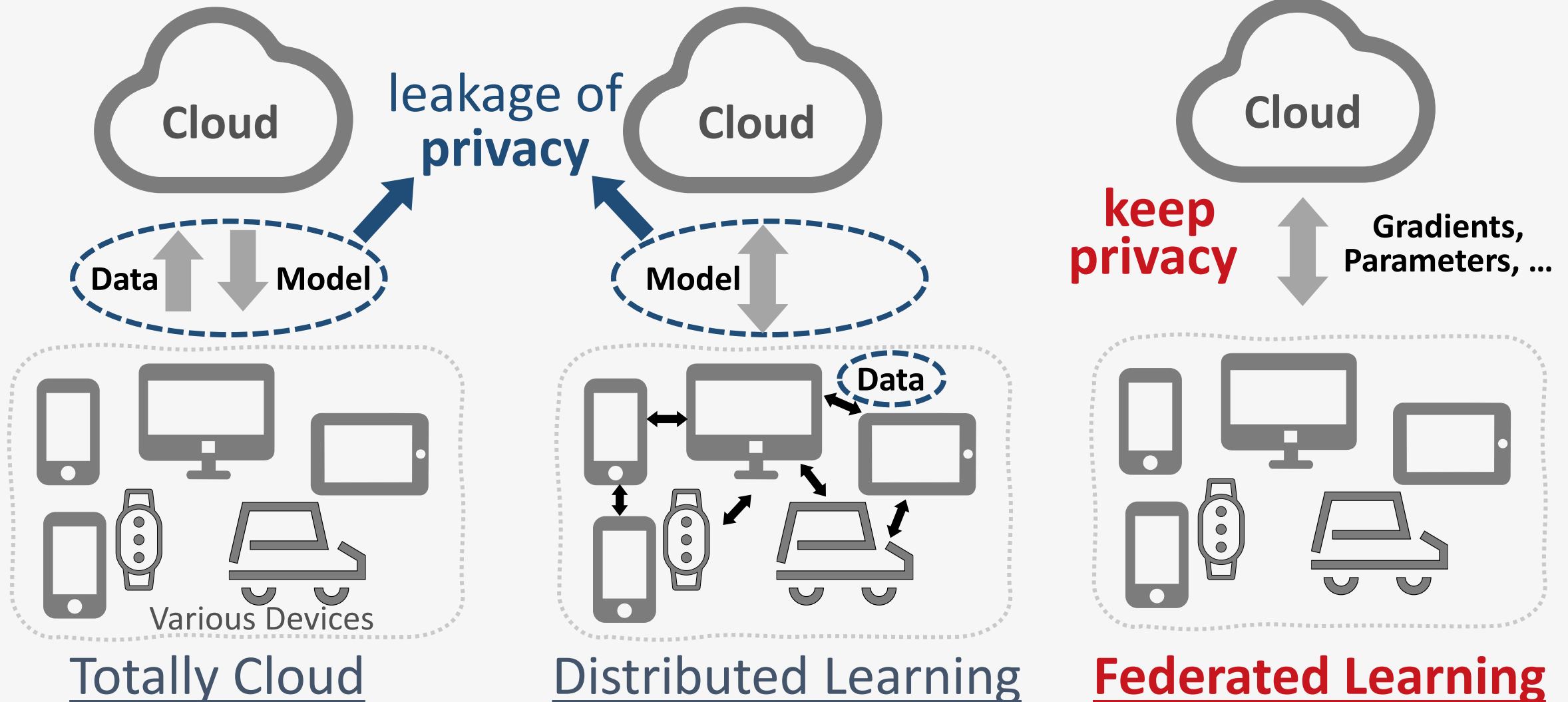
# Federated Learning for Privacy computing



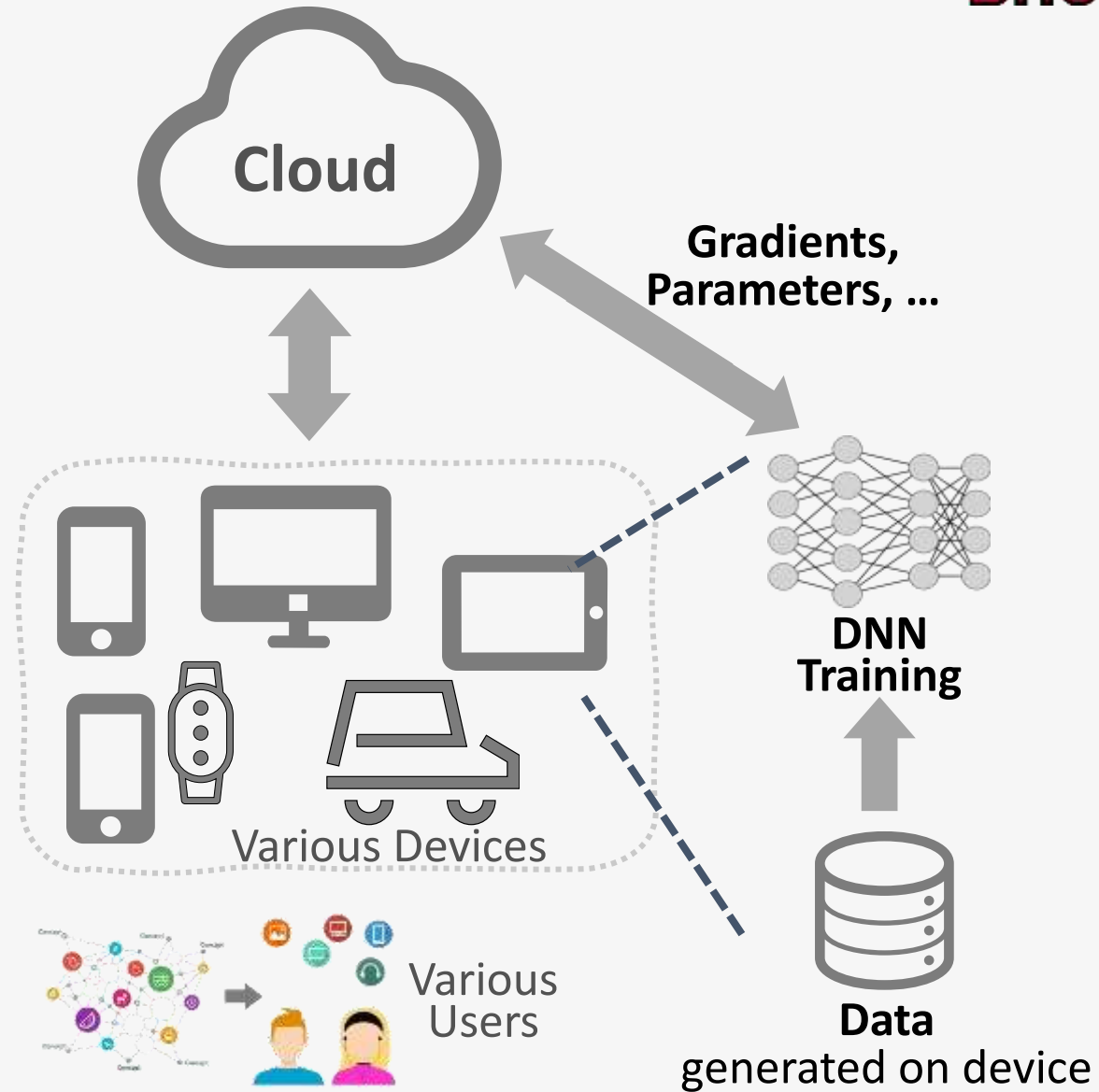
# Federated Learning for Privacy computing



# Federated Learning for Privacy computing

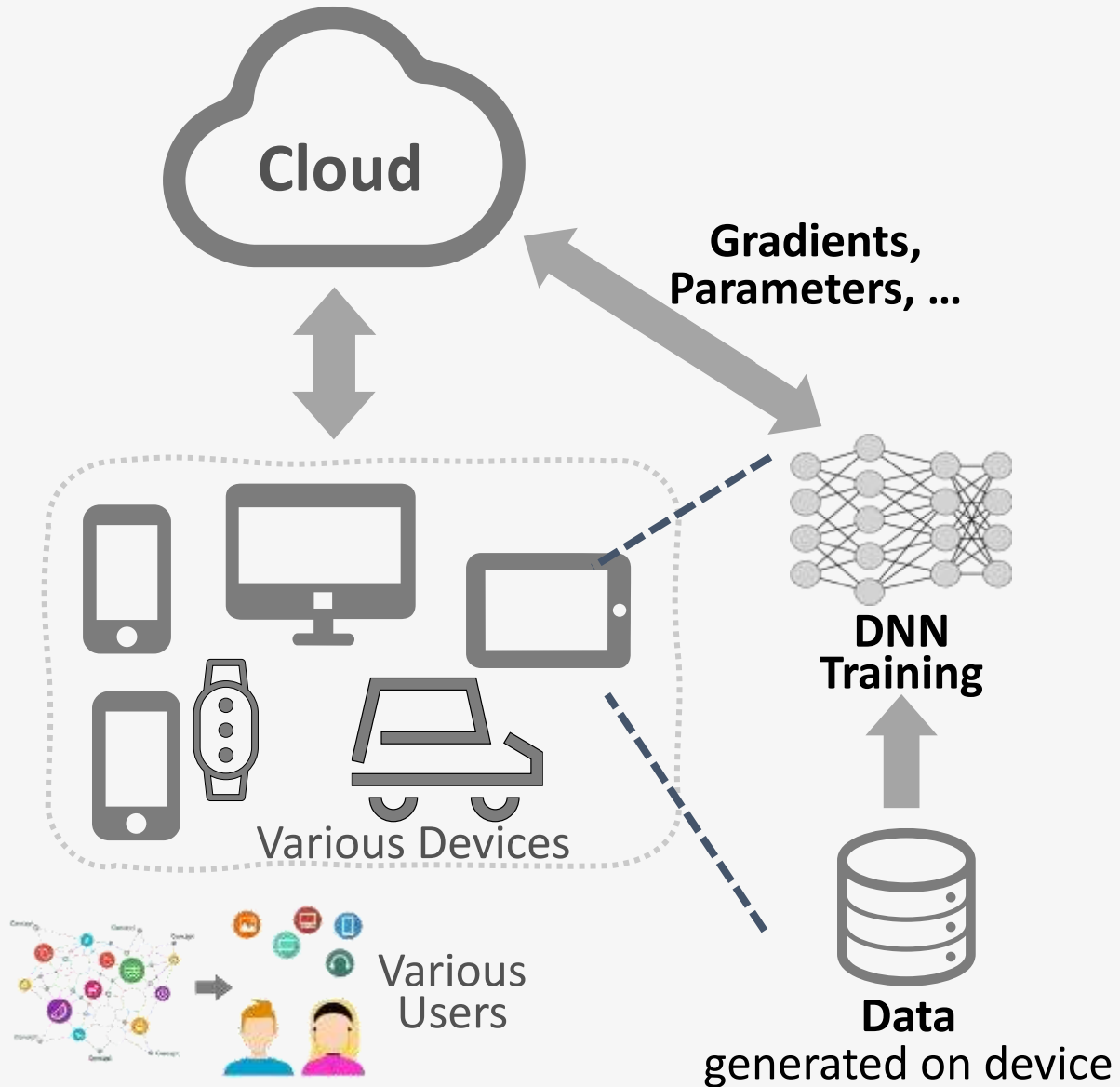


# Federated Learning



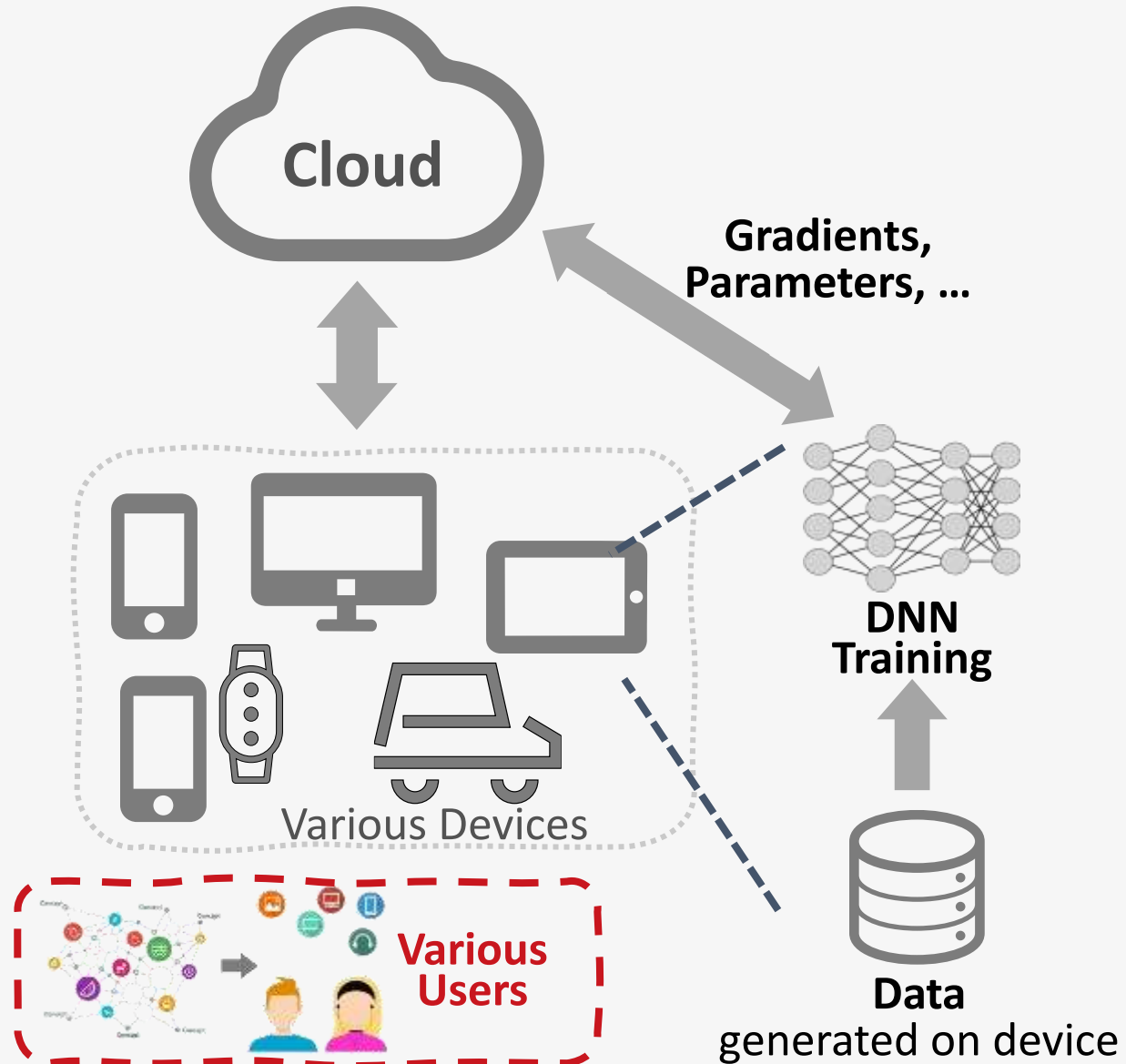
# Federated Learning

## FL Limitations





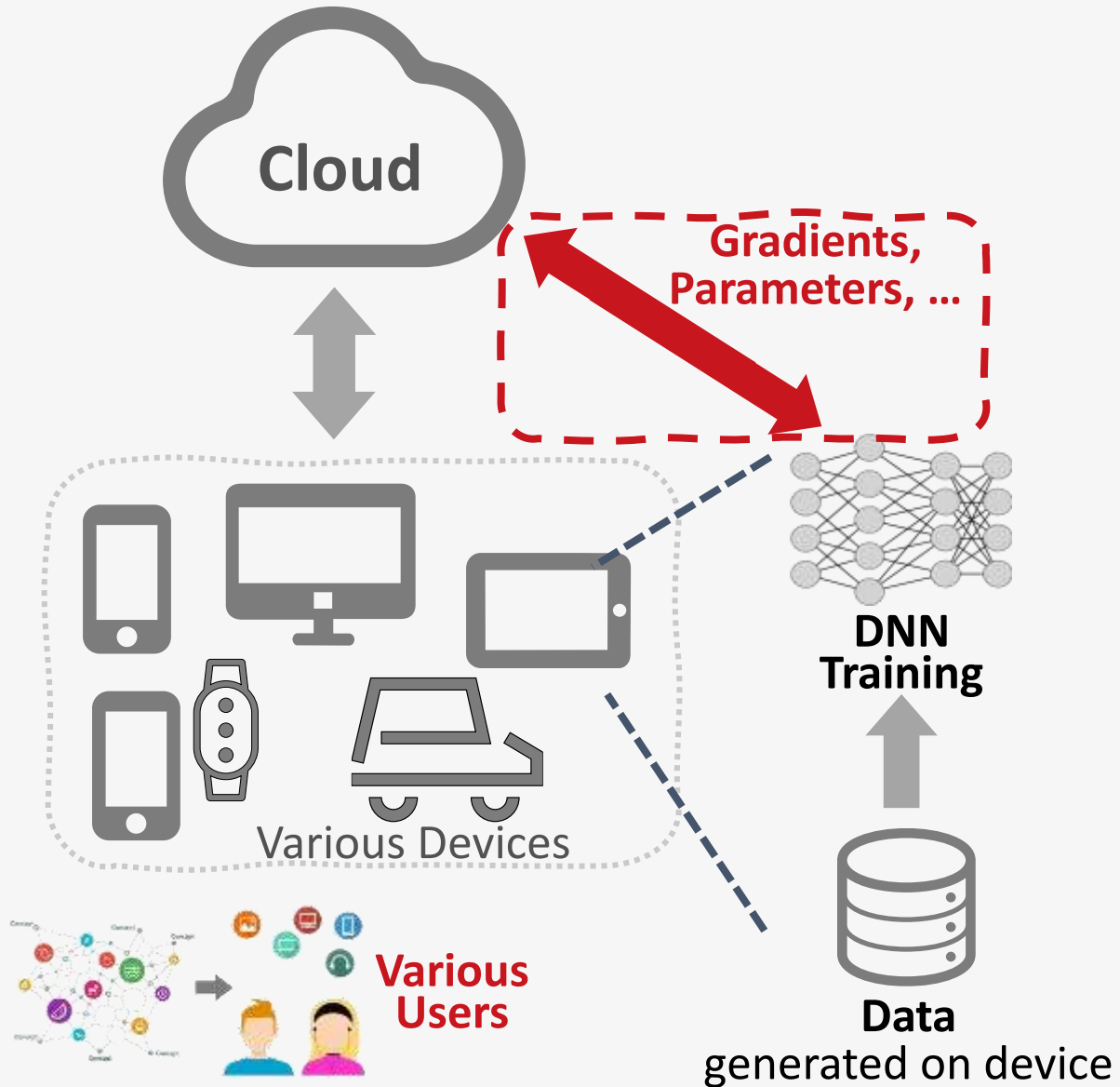
# Federated Learning



## FL Limitations

- **Non-IID Data**

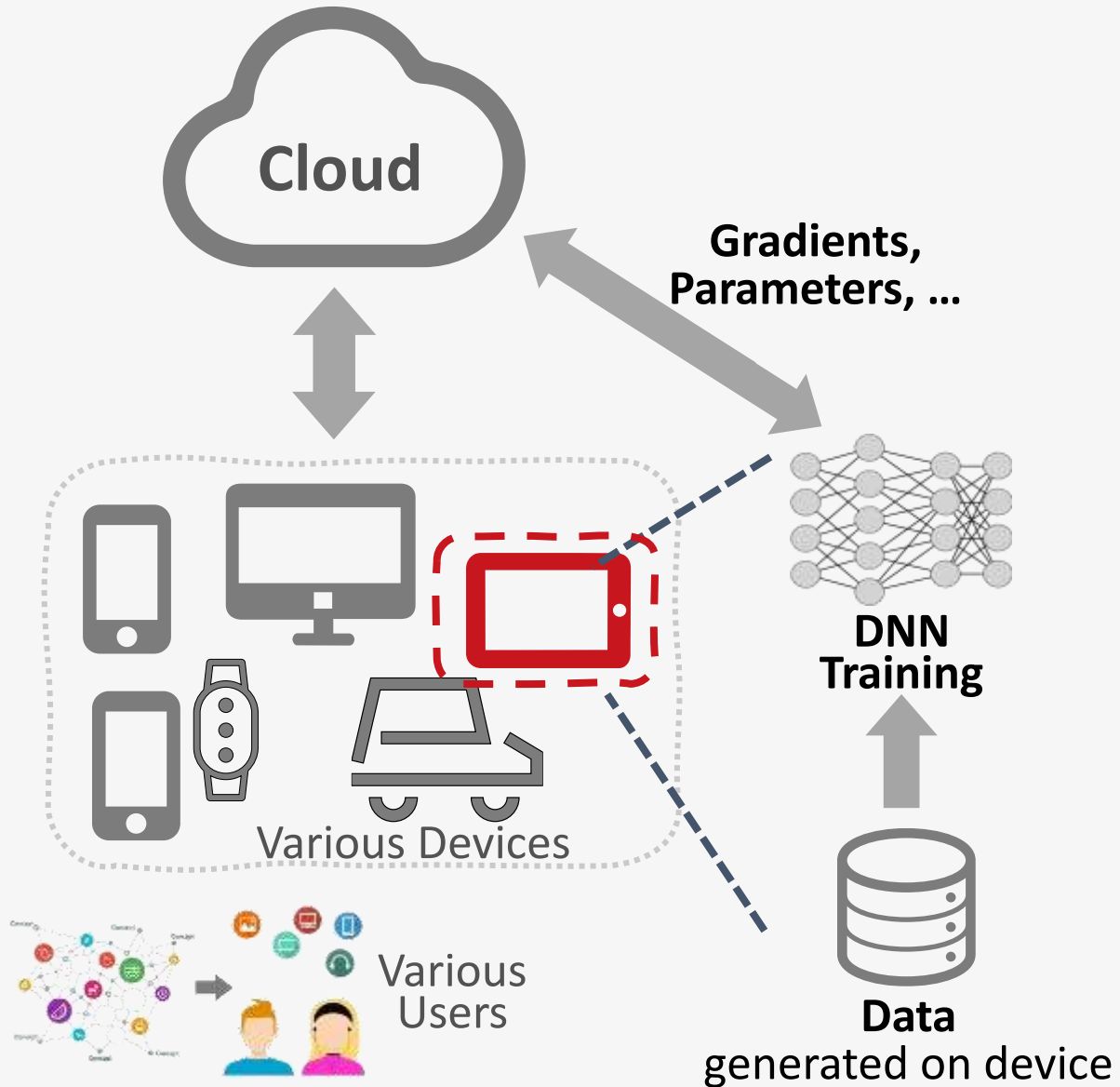
# Federated Learning



## FL Limitations

- Non-IID Data
- Massive Communication

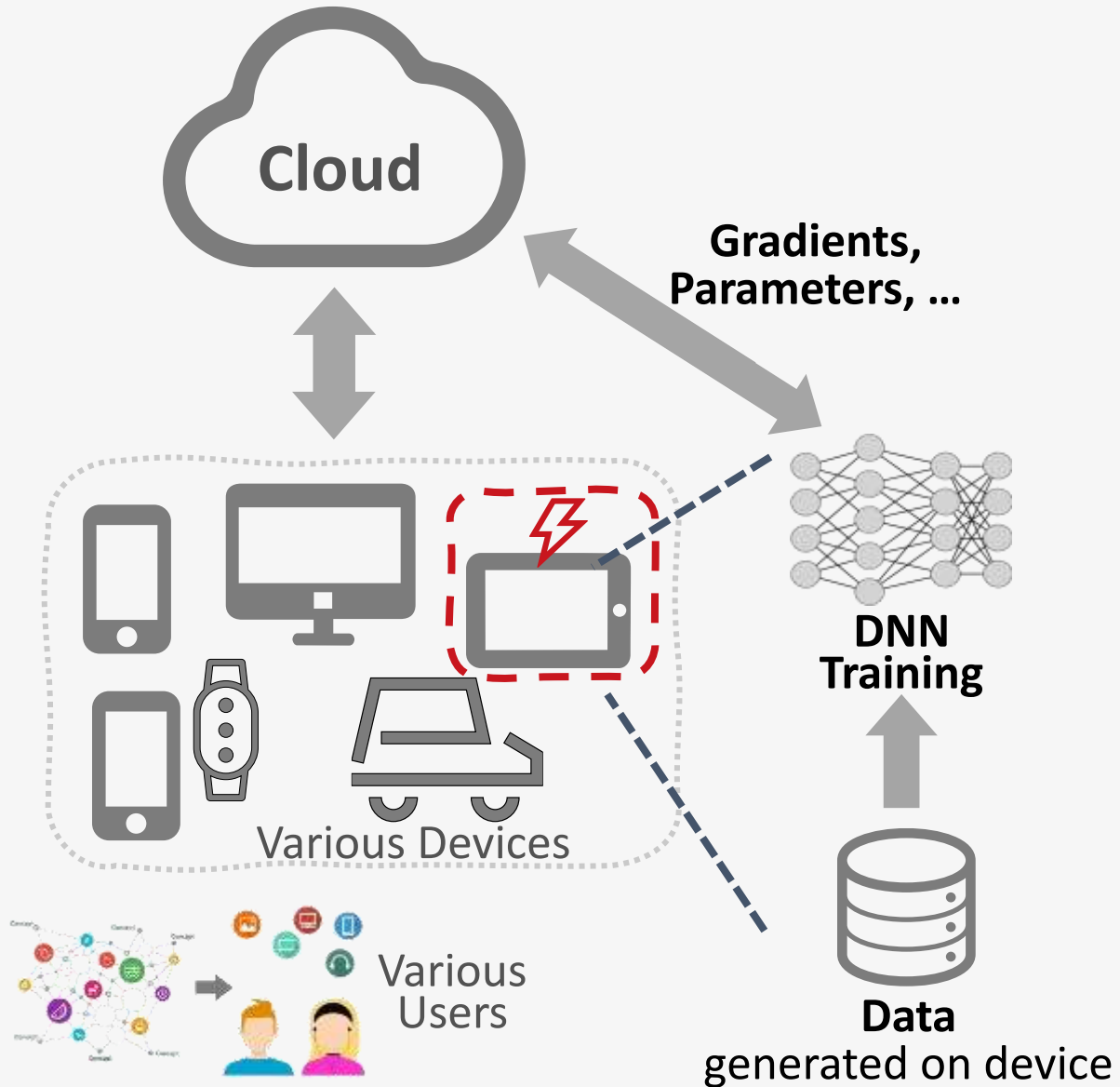
# Federated Learning



## FL Limitations

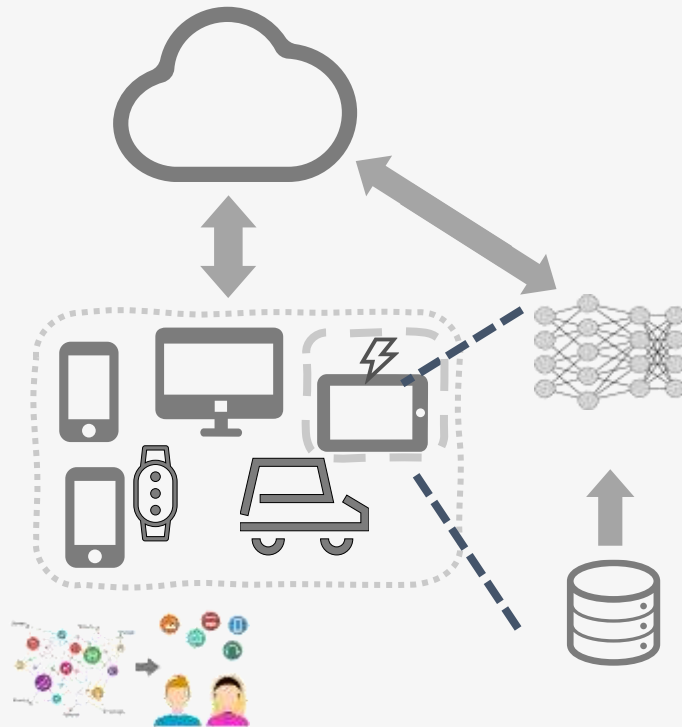
- Non-IID Data
- Massive Communication
- Limited Resource

# Federated Learning



## FL Limitations

- Non-IID Data
- Massive Communication
- Limited Resource
- Disturbance in edge scenes
- .....



## FL Limitations

- Non-IID Data
- Massive Communication
- Limited Resource
- Disturbance in edge scenes
- .....



## Hyper-Dimensional Computing

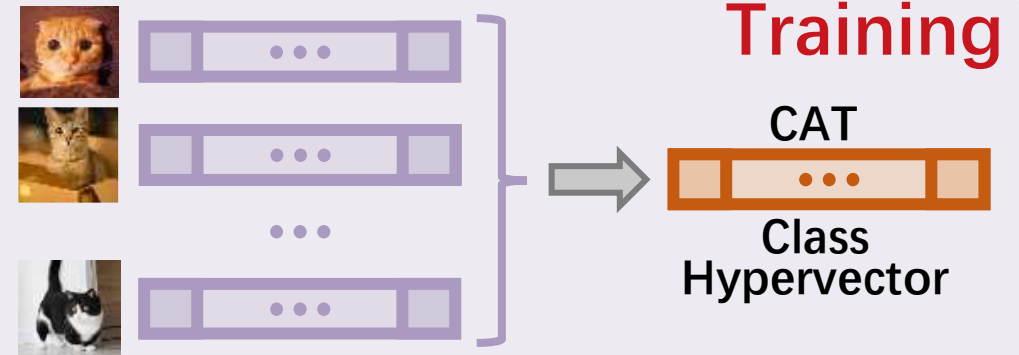
- Prototype
- Light-weight
- Efficient
- Robustness

# Hyper-Dimensional Computing(HDC)

## Hyper-Dimensional Space

### Pseudo-Orthogonal Property

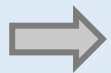
Bundle  $\oplus$  element-wise addition  
Bind  $\otimes$  element-wise multiplication  
Permutation  $\rho$  cyclic right-shift



## Encoding



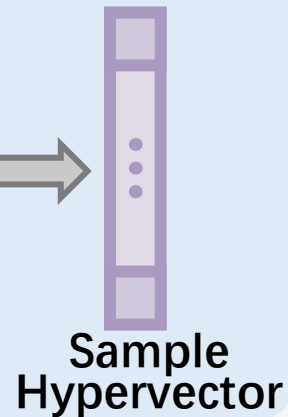
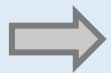
Original Data



Look up

Item Memory

Continuous  
Item Memory



Bird

Cat

Dog

Query

Class 1

Class 2

...

Class K

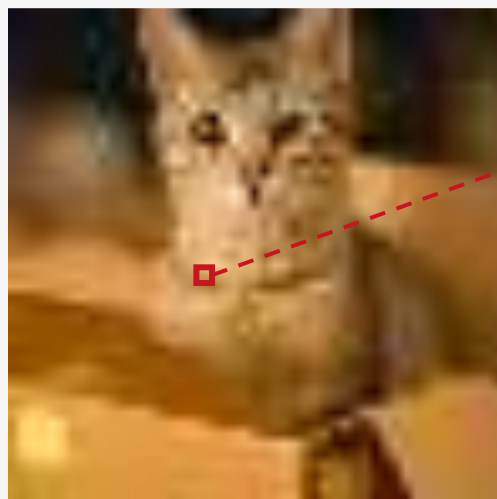
## Inference

Associative  
Search

Cat



# HDC: Encoding



Original Data

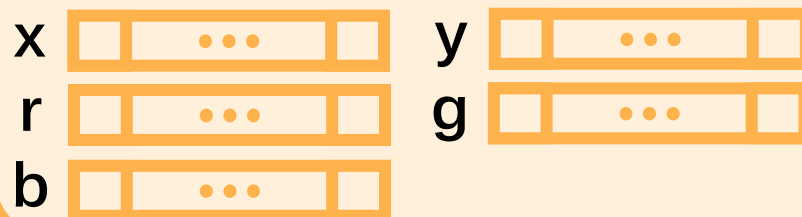
Pixel information

Attribute: (x,y), (r,g,b)

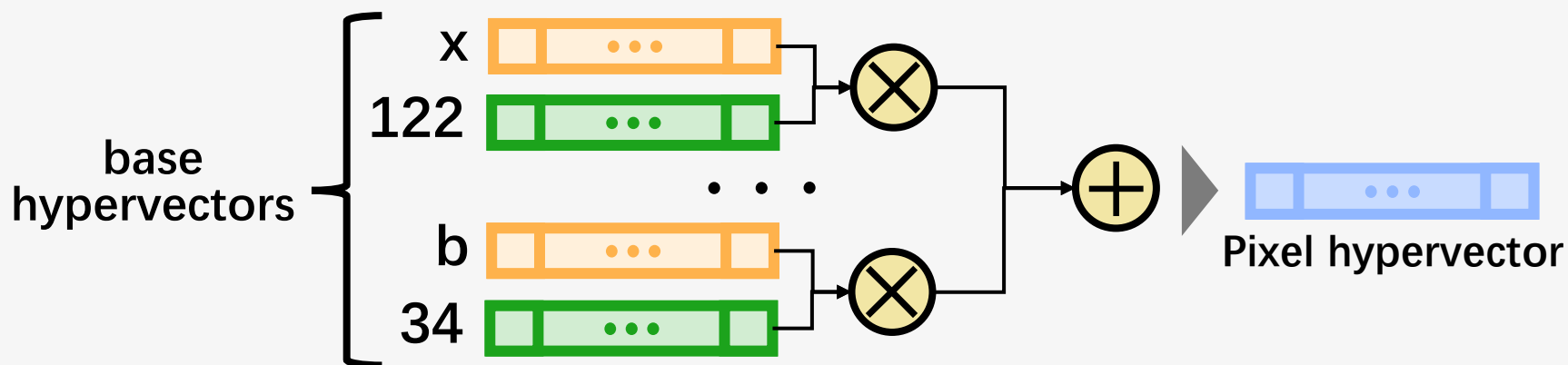
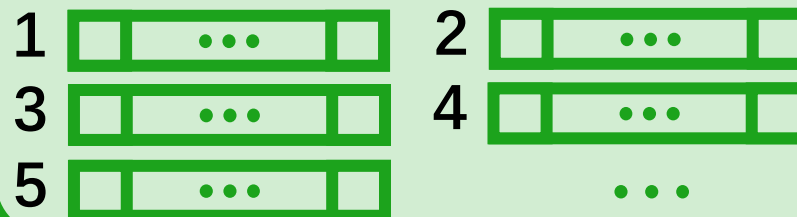
Value: (122,158), (0,12,34)

Look up

Item Memory



Continuous Item Memory





# HDC: Encoding



Original Data

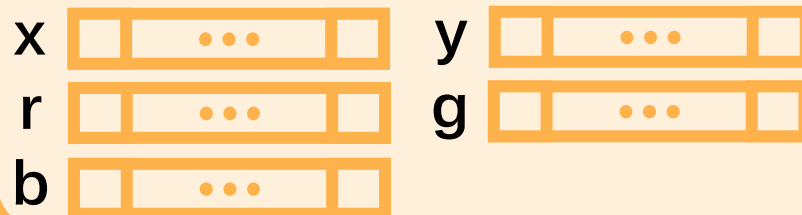
Pixel information

Attribute: (x,y), (r,g,b)

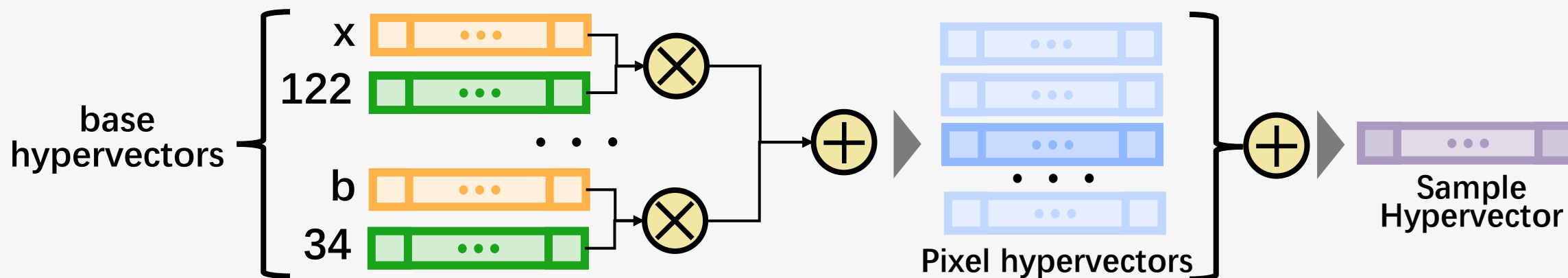
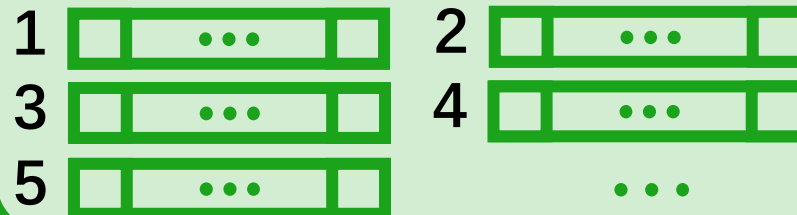
Value: (122,158), (0,12,34)

Look up

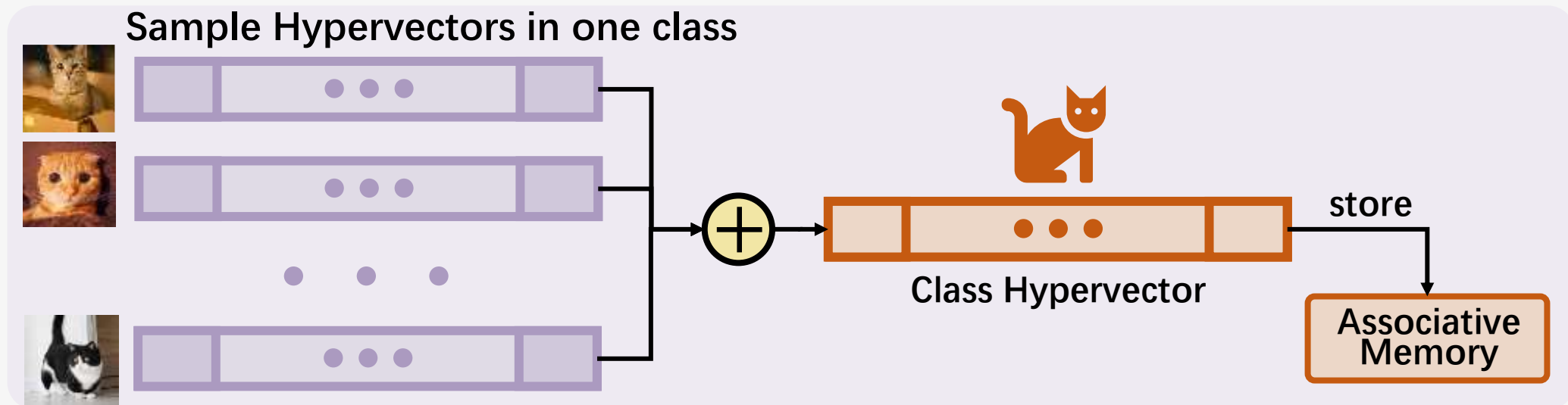
Item Memory



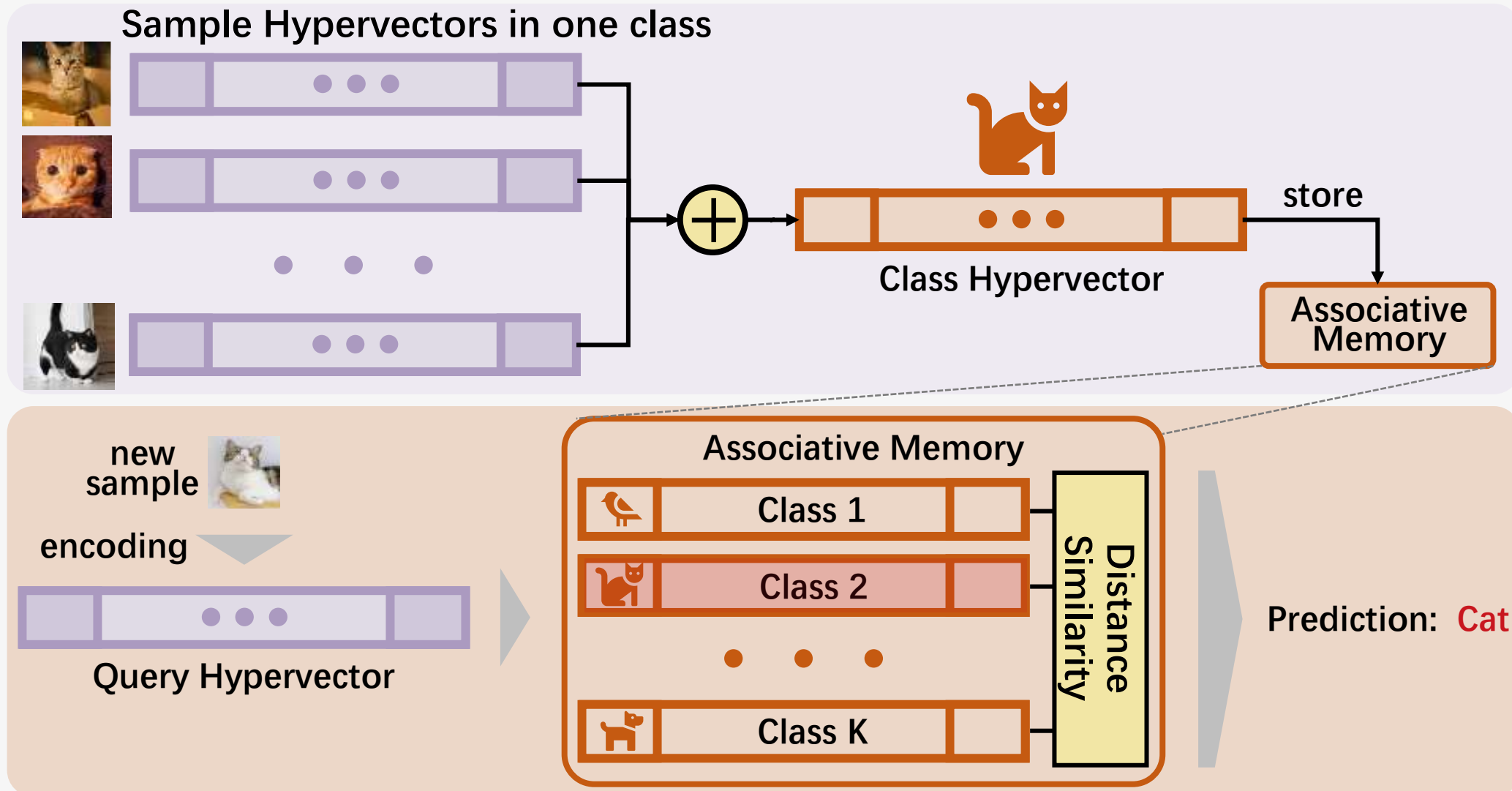
Continuous Item Memory



# HDC: Training & Inference



# HDC: Training & Inference



# Challenges

## Existing HDC works for FL



### FL-HDC<sup>[1]</sup>

- Binary model on device



### FHDnn<sup>[2]</sup>

- Apply NN as feature extractor



## Limitation Analysis



### FL-HDC

- Notable **accuracy loss**



### FHDnn

- Massive **computation overhead**

**An efficient and accurate HDC framework for FL is still missing**

[1] C.-Y. Hsieh *et al.*, "Fl-hdc: Hyperdimensional computing design for the application of federated learning," in AICAS, 2021.

[2] R. Chandrasekaran *et al.*, "FHDnn: communication efficient and robust federated learning for AIoT networks," in DAC, 2022.

# What to consider for designing the framework

① How to design **efficient** training mechanism?

- Low Communication
- Little Computation

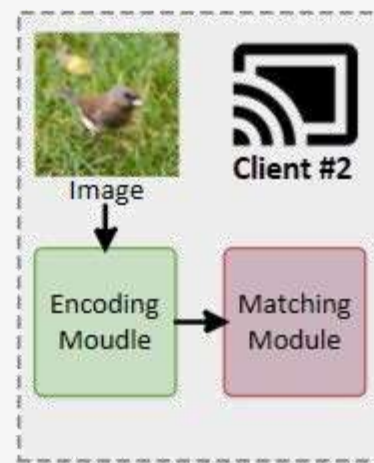
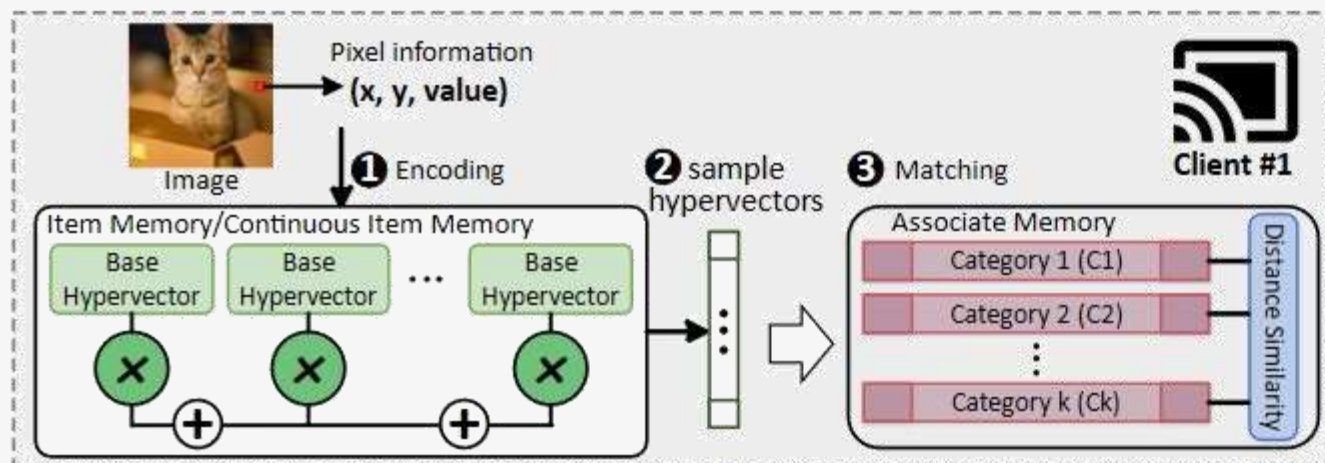
② How to get **accurate** models?

- Reduce influence from non-iid data

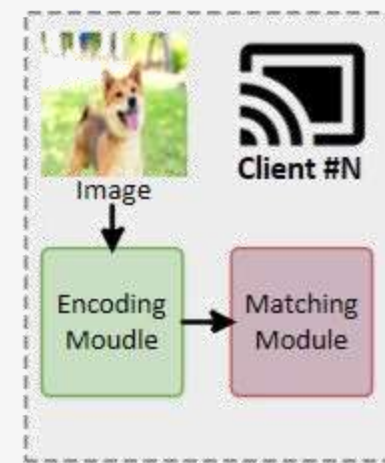
③ How to construct a **general** FL framework?

- Support horizontal FL
- Extend to Vertical FL

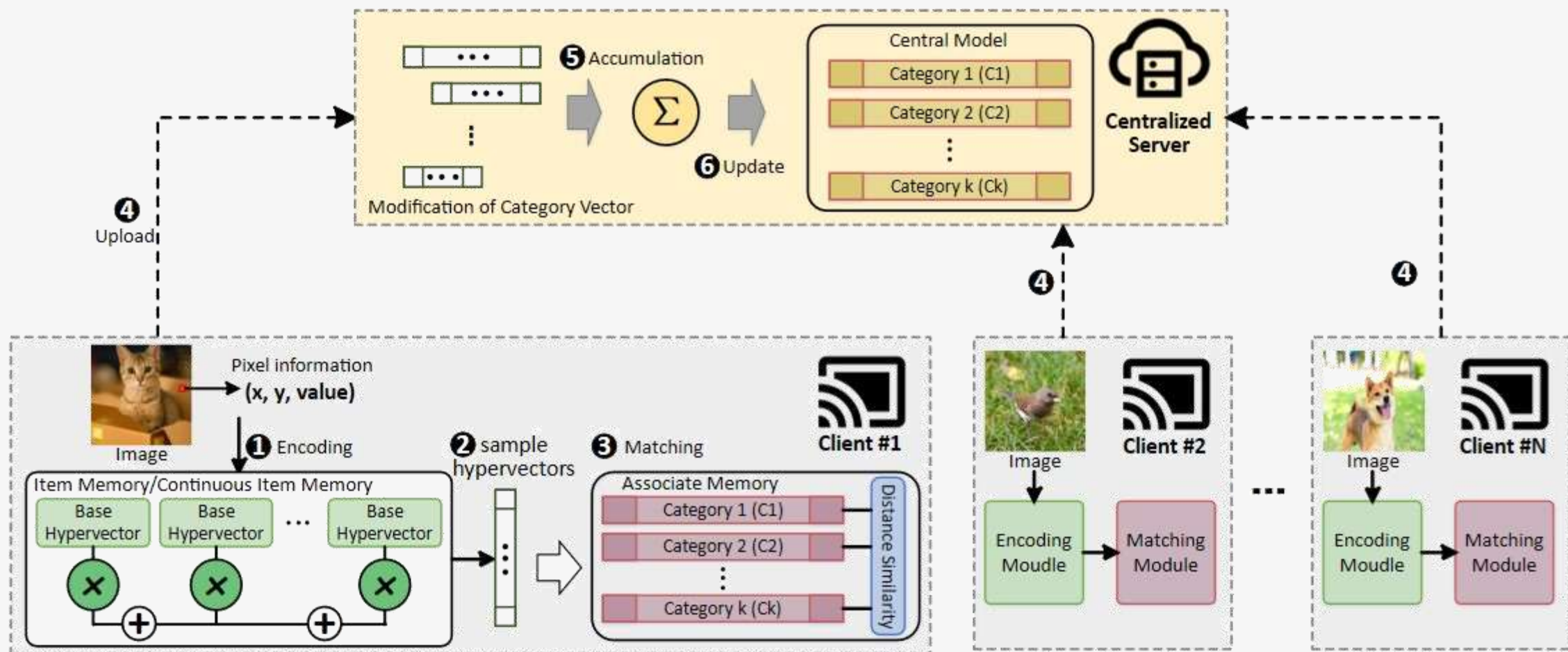
# Overview of HyperFeel



...

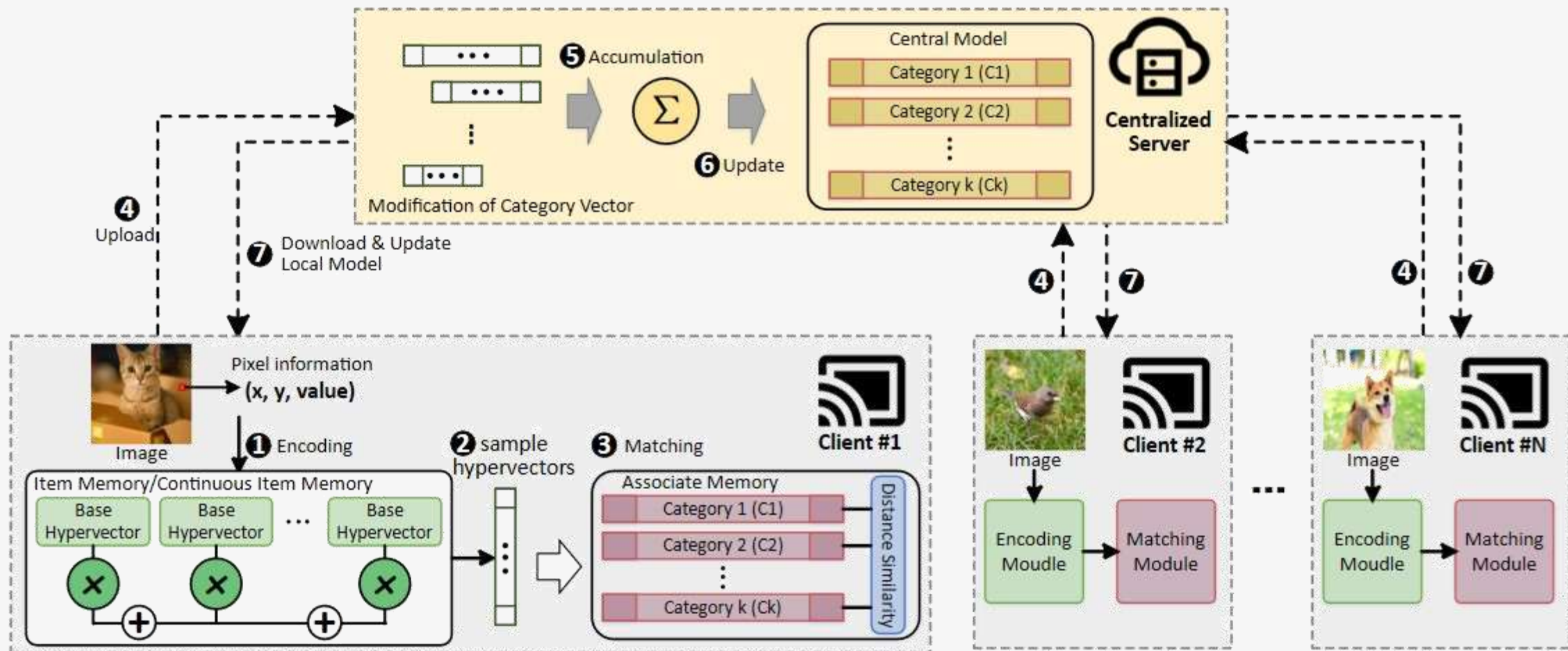


# Overview of HyperFeel






# Overview of HyperFeel





# HyperFeel Encoding

## Tabular Data Encoding

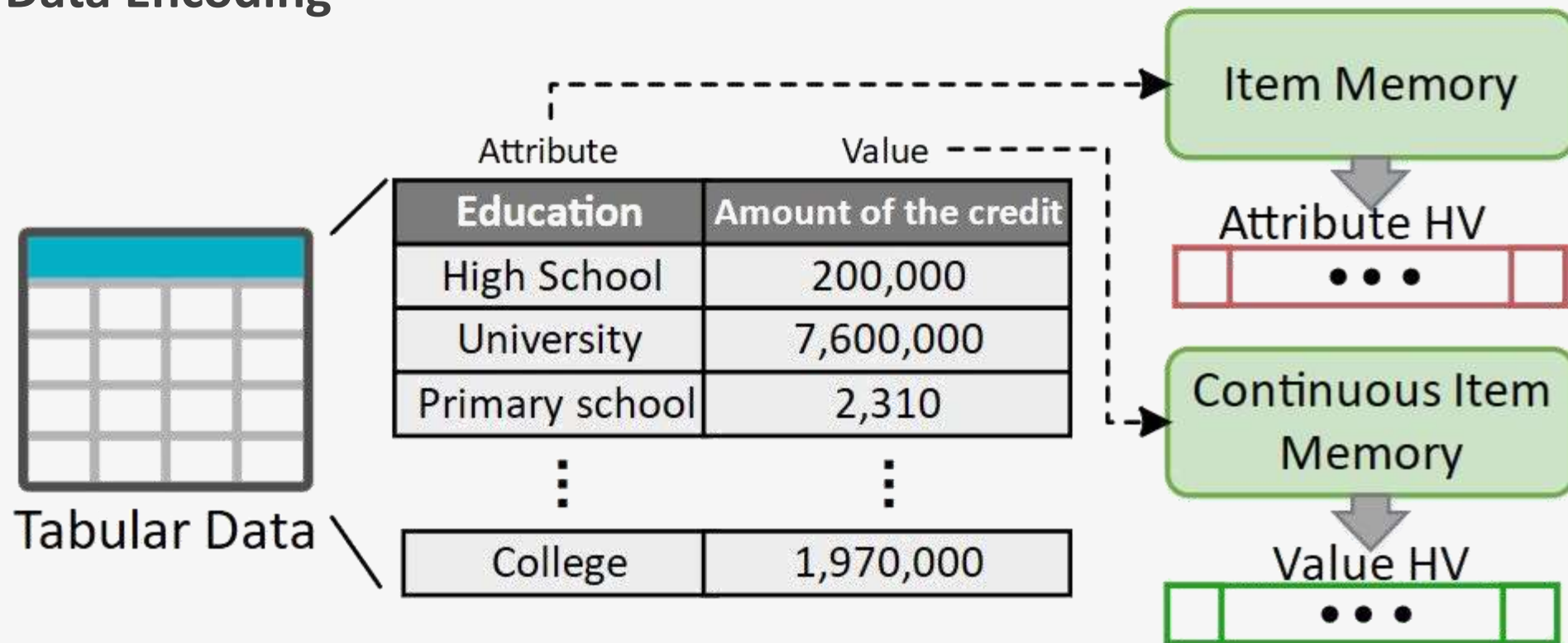


Tabular Data

Attribute	Value
Education	Amount of the credit
High School	200,000
University	7,600,000
Primary school	2,310
⋮	⋮
College	1,970,000

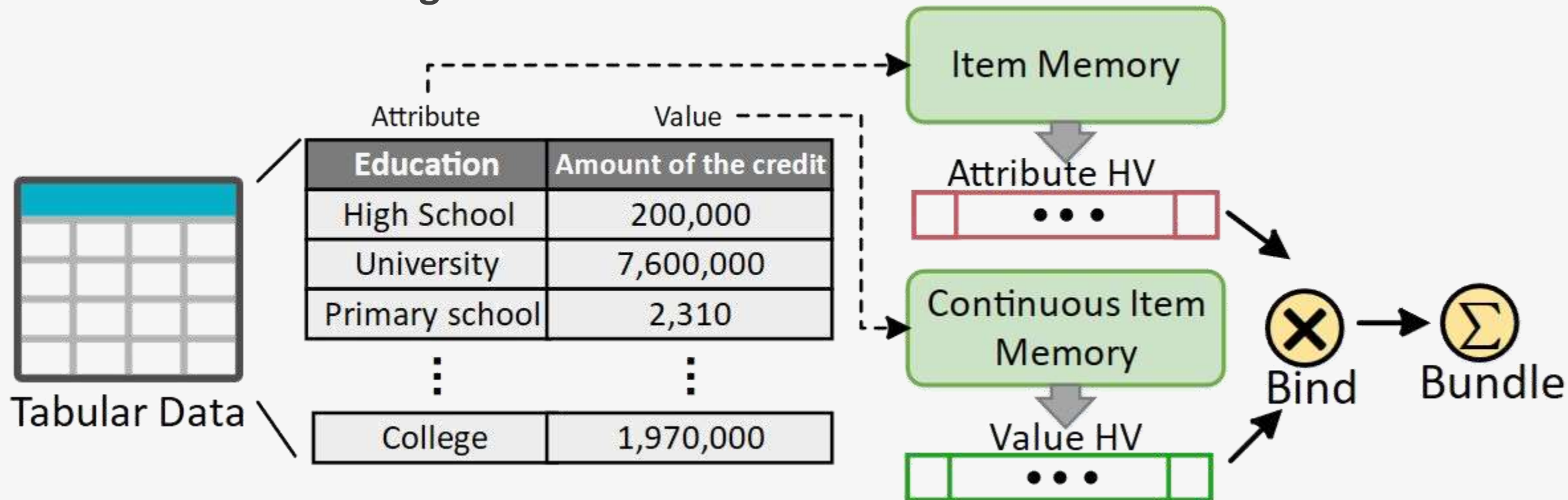
# HyperFeel Encoding

## Tabular Data Encoding



# HyperFeel Encoding

## Tabular Data Encoding



# HyperFeel Encoding

## Image Encoding

- $M$  pixels:  $\vec{F} = \{ \langle f_x^1, f_y^1, f_p^1 \rangle, \langle f_x^2, f_y^2, f_p^2 \rangle, \dots, \langle f_x^M, f_y^M, f_p^M \rangle \}$



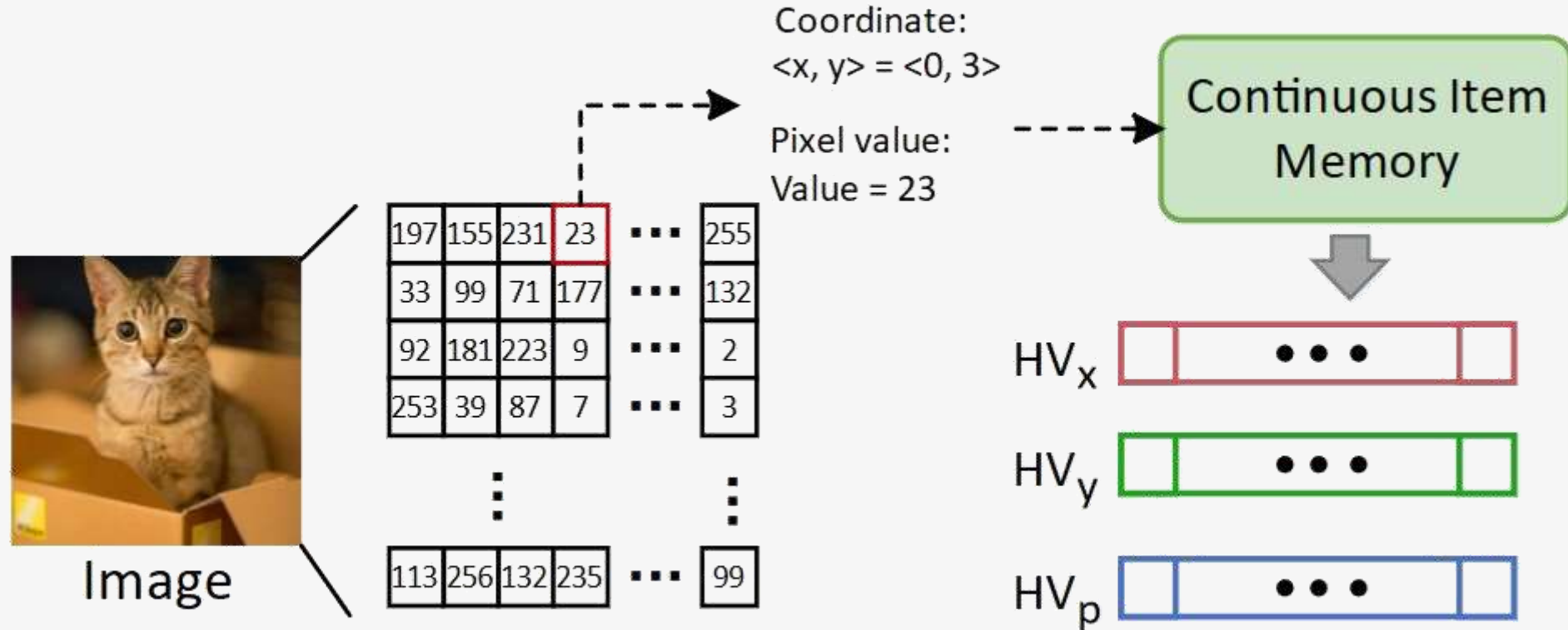
Image

197	155	231	23	...	255
33	99	71	177	...	132
92	181	223	9	...	2
253	39	87	7	...	3
⋮				⋮	
113	256	132	235	...	99

# HyperFeel Encoding

## Image Encoding

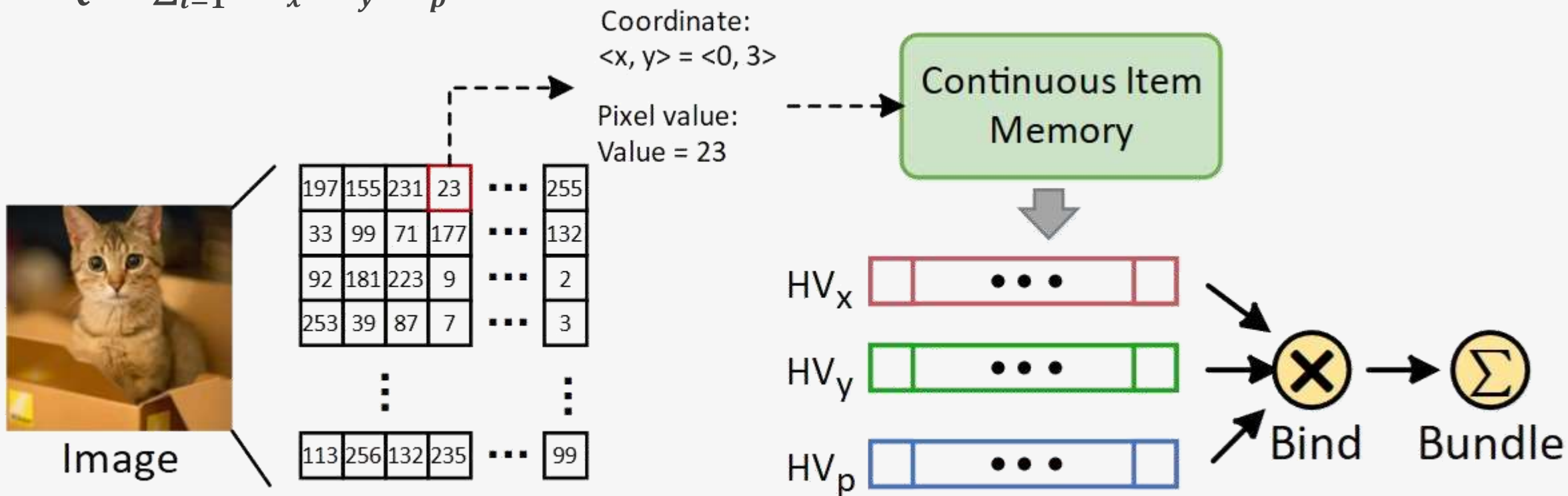
- $M$  pixels:  $\vec{F} = \{ \langle f_x^1, f_y^1, f_p^1 \rangle, \langle f_x^2, f_y^2, f_p^2 \rangle, \dots, \langle f_x^M, f_y^M, f_p^M \rangle \}$



# HyperFeel Encoding

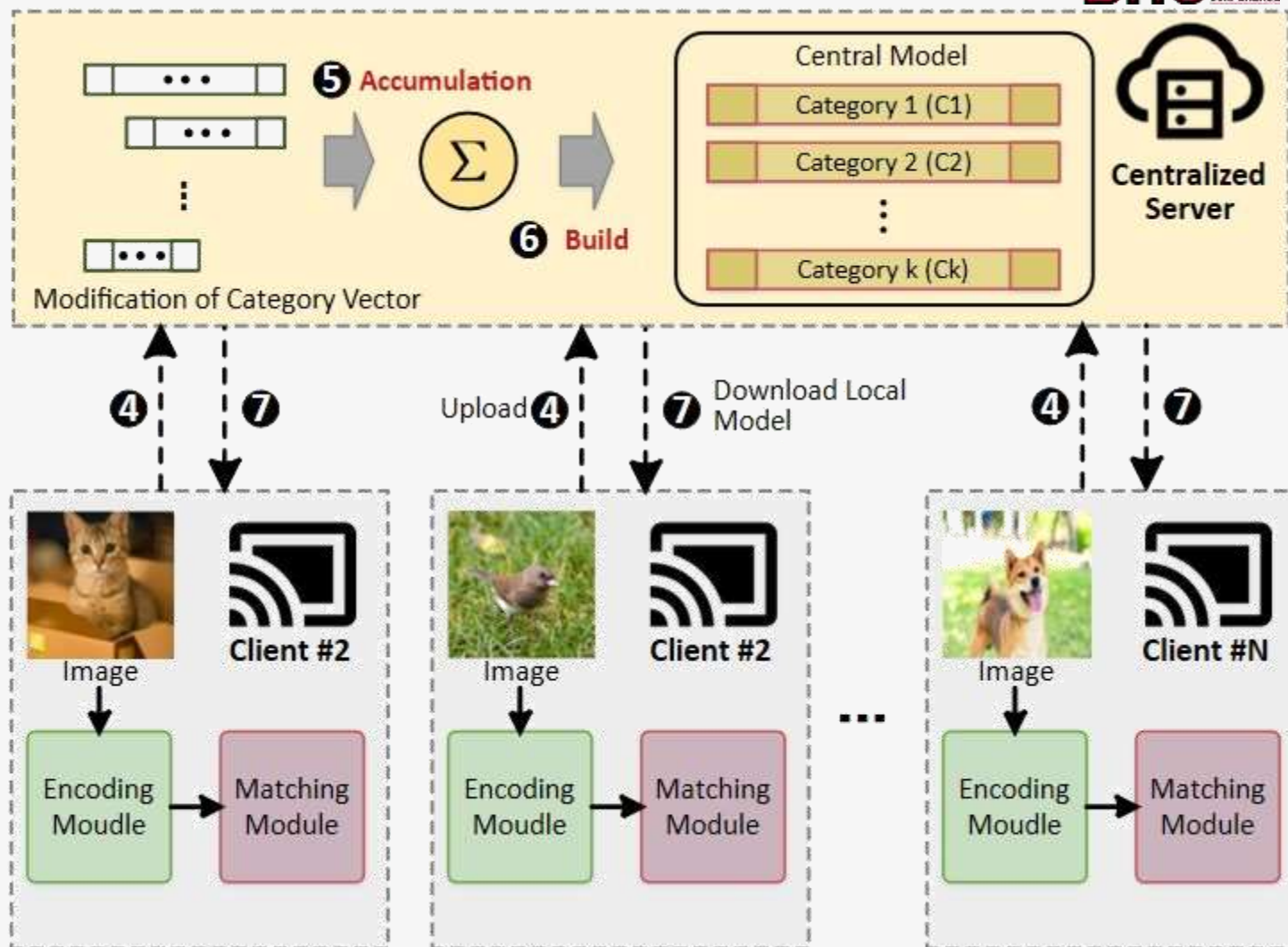
## Image Encoding

- $M$  pixels:  $\vec{F} = \{ \langle f_x^1, f_y^1, f_p^1 \rangle, \langle f_x^2, f_y^2, f_p^2 \rangle, \dots, \langle f_x^M, f_y^M, f_p^M \rangle \}$
- $Q = \sum_{i=1}^M HV_x^i HV_y^i HV_p^i$





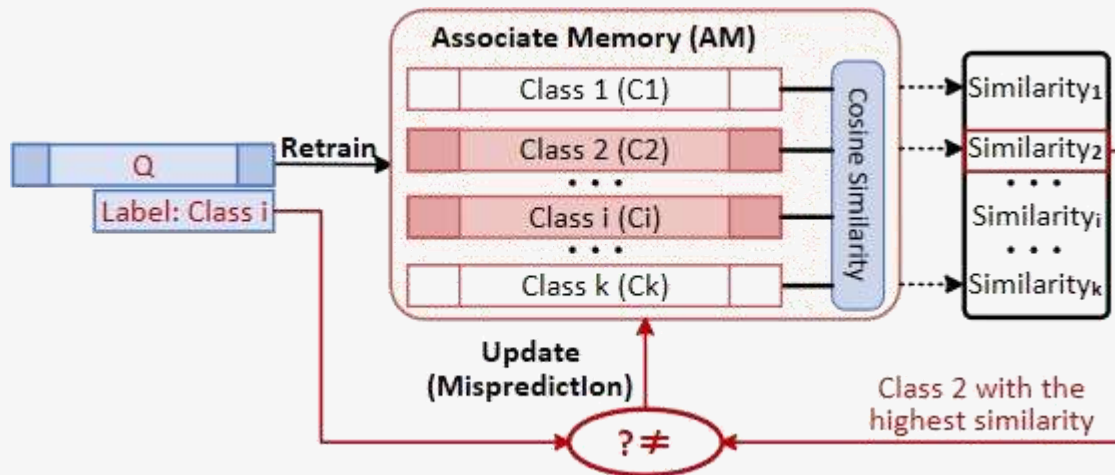
# Training



# Retraining

## In Client $i$

- For encoded local data  $Q$ 
  - Update local AM
    - $C_{ix} = C_{ix} + lr \cdot Q$ ;  $C_{iy} = C_{iy} - lr \cdot Q$
  - Accumulate modified class vector
    - $\delta_{ix} = \delta_{ix} + lr \cdot Q$ ;  $\delta_{iy} = \delta_{iy} - lr \cdot Q$
- Upload  $\delta_i$



### Algorithm 1: Retraining Strategy

**Data:** number of retrain rounds  $R$ , number of clients  $n$ , number of classes  $k$

**Result:** models  $C_1, \dots, C_n$

```

1 for  $r \leftarrow 1$  to  $R$  do
2   for  $i \leftarrow 1$  to  $n$  in parallel do
3     Clienti does:
4      $\Delta \leftarrow \text{download}_{\text{Server} \rightarrow \text{Client}_i}(\Delta)$ ;
5     for  $j \leftarrow 1$  to  $k$  do
6        $C_{ij} \leftarrow \text{Personalization Update}(C_{ij}, \Delta_j)$ ;
7     end
8     for sample, labelreal  $\in$  local data do
9        $Q \leftarrow \text{encode}(\text{sample})$ ;
10      labelpredict  $\leftarrow \text{Associative Search}(Q, C_i)$ ;
11      if labelpredict  $\neq$  labelreal then
12         $C_i \leftarrow \text{Accumulation}(C_i, Q, \text{label}_{\text{real}}, \text{label}_{\text{predict}})$ ;
13         $\delta_i \leftarrow \text{Accumulation}(\delta_i, Q, \text{label}_{\text{real}}, \text{label}_{\text{predict}})$ ;
14      end
15    end
16    uploadClienti  $\rightarrow$  Server( $\delta_i$ );
17  end
18  Server does:
19  gatherClienti  $\rightarrow$  Server( $\delta_i$ ),  $i = 1, 2, \dots, n$ ;
20  for  $j \leftarrow 1$  to  $k$  do
21     $\Delta_j \leftarrow \sum_{i=1}^N \delta_{ij}$ ;
22  end
23  broadcastServer  $\rightarrow$  Clienti( $\Delta$ ),  $i = 1, 2, \dots, n$ ;
24 end
  
```



# Retraining

## In Client $i$

- For encoded local data  $Q$ 
  - Update local AM
    - $C_{ix} = C_{ix} + lr \cdot Q$ ;  $C_{iy} = C_{iy} - lr \cdot Q$
  - Accumulate modified class vector
    - $\delta_{ix} = \delta_{ix} + lr \cdot Q$ ;  $\delta_{iy} = \delta_{iy} - lr \cdot Q$
- Upload  $\delta_i$

## In Server

- Gather  $\delta_i$  from clients
- Generate  $\Delta$ 
  - $\Delta_j = \sum_{i=1}^N \delta_{ij}$ ,  $j = 1, 2, \dots, k$
- Broadcast

### Algorithm 1: Retraining Strategy

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17  end
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21     $\Delta_j \leftarrow \sum_{i=1}^N \delta_{ij}$ ;
22  end
23   $\text{broadcast}_{\text{Server} \rightarrow \text{Client}_i}(\Delta)$ ,  $i = 1, 2, \dots, n$ ;
24 end
```

# Retraining

## In Client $i$

- Download  $\Delta$  from Server
- Personalization Update

- $C_{ij} = C_{ij} + \frac{error_{ij}}{cnt_{ij}} \cdot lr \cdot \Delta_j$
- $cnt_{ij}$ 
  - total number of samples of class  $j$  on client  $i$
- $error_{ij}$ 
  - number of samples with errors in one-round retraining

### Algorithm 1: Retraining Strategy

**Data:** number of retrain rounds  $R$ , number of clients  $n$ , number of classes  $k$   
**Result:** models  $C_1, \dots, C_n$

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```

# Extension to Vertical FL

## Vertical FL

- Different clients have different attribute sets

## Vertical FL assumption

- “the server is honest and does not collude with clients, but all the clients are honest but curious to each other”

# Extension to Vertical FL

## Vertical FL

- Different clients have different attribute sets

## Vertical FL assumption

- “the server is honest and does not collude with clients, but all the clients are honest but curious to each other”

## participating clients create **local** IMs

## All clients **share** a CIM for attribute value hypervectors

## Data alignment between clients

- employ Privacy Set Intersection (PSI) approach

# Overhead Analysis

## HyperFeel vs. FedAvg

- $N$ : #clients
- $M$ : #parameters (FedAvg)
- $C$ : fraction of clients performing computation in each round
- #dimensions  $D$ , #classes  $K$  (HyperFeel)


Method	Storage Cost	Comm. Cost(per round)
FedAvg	$N \times M$	$C \times N \times M$
HyperFeel	$D \times N \times K$	$D \times N \times K$

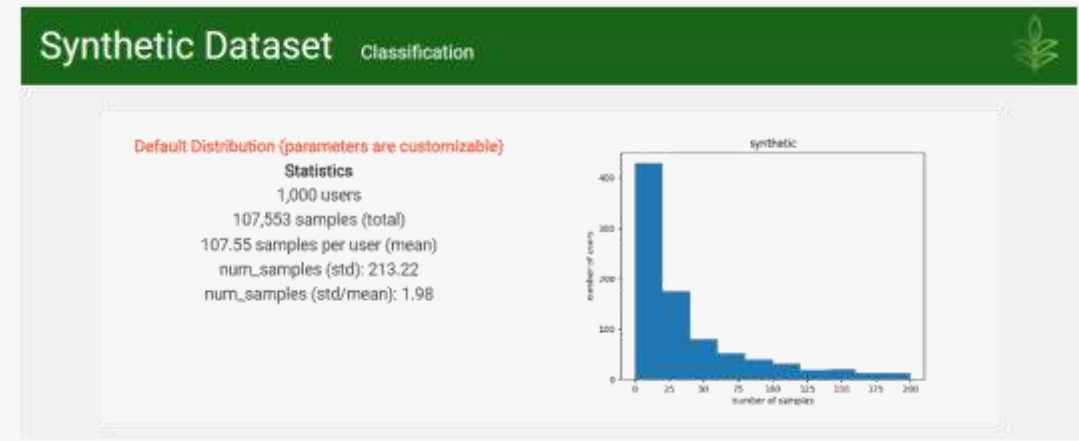
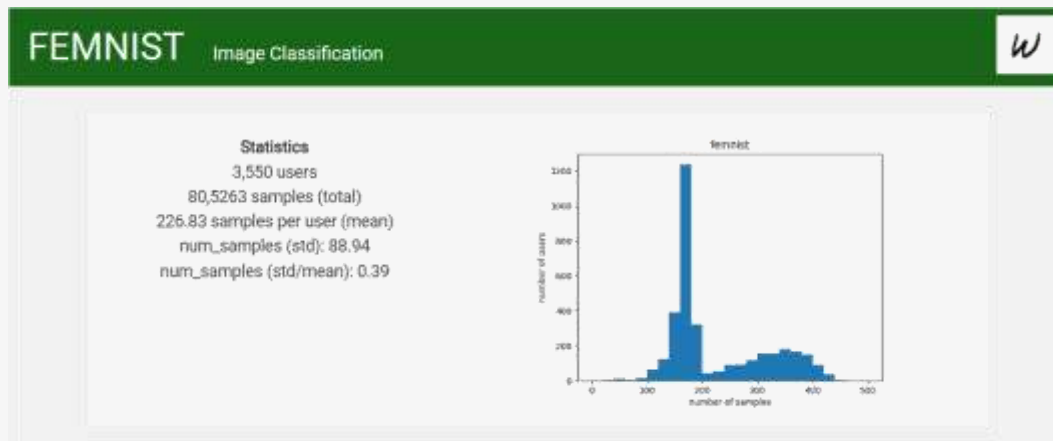
$$M \gg D \times K$$

$$C \times M \gg D \times K$$

# Experimental Setup

## Dataset

- Horizontal FL
  - FEMNIST & Synthetic
- Vertical FL
  - credit card customer default probability prediction
- Dataset Process & Partition
  - LEAF<sup>[1]</sup> 



[1] S. Caldas *et al.*, "Leaf: A benchmark for federated settings," arXiv, 2018.

## Dataset

- FEMNIST, Synthetic, credit card customer default probability prediction
- Process & Partition: LEAF

## Baselines

- Horizon FL
  - FedAvg, FedAvg with additional Pipeline, FL-HDC
- Vertical FL
  - KNN, LR, Parsimonious Bayesian, NN

## Configurations

- Dimension  $D = 1000$
- #Clients  $N = 30$

# Performance Comparison

Method	Storage Cost	Commun. Cost	Acc.
FEMNIST DataSet			
FedAvg [5]	6.35MB	5.58GB	74.72%
Additional pipeline [20]	-	-	80.24%
FL-HDC [15]	2.37MB	2.08GB	48.99%
<b>HyperFeel (ours)</b>	<b>249.63KB</b>	<b>70.95MB</b>	<b>68.54%</b>
Synthetic DataSet			
FedAvg [5]	1.19KB	1.17MB	71.89%
Additional pipeline [20]	-	-	87.34%
FL-HDC [15]	195.31KB	183.11MB	79.69%
<b>HyperFeel (ours)</b>	<b>27.47KB</b>	<b>6.10MB</b>	<b>90.13%</b>

**26× Storage Reduction**  
**80.5× Communication Reduction**



# Performance Comparison

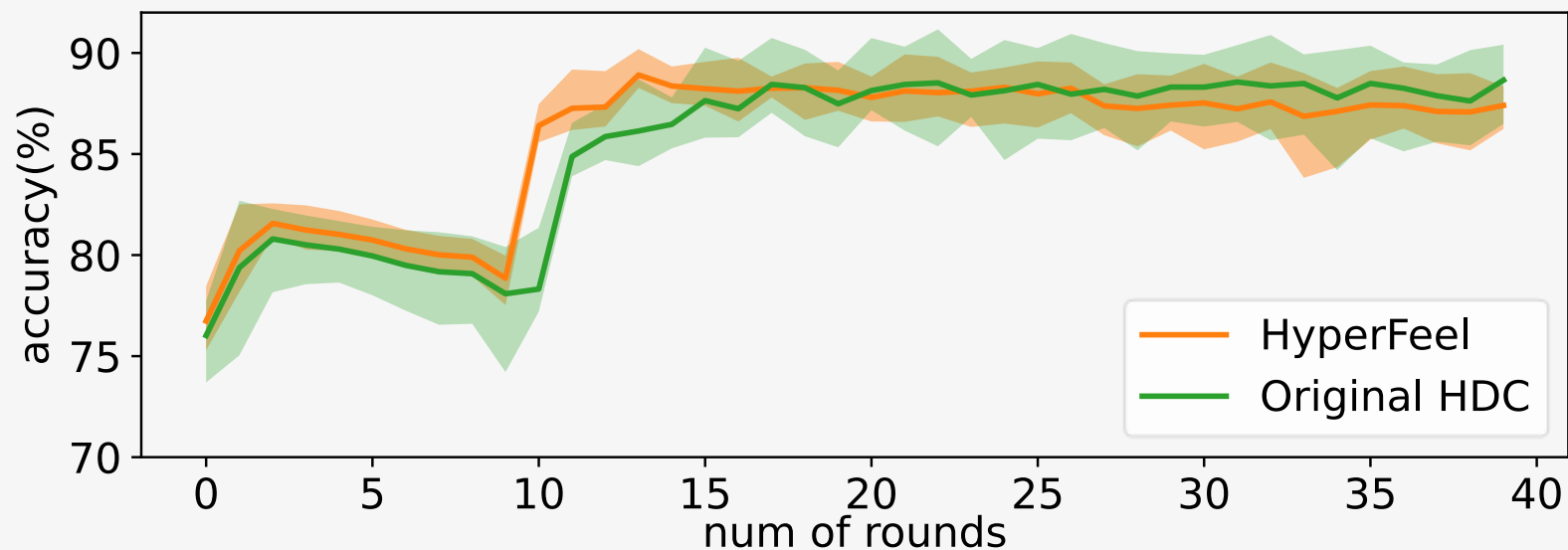
Method	Accuracy	Storage	Communication
KNN	84%	182,169KB	182,169KB
LR	82%	-	-
Bayesian	79%	813KB	813KB
Neural Network	83%	2,412KB	2,412KB
<b>HyperFeel (ours)</b>	<b>82%</b>	<b>430.91KB</b>	<b>39.06KB</b>

**A little accuracy loss**

**113× Storage Reduction**

**1257× Communication Reduction**

# Impact of Online Update & Robustness

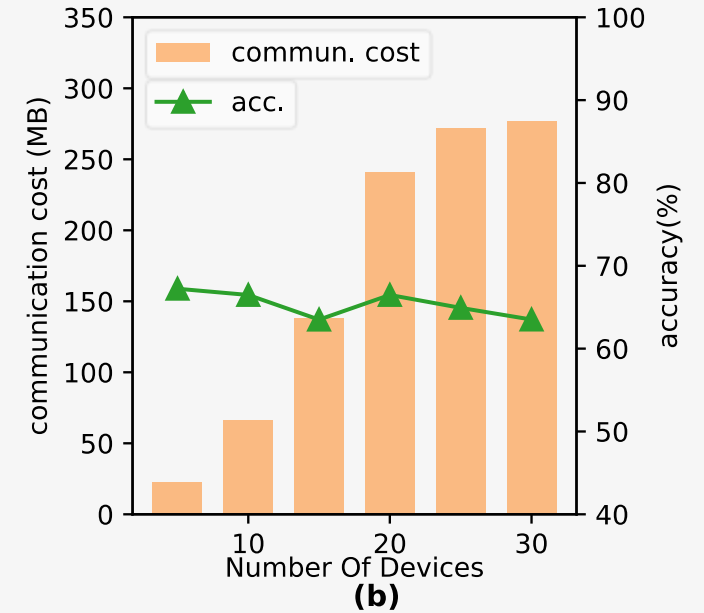
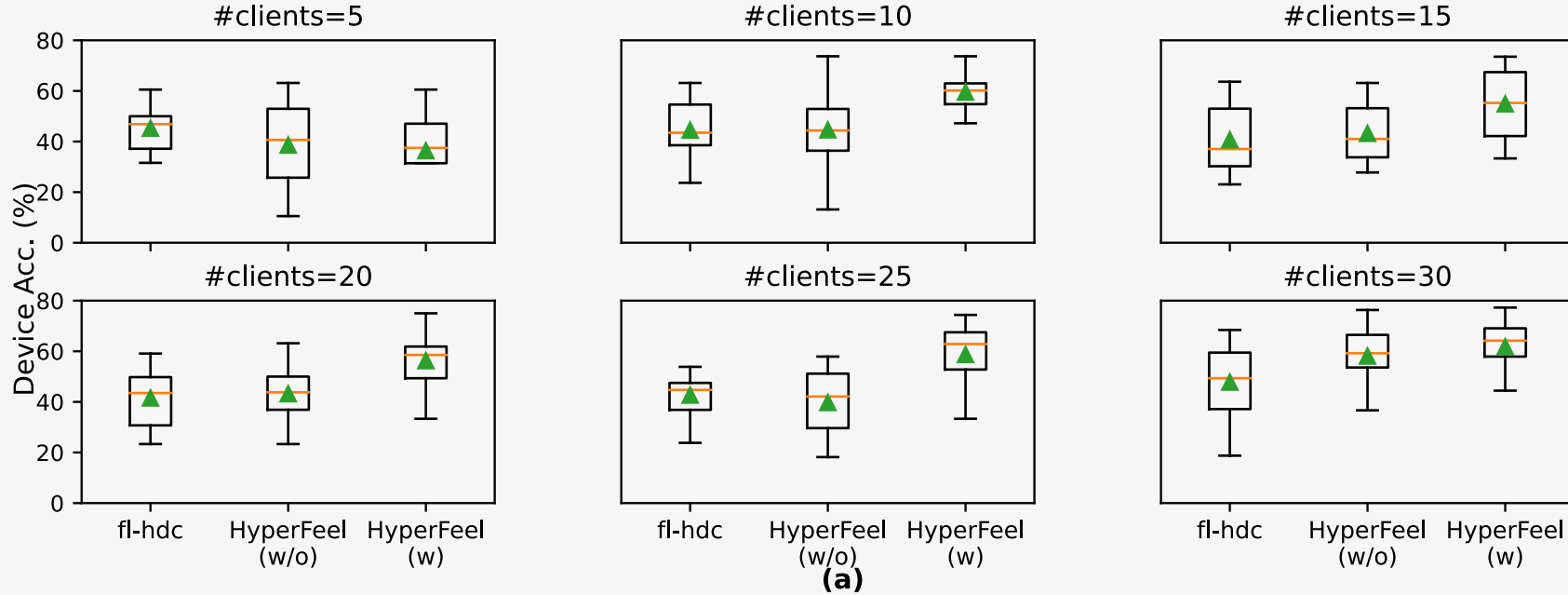


**Converge Faster**

bit-flip rate	1%	5%	10%	20%	30%
Accuracy	88.37%	88.00%	87.82%	87.80%	86.41%

**High Robustness**

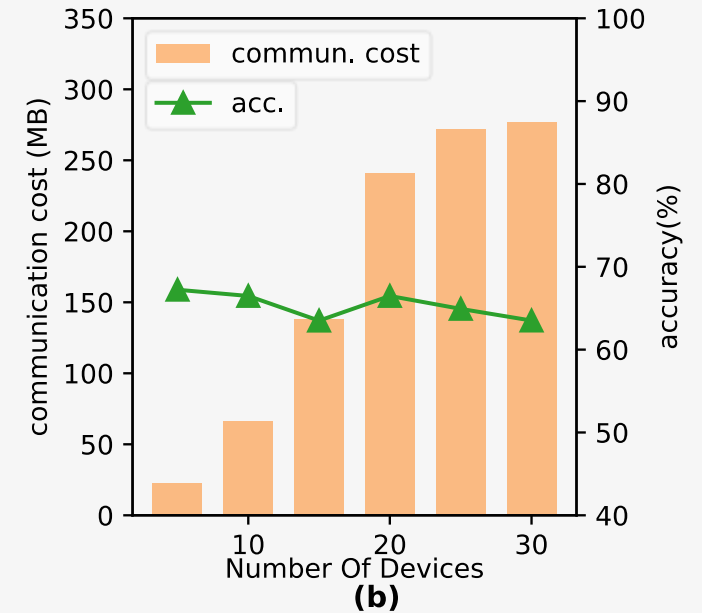
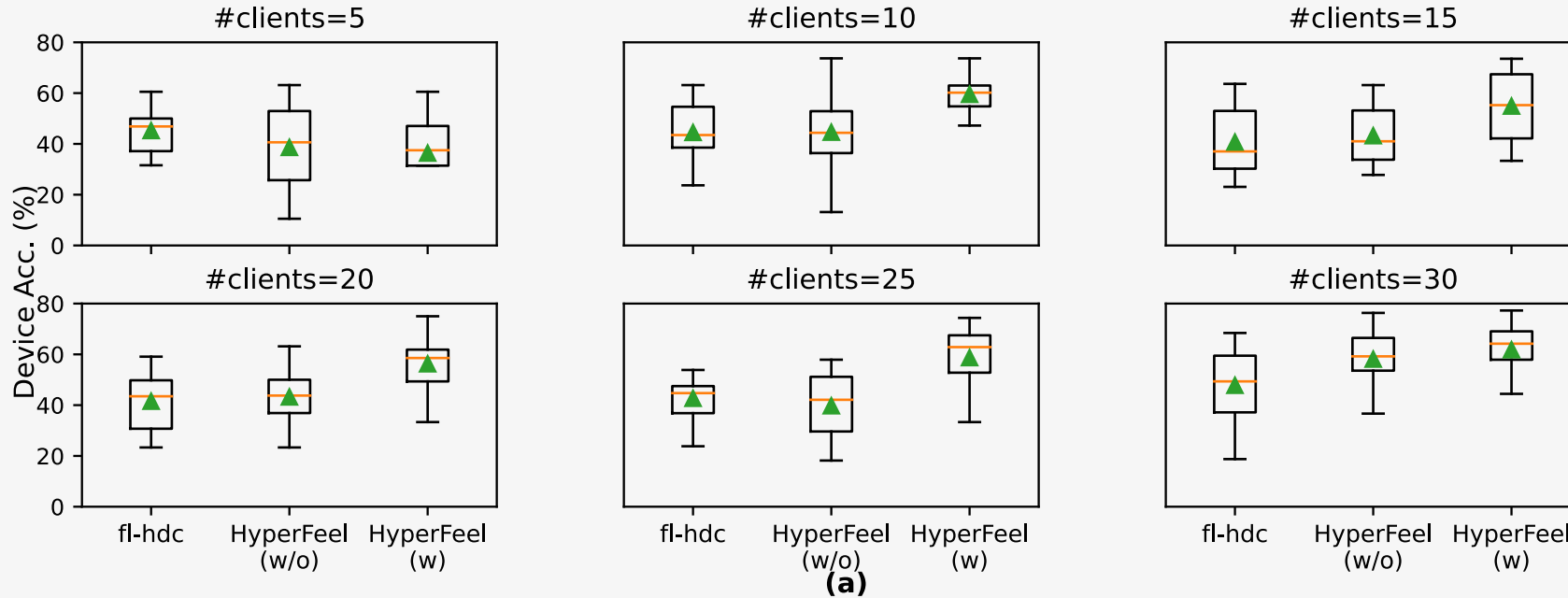
# Impact of non-IID data & #clients



**FL-HDC vs. HyperFeel (without personalization) vs. HyperFeel (with personalization)**



# Impact of non-IID data & #clients



**Accuracy of HyperFeel is barely affected by varying the number of client.**

**Average communication per client: 8MB**

**Average Storage per client: 240KB**

# Conclusion

🌀 A novel FL framework based on the HDC

🌀 Efficient

- Reduce storage cost
- Reduce communication cost

🌀 Accurate

- Personalization update strategy for non-iid data

🌀 General

- Fit for both horizon FL and vertical FL

# Thank you!

## HyperFeel: An Efficient Federated Learning Framework Using Hyperdimensional Computing

**Haomin Li (Speaker)**

Fangxin Liu, Yichi Chen, and Li Jiang\*

Shanghai Jiao Tong University

